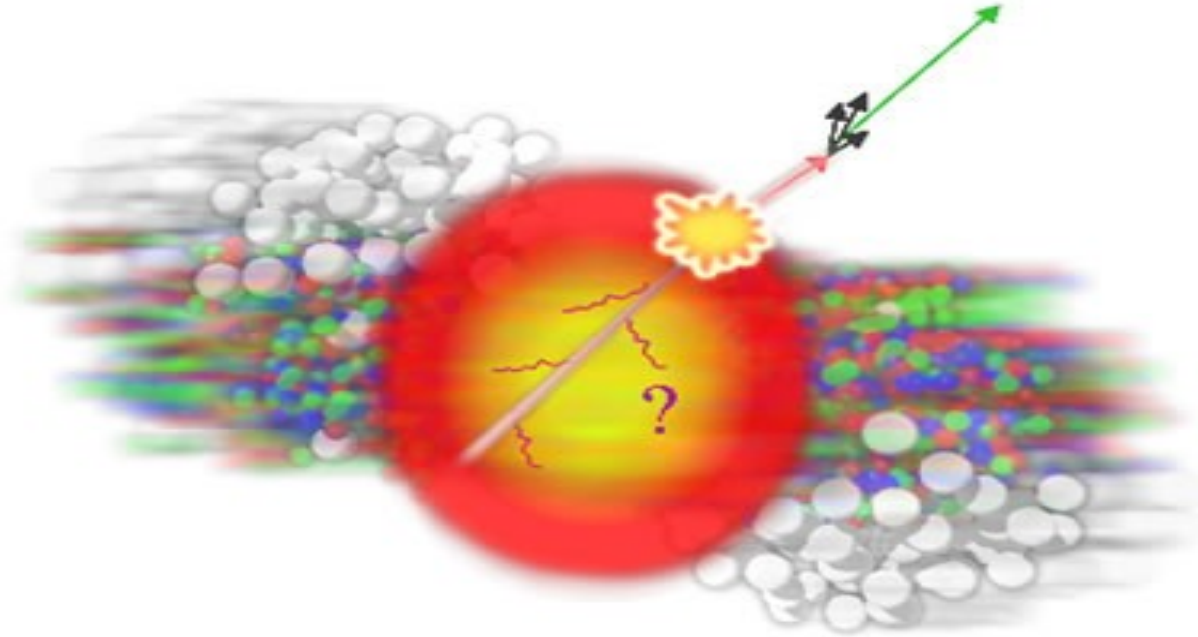


A skeptic's guide to jets

Part 1: Jet spectra



Christine Nattrass
University of Tennessee, Knoxville

Acknowledgements

The following people contributed ideas and/or slides, but of course I take full responsibility for anything you don't like:

Rosi Reed, Megan Connors, Sevil Salur

Abhijit Majumder, Raghav Kunnawalkam Elayavalli

Marta Verweij, Laura Havener

Austin Schmier, Charles Hughes, Will Witt

Questions an experimentalist should ask

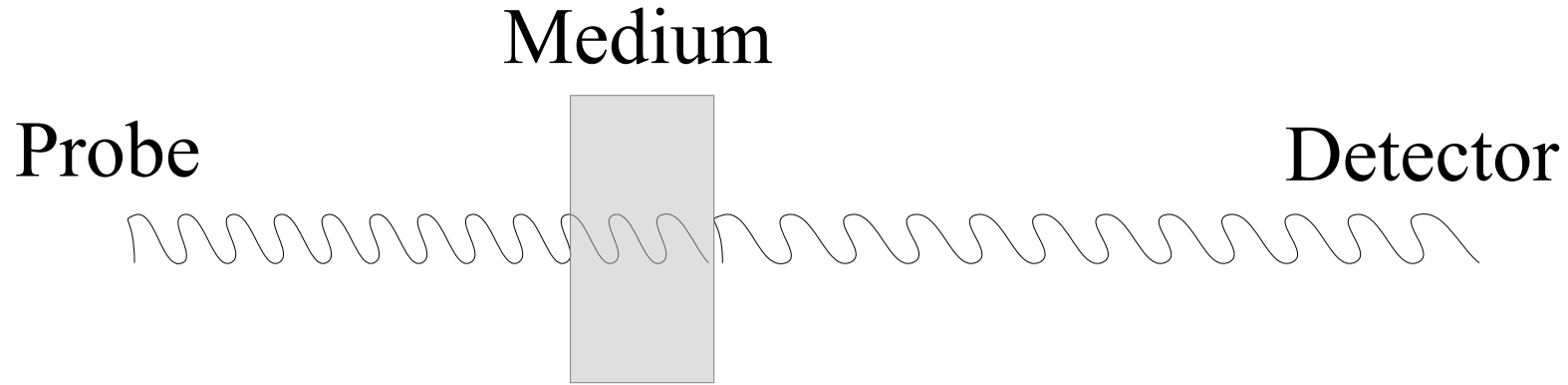
- What do I want to learn?
- What am I measuring?
- What assumptions am I making?
- What are the dominant uncertainties?
- How do I compare to models?

The answers for jets are highly non-trivial!

What do I want to learn? The cartoon picture



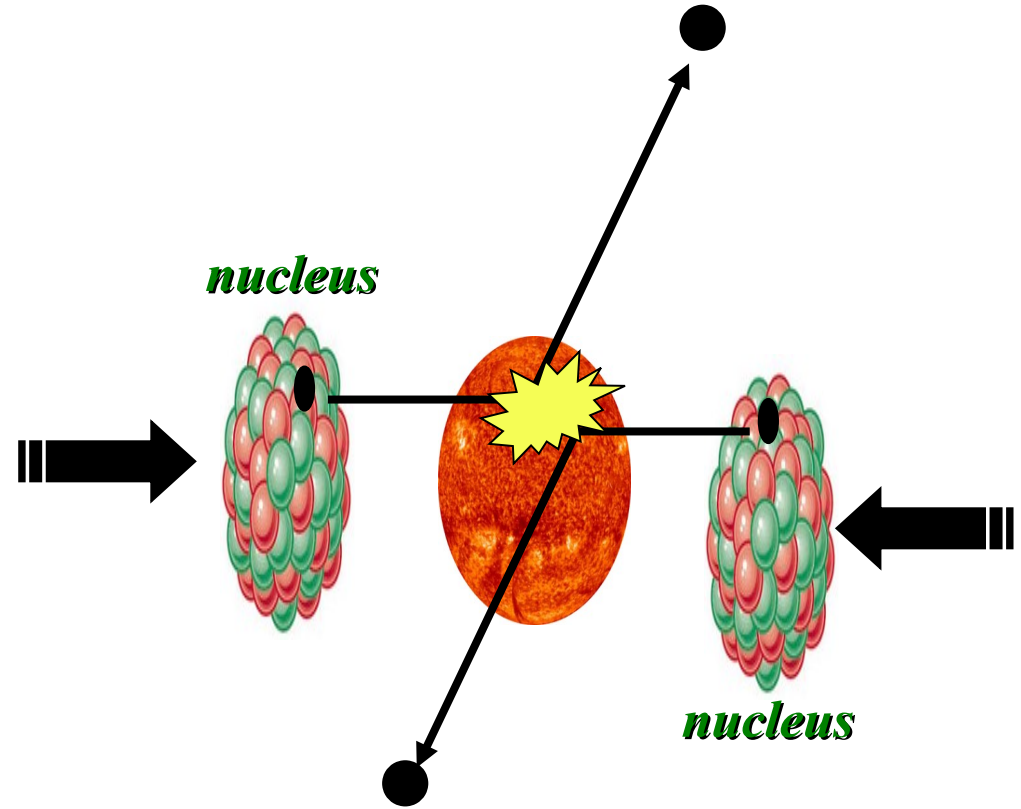
Probing the Quark Gluon Plasma



Want a probe which traveled through the collision
QGP is very short-lived ($\sim 1-10$ fm/c) \rightarrow
cannot use an external probe

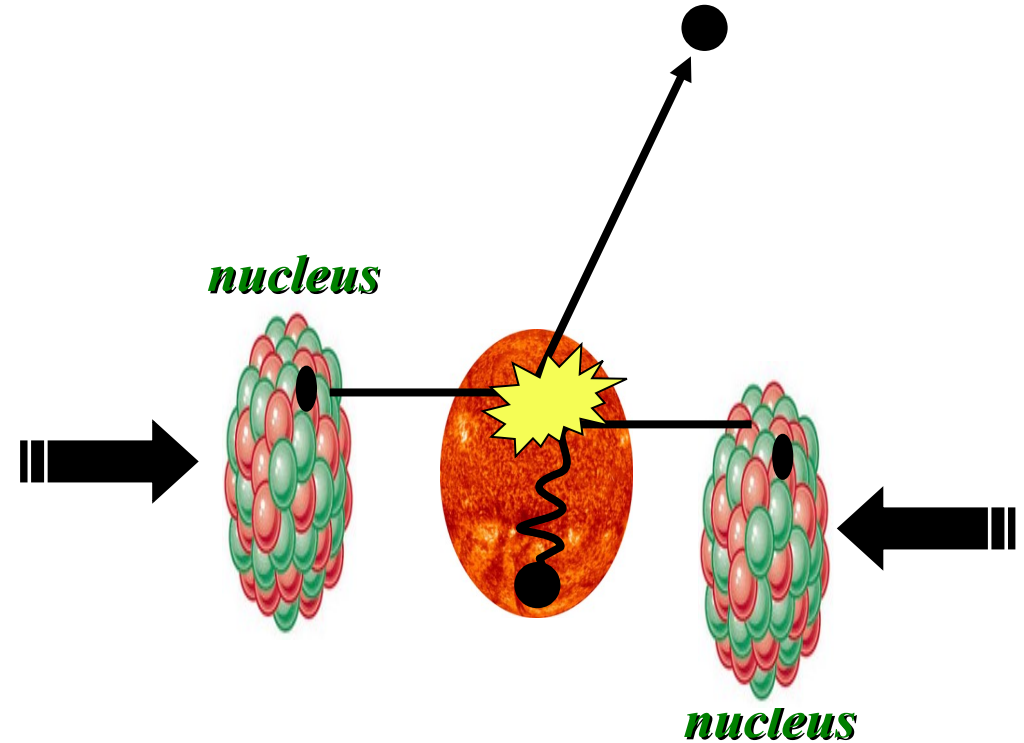
Probes of the Quark Gluon Plasma

Want a probe which traveled through the medium
QGP is short lived \rightarrow need a probe created in the collision



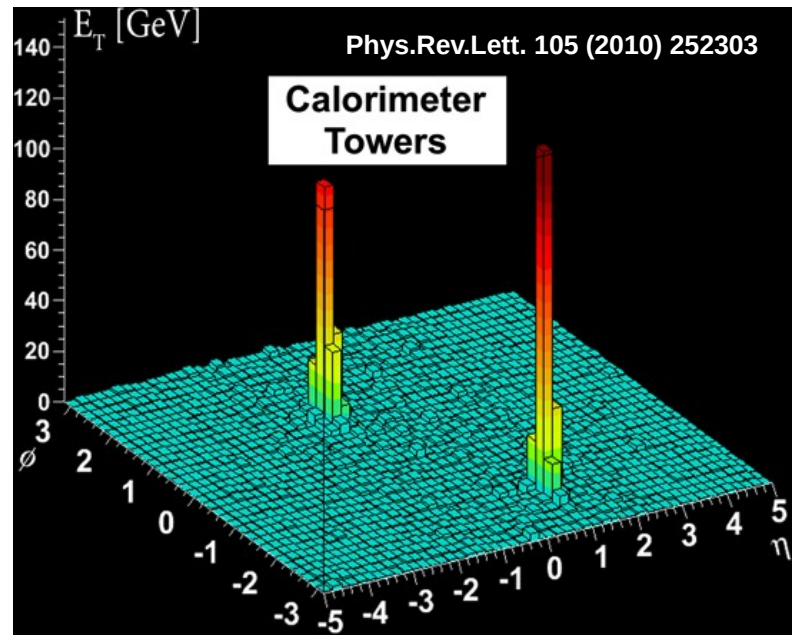
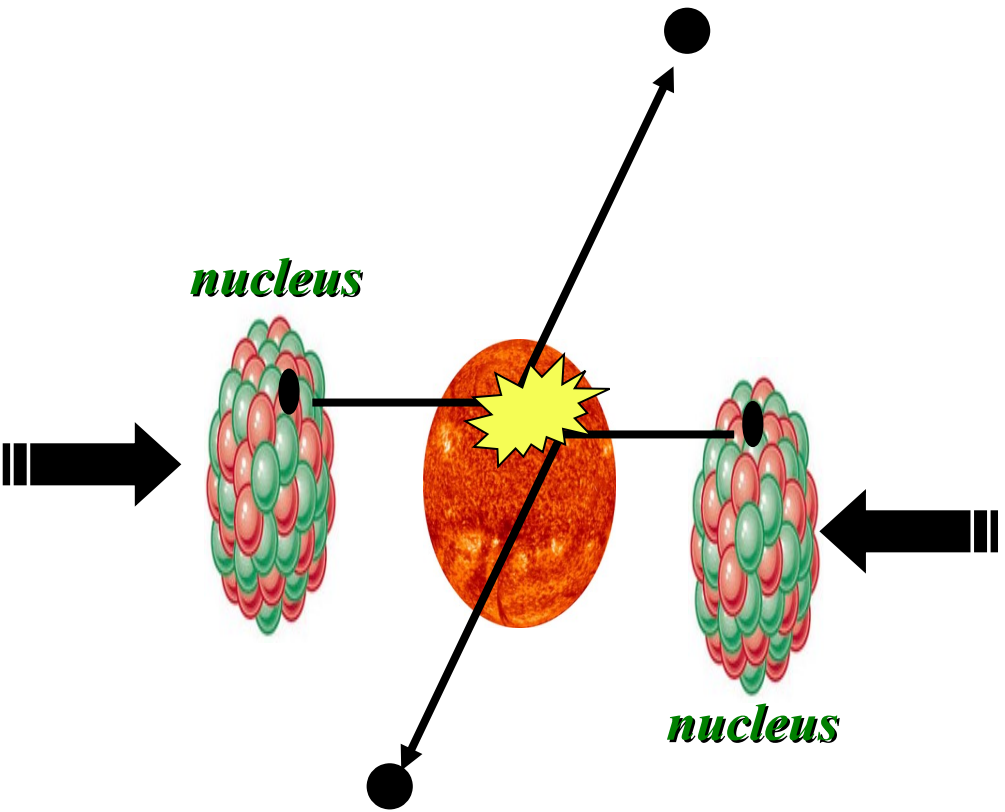
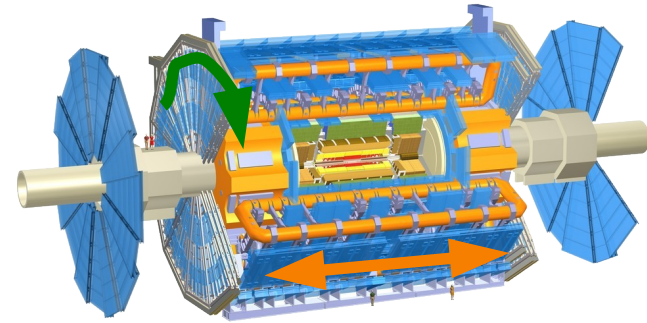
Probes of the Quark Gluon Plasma

Want a probe which traveled through the medium
QGP is short lived \rightarrow need a probe created in the collision
We expect the medium to be dense \rightarrow absorb/modify probe



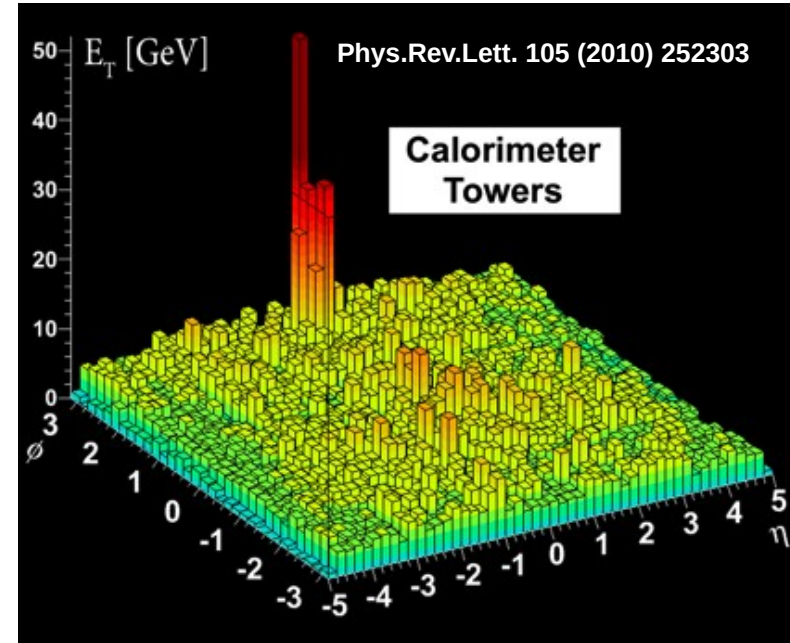
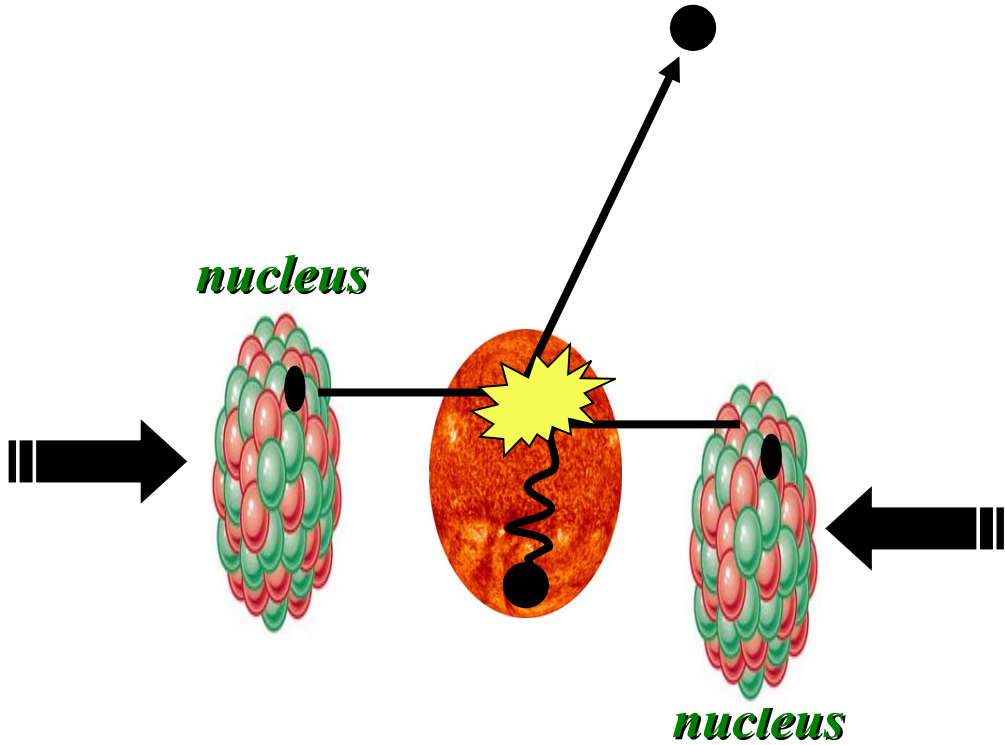
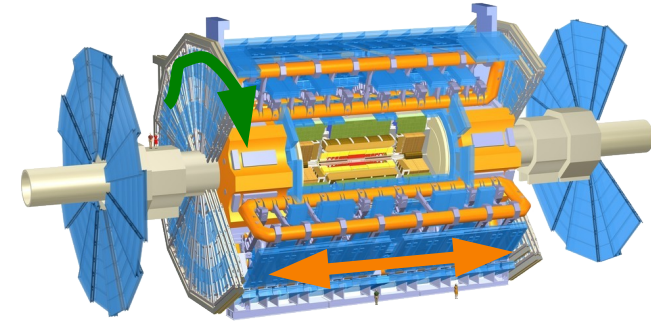
Probes of the Quark Gluon Plasma

ATLAS



Probes of the Quark Gluon Plasma

ATLAS

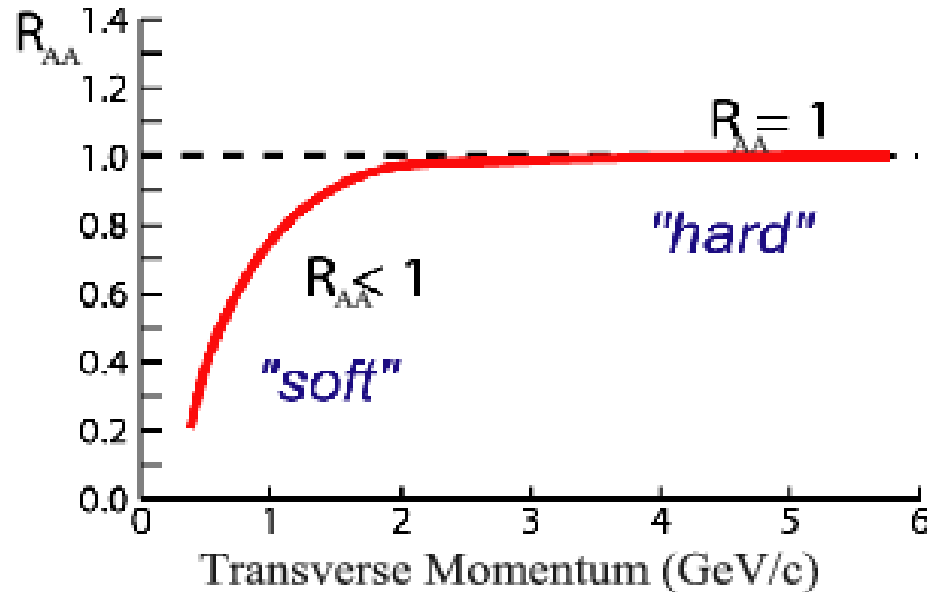


“Simple” example: Single hadrons

Nuclear modification factor

- Measure spectra of probe (jets) and compare to those in p+p collisions or peripheral A+A collisions
- If high- p_T probes (jets) are suppressed, this is evidence of jet quenching

$$R_{AA} = \frac{d^2 N_{AA}/dp_T d\eta}{T_{AA} d^2 \sigma^{pp}/dp_T d\eta}$$



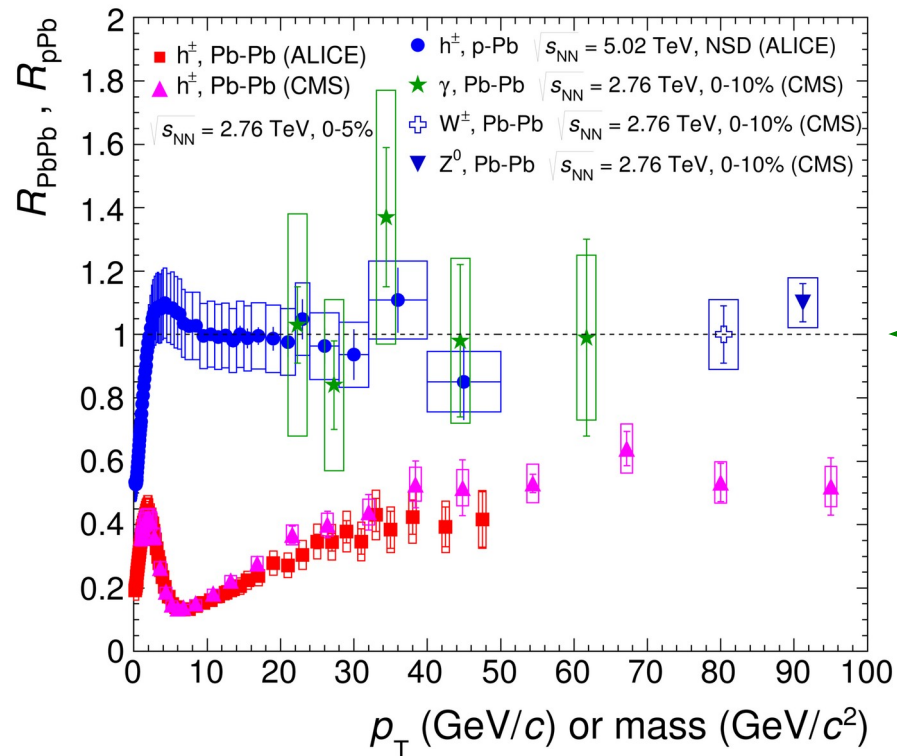
Enhancement

Suppression

Nuclear modification factor

Control →

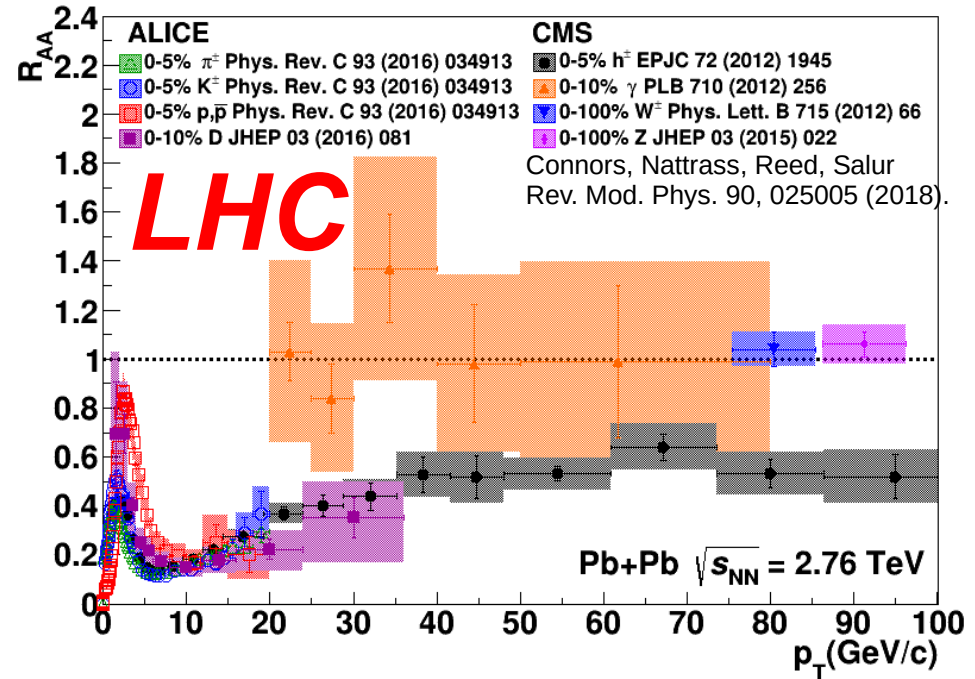
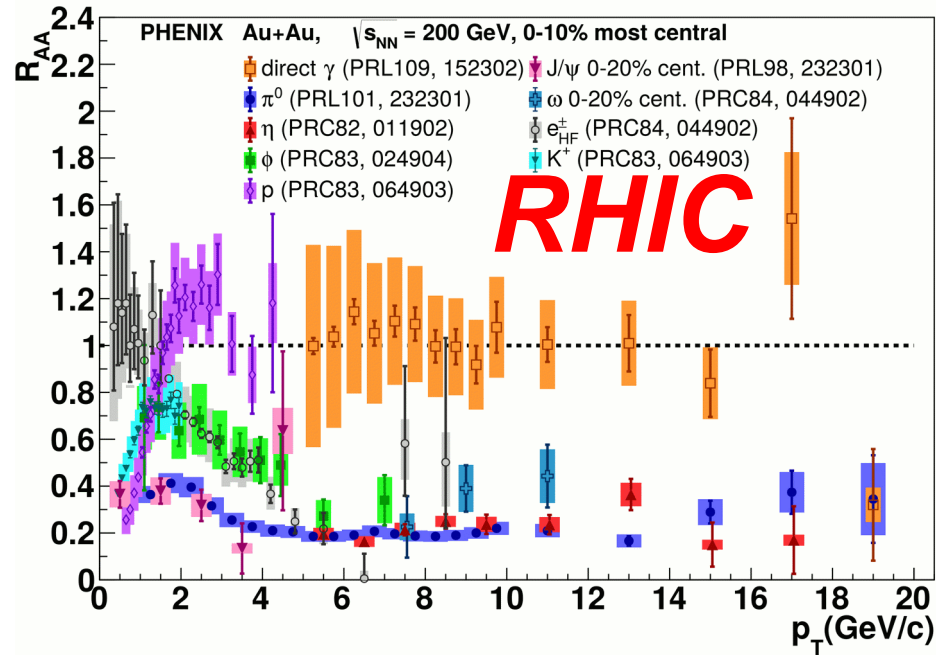
Probe →



← **Control**

- Charged hadrons (colored probes) suppressed in Pb—Pb
- Charged hadrons not suppressed in p—Pb at midrapidity
- Electroweak probes not suppressed in Pb—Pb

Nuclear modification factor R_{AA}



Electromagnetic probes – consistent with no modification – medium is transparent to them

Strong probes – significant suppression – medium is opaque to them
- even heavy quarks!

What am I measuring?
Definition of a jet

Theoretical calculations

Factorization theorem

- Assumption: Parton distribution functions, perturbative cross section, fragmentation function factorize
- What people really mean by “perturbatively calculable”
 - D and f are *explicitly non-perturbative!*
 - D is for $\text{parton } c \rightarrow \text{hadron } h$
Not what is experimentally measured
- Most theories for jet quenching modify fragmentation function D

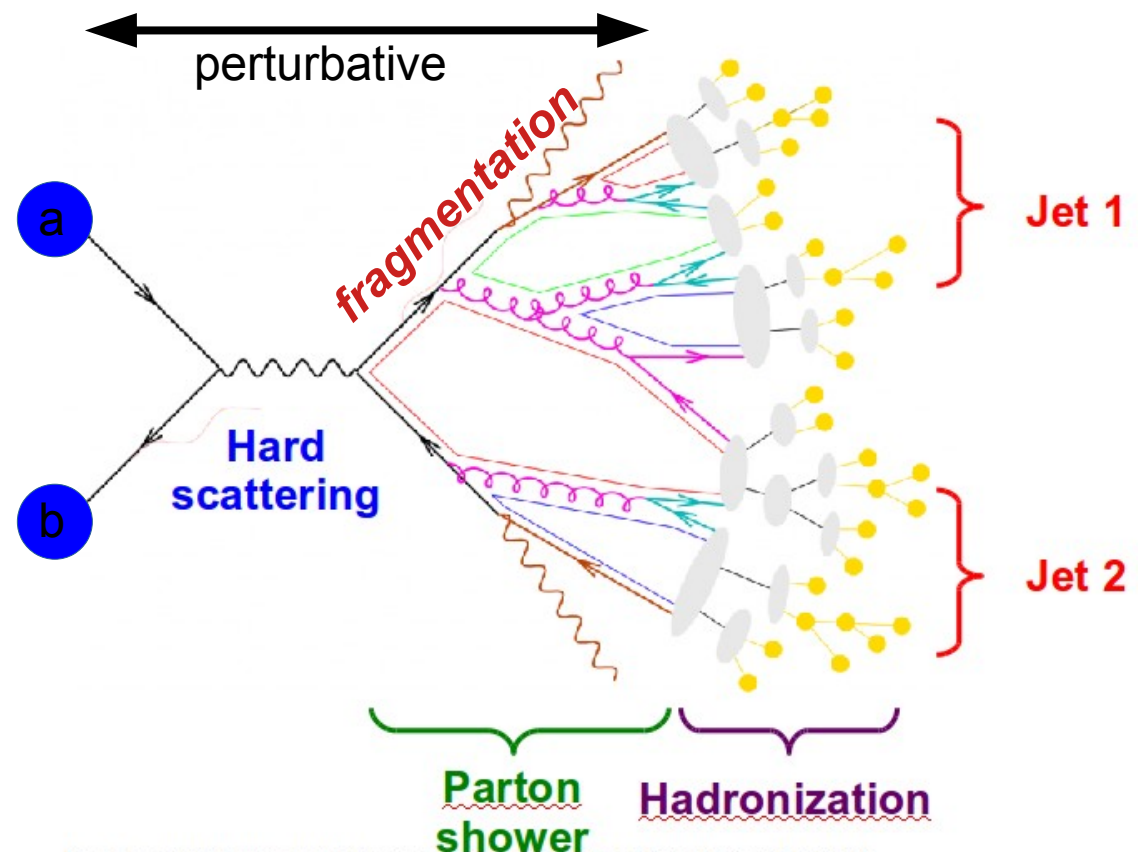


Image from <http://www.gk-eichtheorien.physik.uni-mainz.de/Dateien/Zeppenfeld-3.pdf>

$$\frac{d^3 \sigma^h}{dy d^2 p_T} = \frac{1}{\pi} \int d x_a \int d x_b f_a^A(x_a) f_b^B(x_b) \frac{d \sigma_{ab \rightarrow cX}}{d \hat{t}} \frac{D_c^h(z)}{z}$$

Jet finders

What is a jet?

What is a jet?

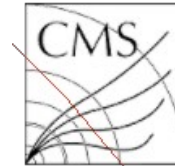
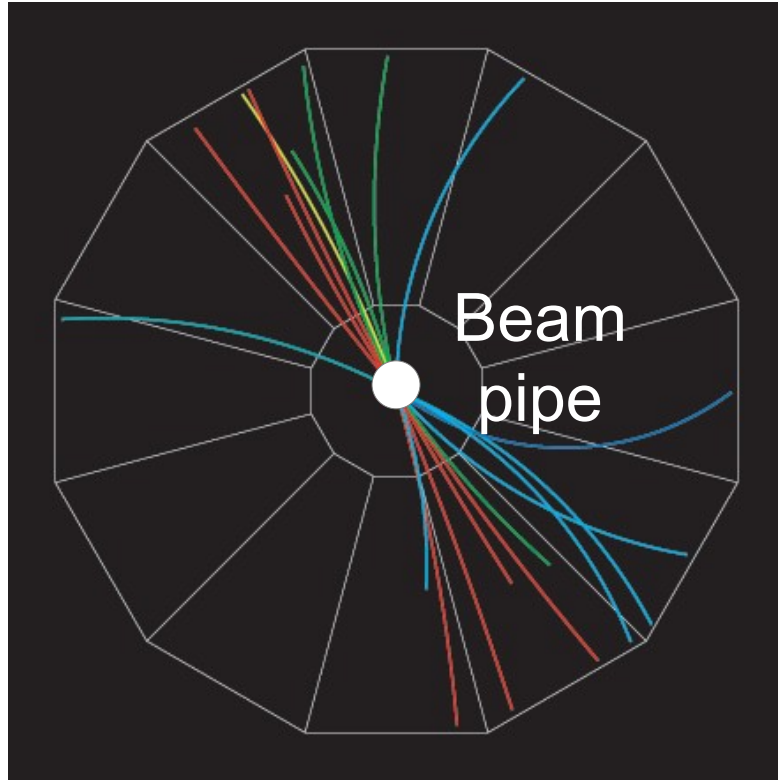
A measurement of a jet is a measurement of a parton.

What is a jet?

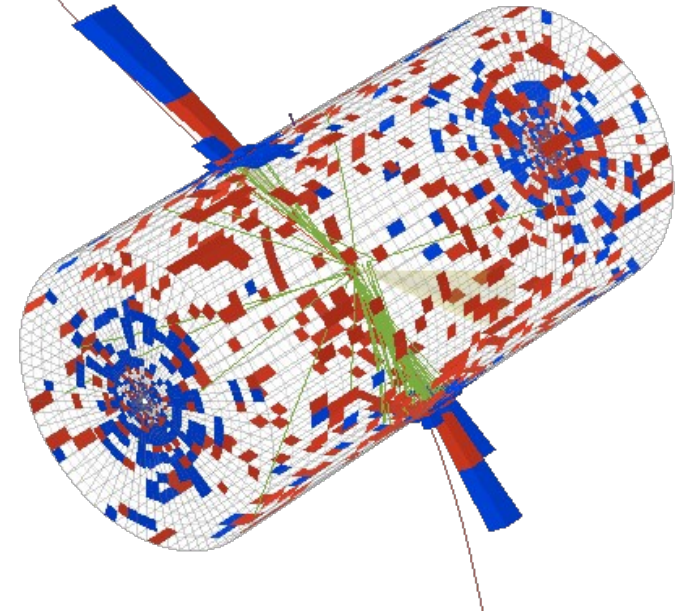
~~A measurement of a jet is a measurement of a
parton.~~

What is a jet?

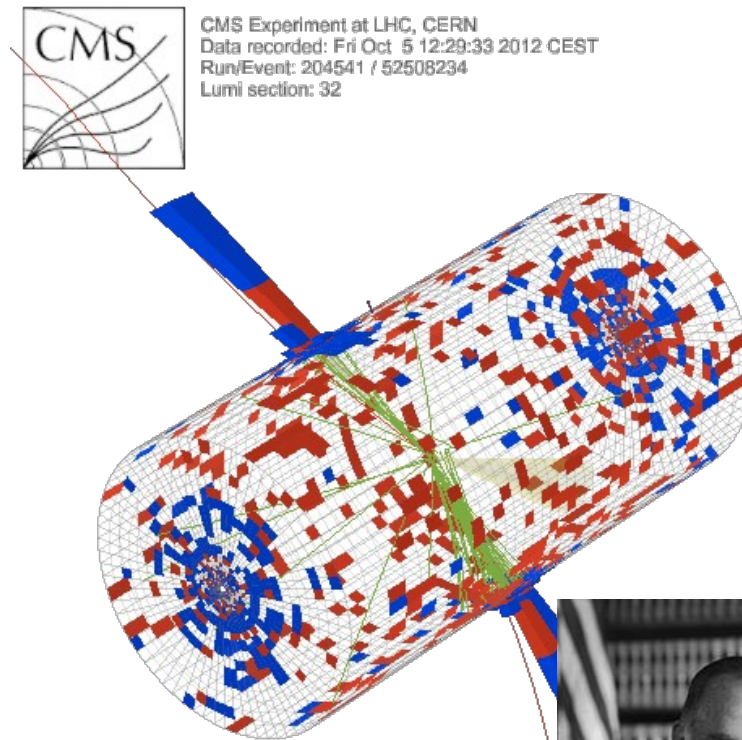
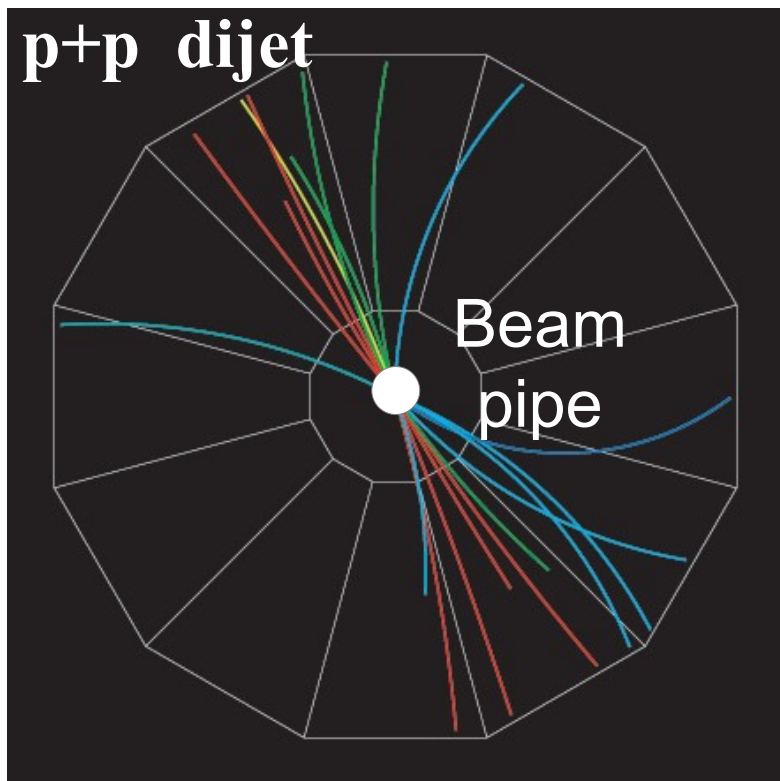
p+p dijet



CMS Experiment at LHC, CERN
Data recorded: Fri Oct 5 12:29:33 2012 CEST
Run/Event: 204541 / 52508234
Lumi section: 32

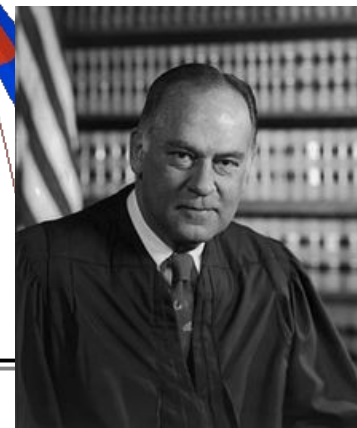


What is a jet?

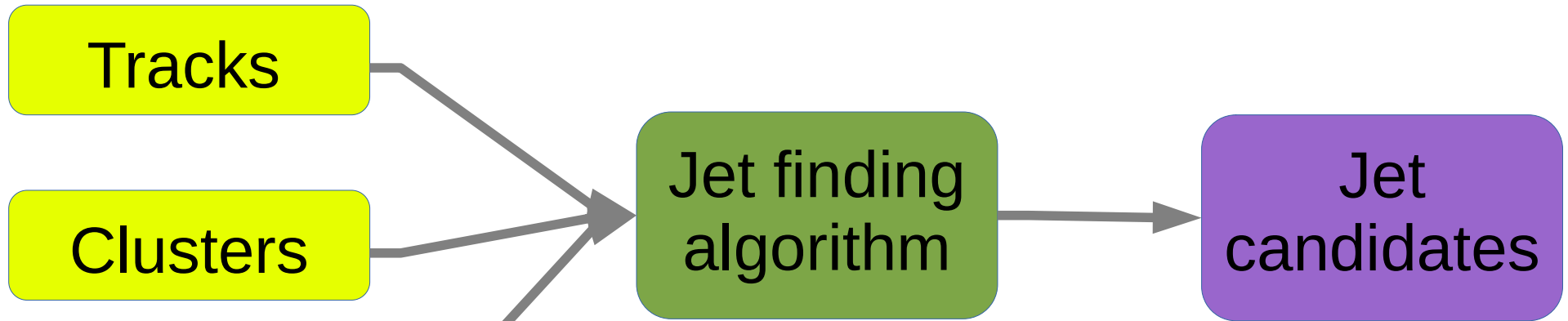


“I know it when I see it”

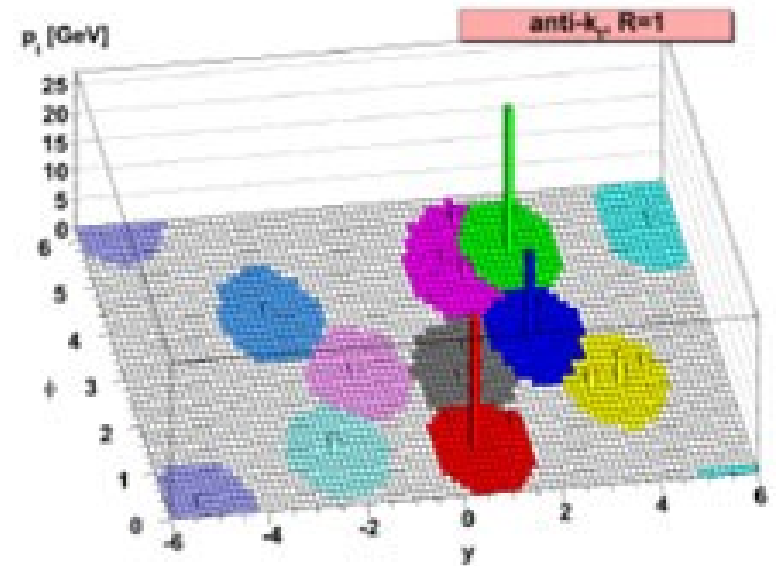
US Supreme Court Justice Potter Stewart, *Jacobellis v. Ohio*



Jet finding algorithms



- Any list of objects works as input
- Use the same algorithm on theory & experiment
- Output only as good as input



Jet finding *in pp collisions*

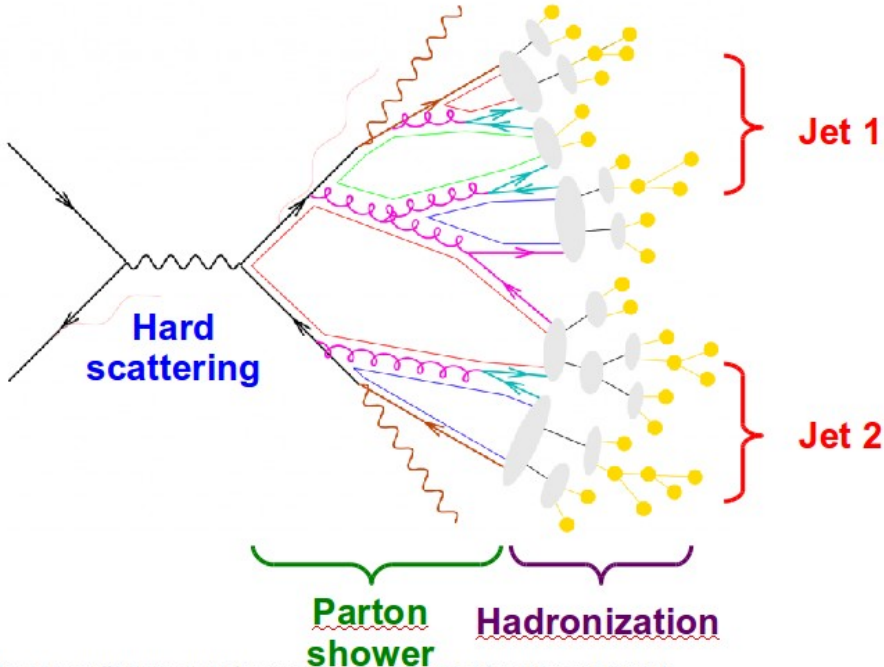
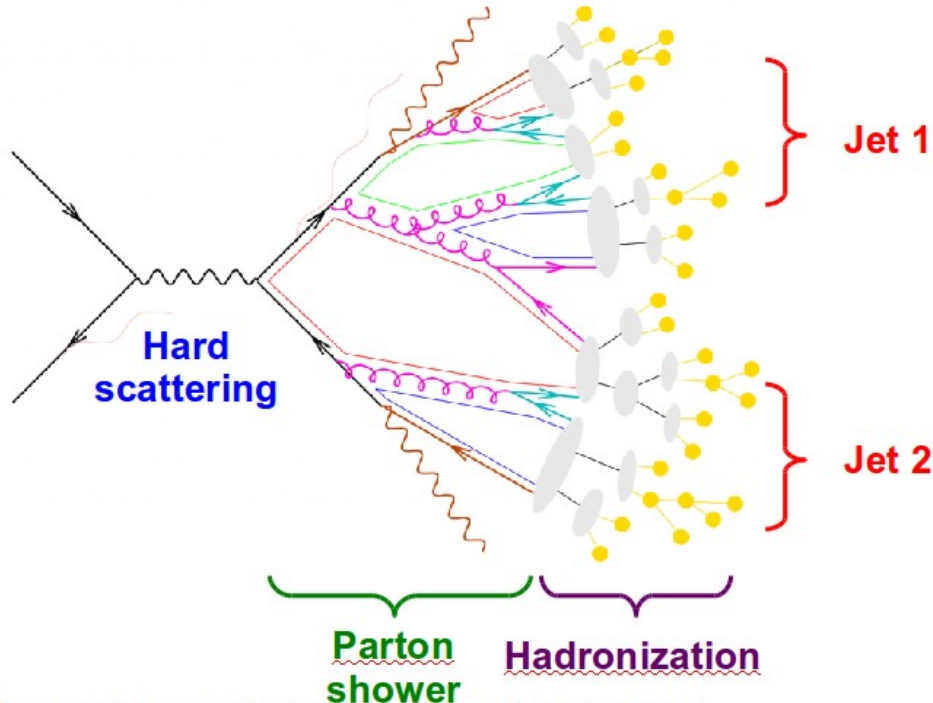


Image from <http://www.gk-eichtheorien.physik.uni-mainz.de/Dateien/Zeppenfeld-3.pdf>

- Jet finder: groups final state particles into jet candidates
 - Anti- k_T algorithm
[JHEP 0804 \(2008\) 063 \[arXiv:0802.1189\]](#)
- Depends on hadronization
- Ideally
 - Infrared safe
 - Collinear safe

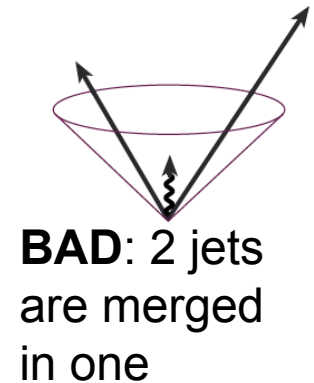
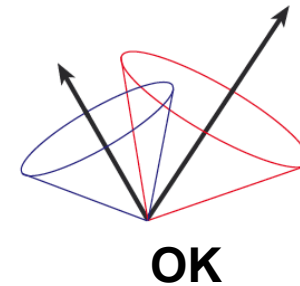
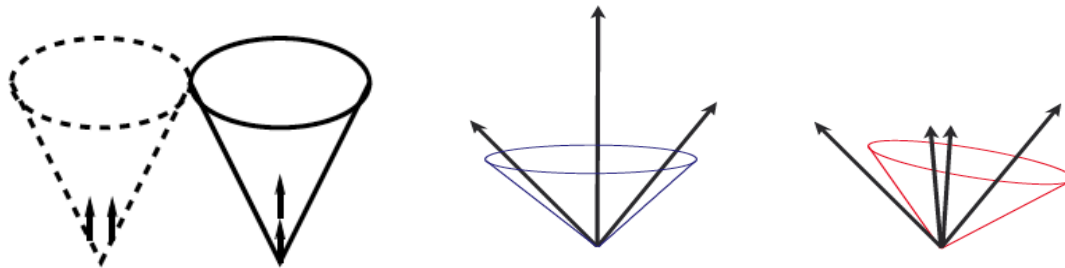
Snowmass Accord: Theoretical calculations and experimental measurements should use the same jet finding algorithm. Otherwise they will not be comparable.

Jets in principle



- Jet measures **partons**
- Hadronic degrees of freedom are integrated out
- Algorithms are infrared and collinear safe

Image from <http://www.gk-eichtheorien.physik.uni-mainz.de/Dateien/Zepfenfeld-3.pdf>



k_T jet finding algorithm

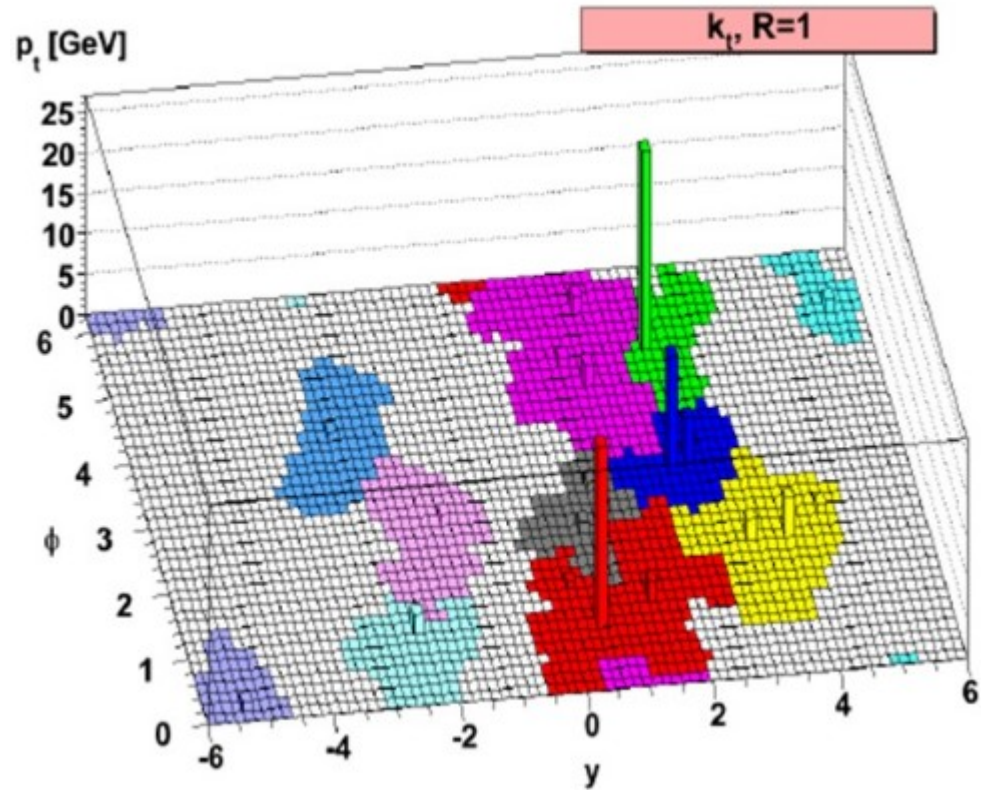
Particles, clusters

k_T algorithm

$$k_T = p_T, \Delta R_{ij} = \sqrt{(\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2}$$

- For all i, j calculate:
$$d_{ij} = \min(p_{T,i}^2, p_{T,j}^2) \frac{\Delta R_{ij}^2}{R^2}$$
 - $d_{iB} = p_{T,i}^2$
 - Combine smallest d_{ij} .
If d_{iB} smallest, $d_{iB} \rightarrow$ jet
- Repeat until no particles left

Jet candidates



anti- k_T jet finding algorithm

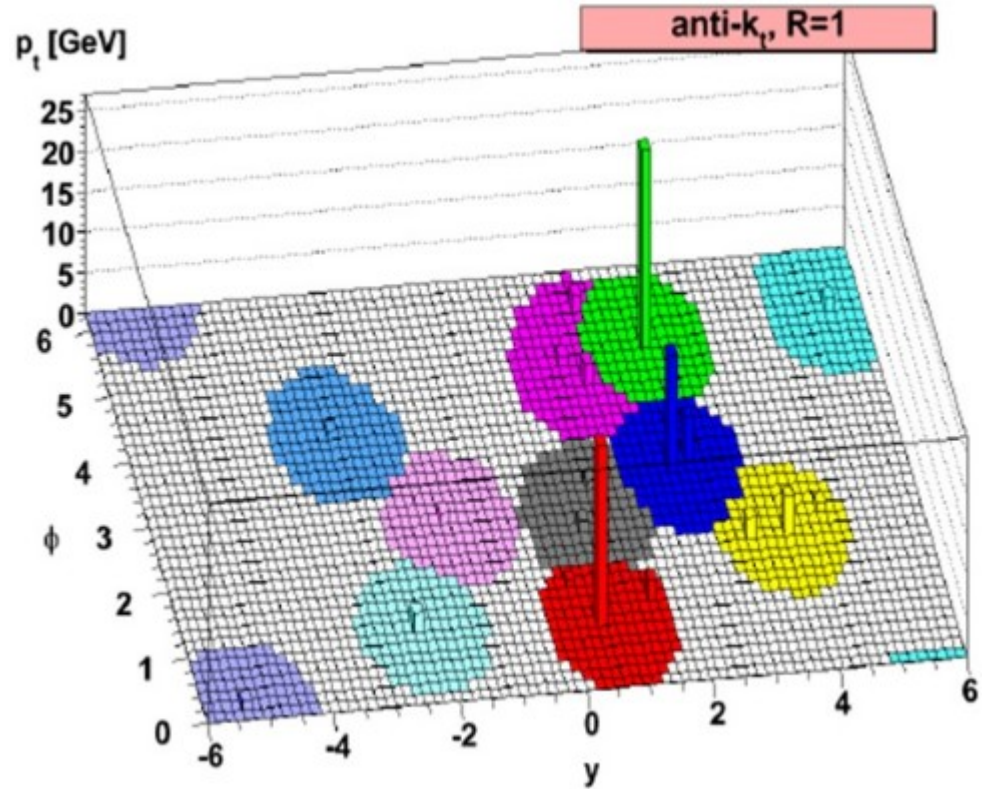
Particles, clusters

k_T algorithm

$$k_T = p_T, \Delta R_{ij} = \sqrt{(\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2}$$

- For all i, j calculate:
$$d_{ij} = \min(p_{T,i}^{-2}, p_{T,j}^{-2}) \frac{\Delta R_{ij}^2}{R^2}$$
 - $d_{iB} = p_{T,i}^{-2}$
 - Combine smallest d_{ij} .
If d_{iB} smallest, $d_{iB} \rightarrow$ jet
- Repeat until no particles left

Jet candidates



Cambridge/Aachen jet finding algorithm

Particles, clusters

k_T algorithm

$$k_T = p_T, \Delta R_{ij} = \sqrt{(\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2}$$

- For all i, j calculate:

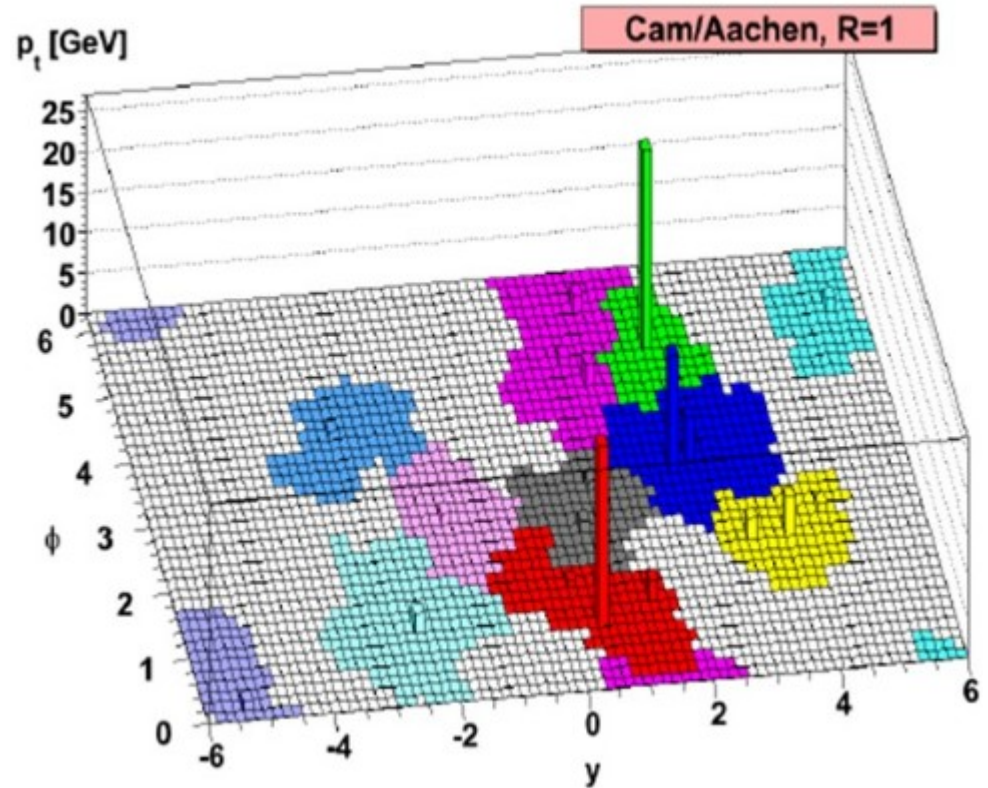
$$d_{iB} = 1 \quad d_{ij} = \frac{\Delta R_{ij}^2}{R^2}$$

- Combine smallest d_{ij} .

If d_{iB} smallest, $d_{iB} \rightarrow$ jet

Repeat until no particles left

Jet candidates



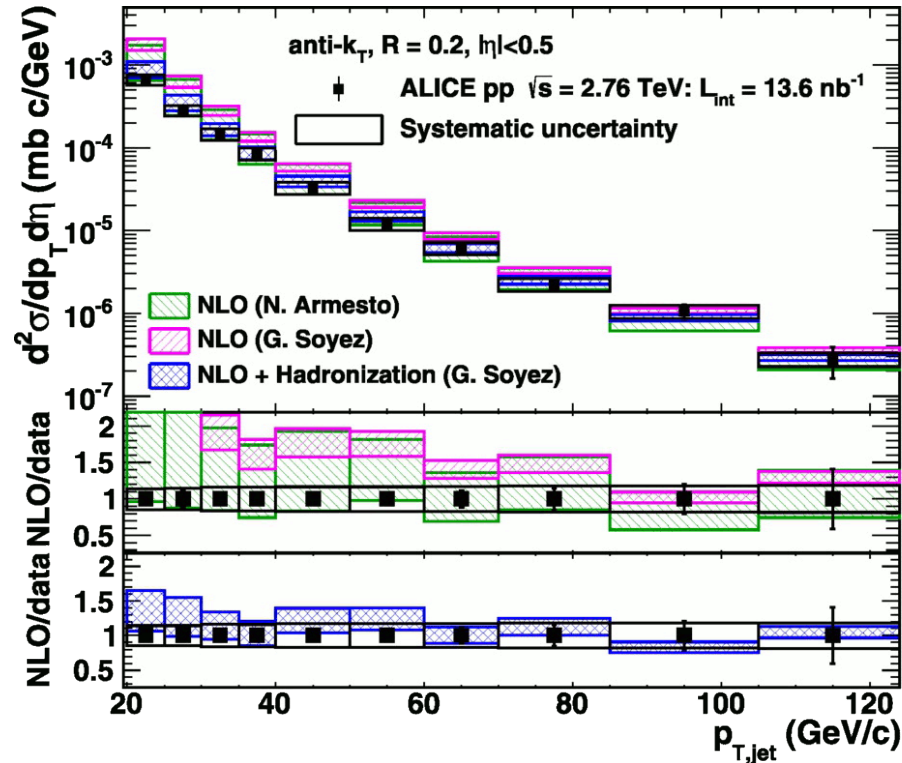
A jet is what a jet finder finds.

Jet cross-section in pp

$\sqrt{s} = 2.76$ TeV, $R = 0.2$ Inclusive

arXiv:1301.3475

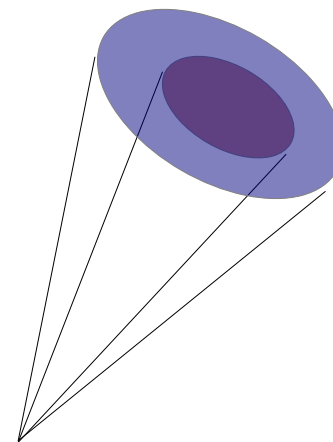
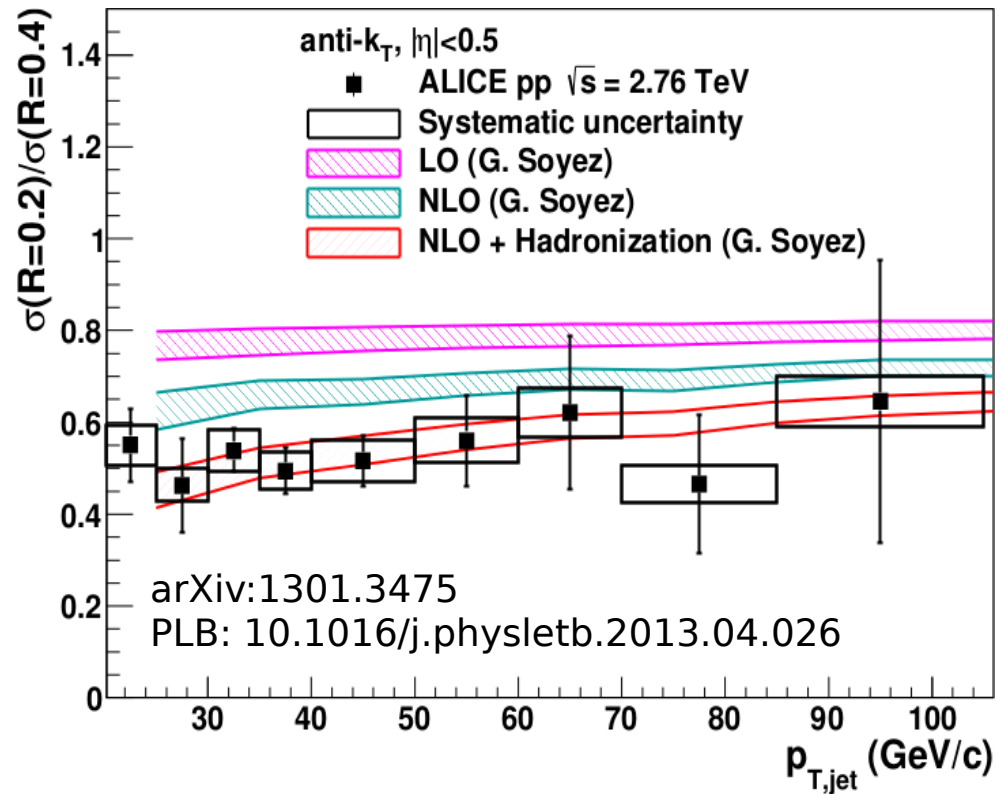
PLB: 10.1016/j.physletb.2013.04.026



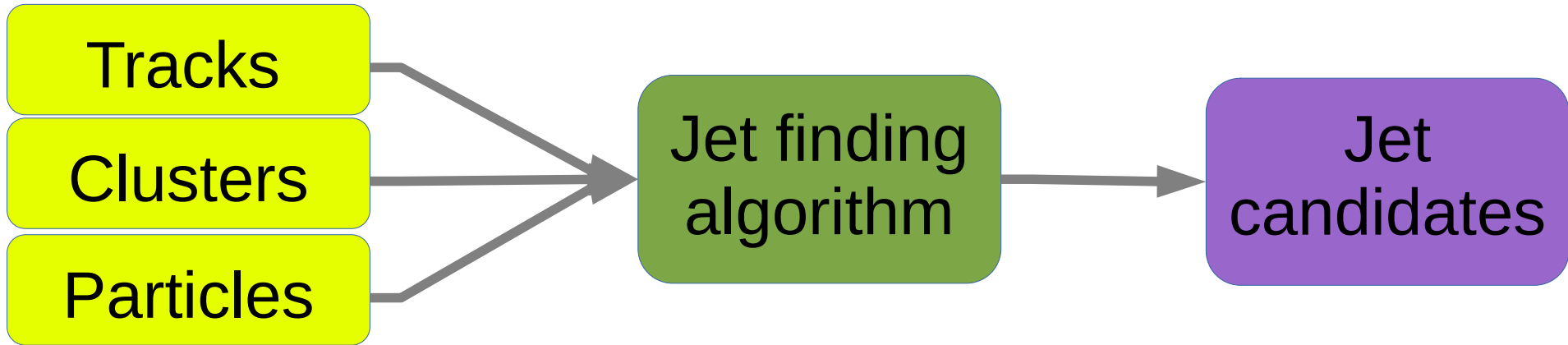
- Green and magenta bands: NLO on Parton level
- Blue band: NLO + hadronization
- Hadronization calculations necessary to describe data

Jet ratios in pp

$\sqrt{s} = 2.76$ TeV, $R = 0.2, 0.4$ Inclusive



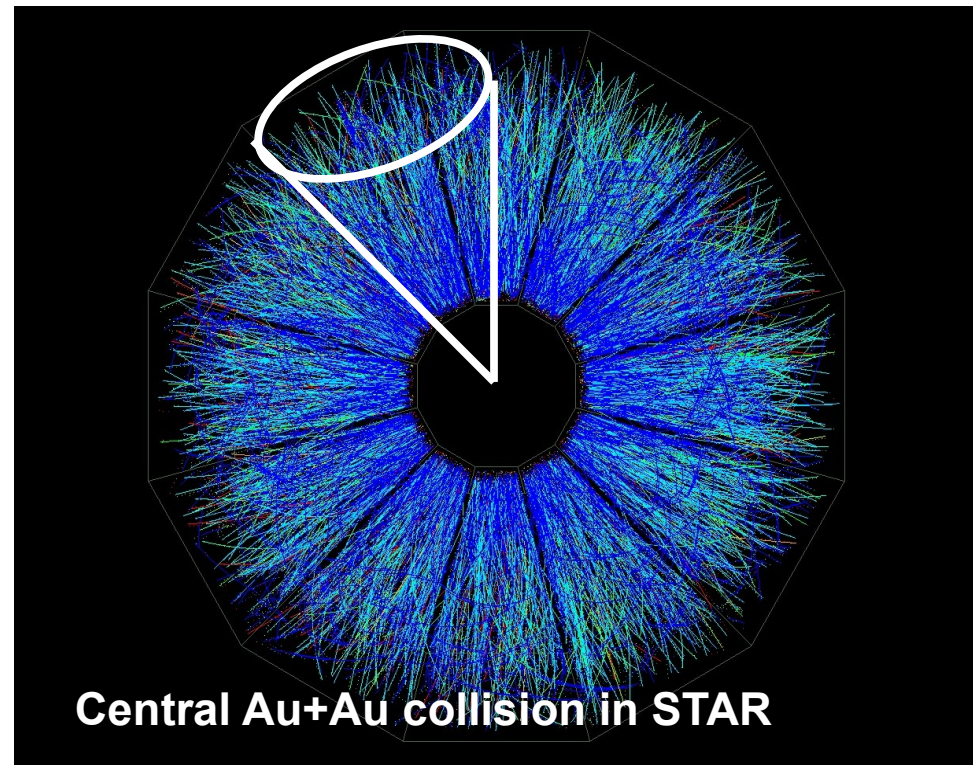
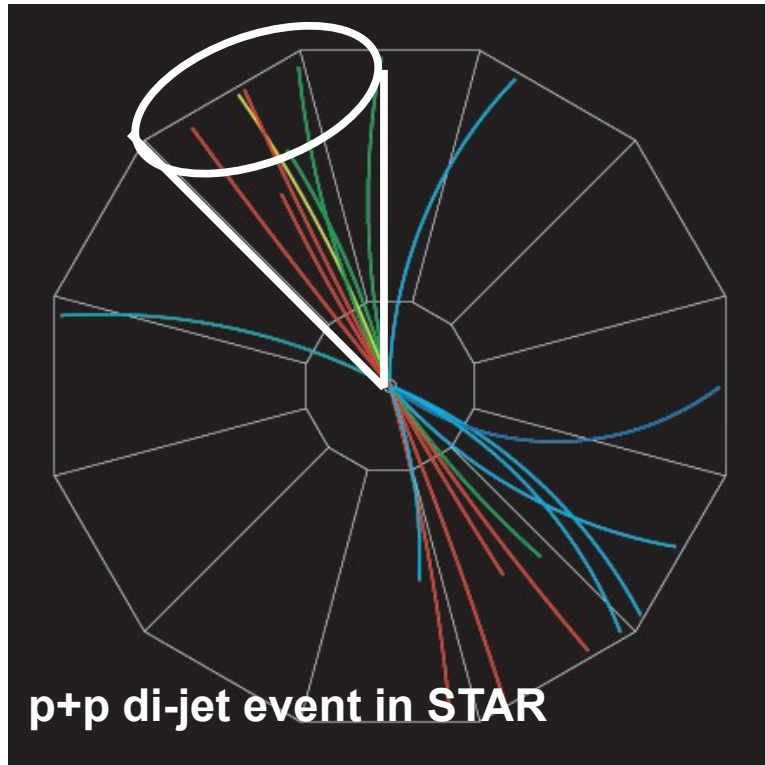
Mini-summary



- Jets are not partons
- Good jet finders:
 - Infrared and collinear safe
 - k_T , anti- k_T , Cambridge/Aachen, SIScone
- Jet is defined by jet finder, its parameters
- PDFs, fragmentation functions non-perturbative
→ all jet measurements sensitive to somewhat non-perturbative effects
- Good agreement between theory and experiment

Jets in A+A collisions
What assumptions am I making?

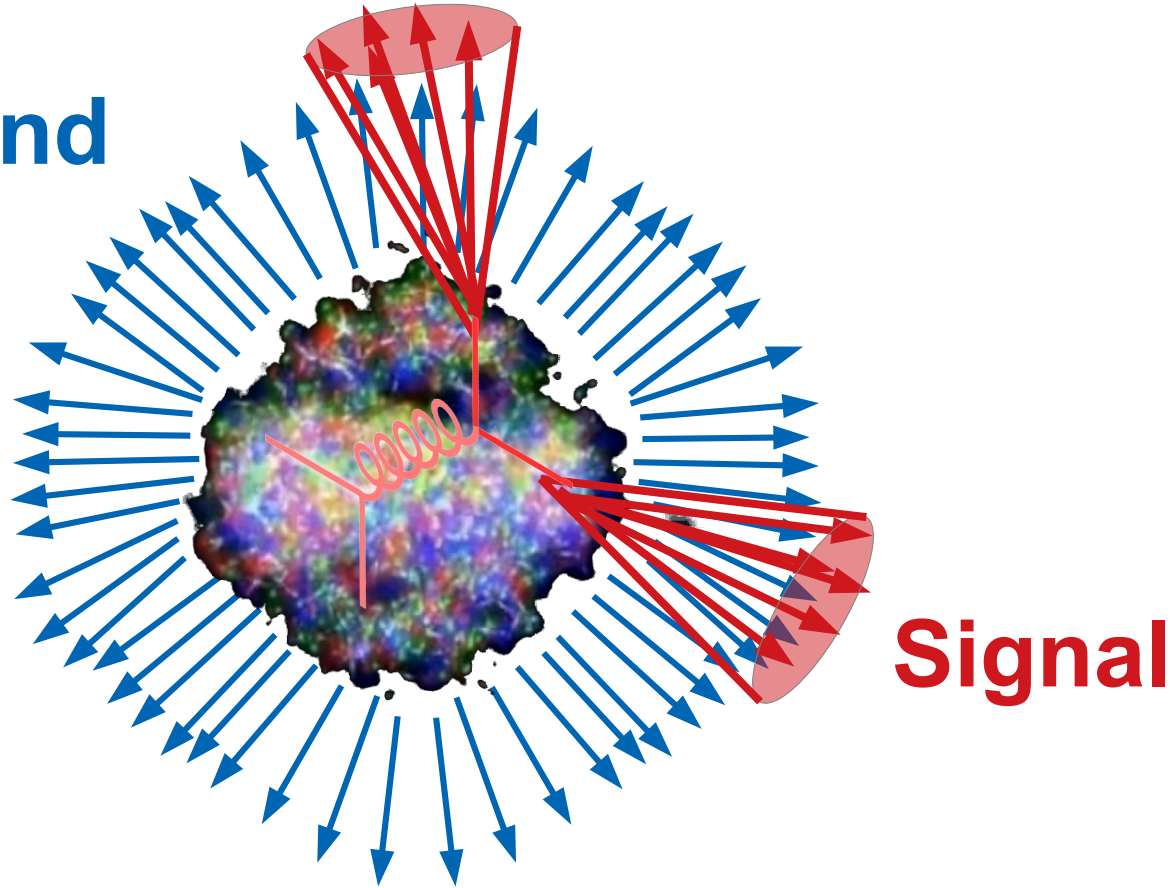
p+p vs A+A



Signal vs Background:

The standard paradigm

Background

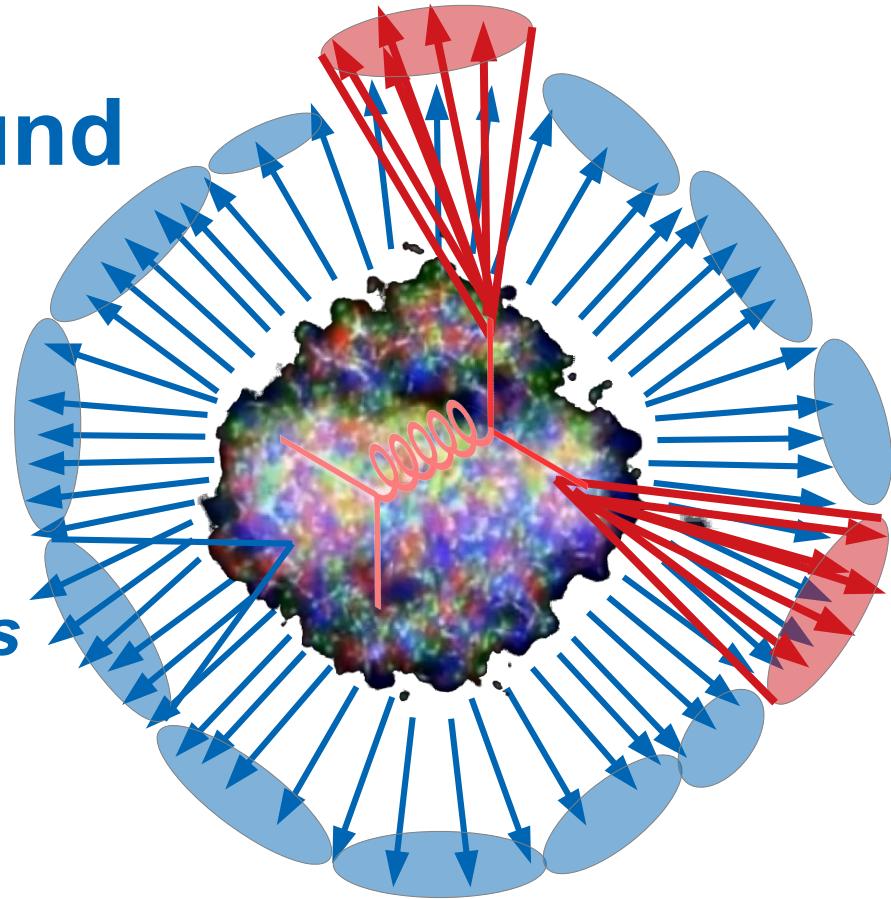


Signal vs Background:

The standard paradigm

Background

Combinatorial jets



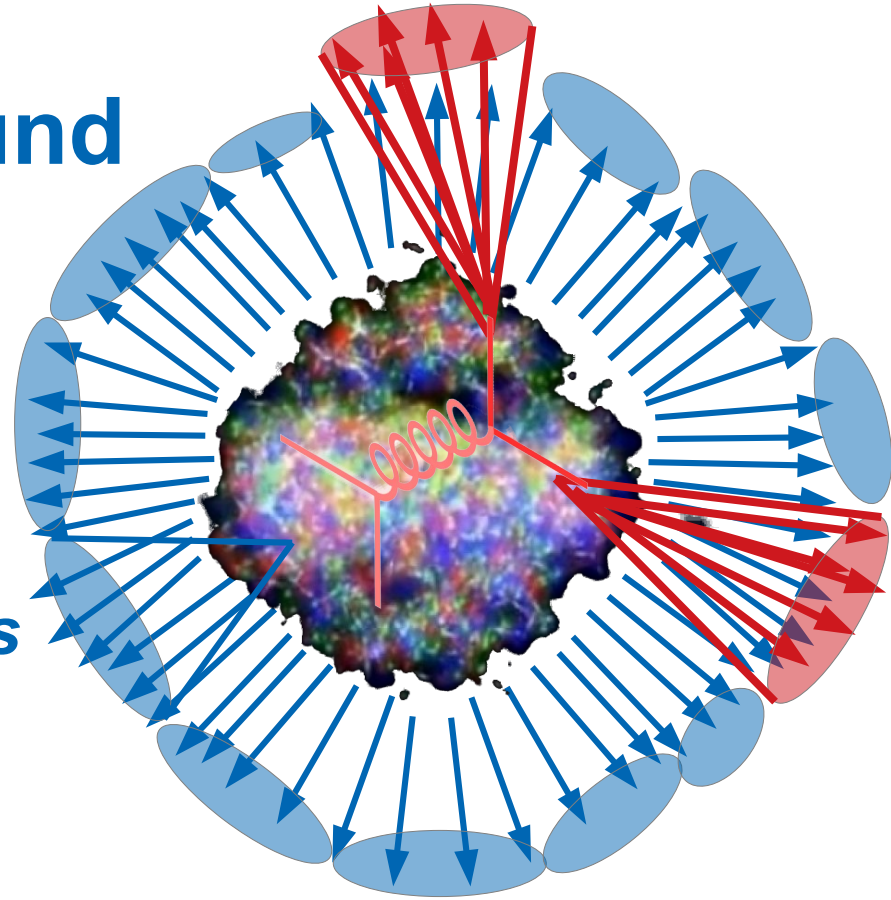
Signal

Signal vs Background:

The standard paradigm

Background

**Combinatorial jets
= “fake” jets**



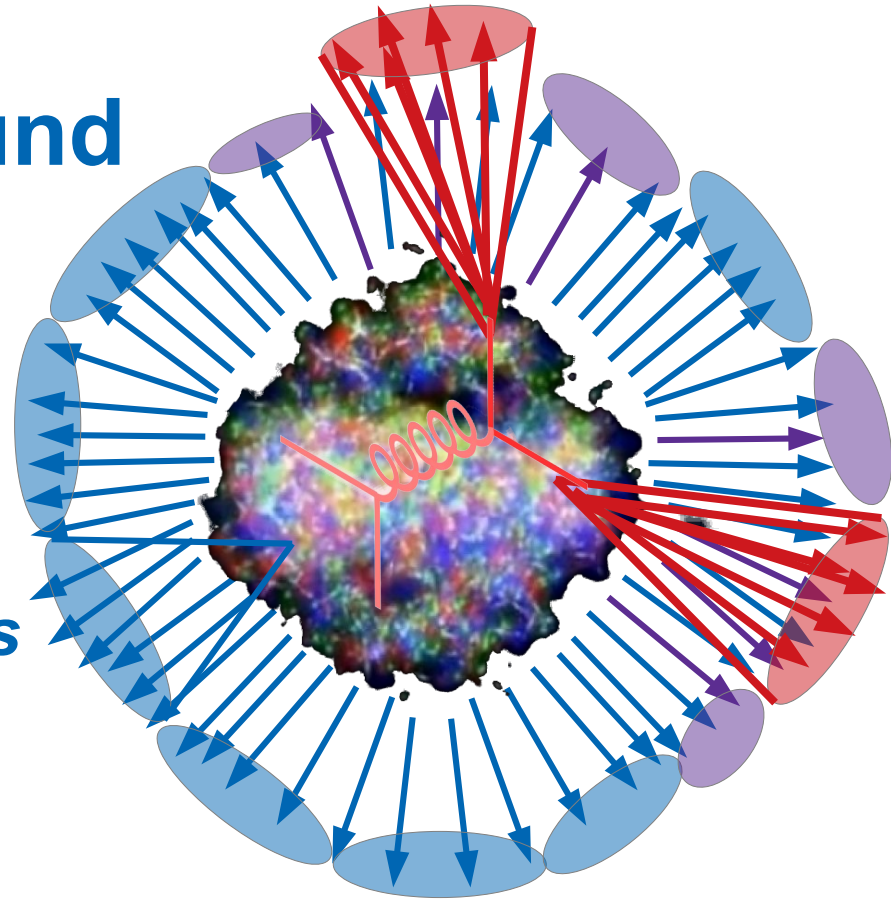
Signal

Signal vs Background:

The standard paradigm

Background

Combinatorial jets



Signal

*Some gray areas

Jet finding in AA collisions

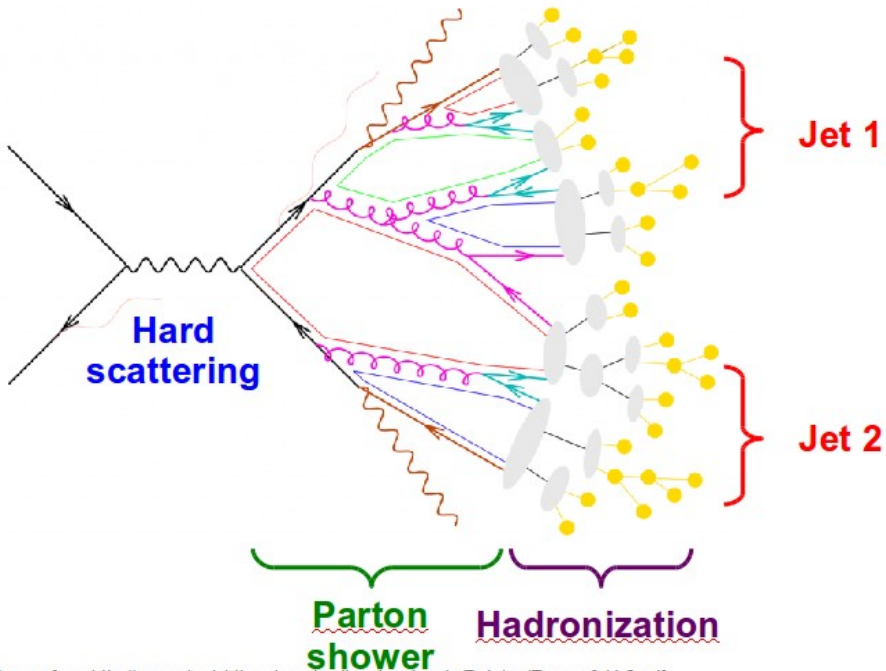
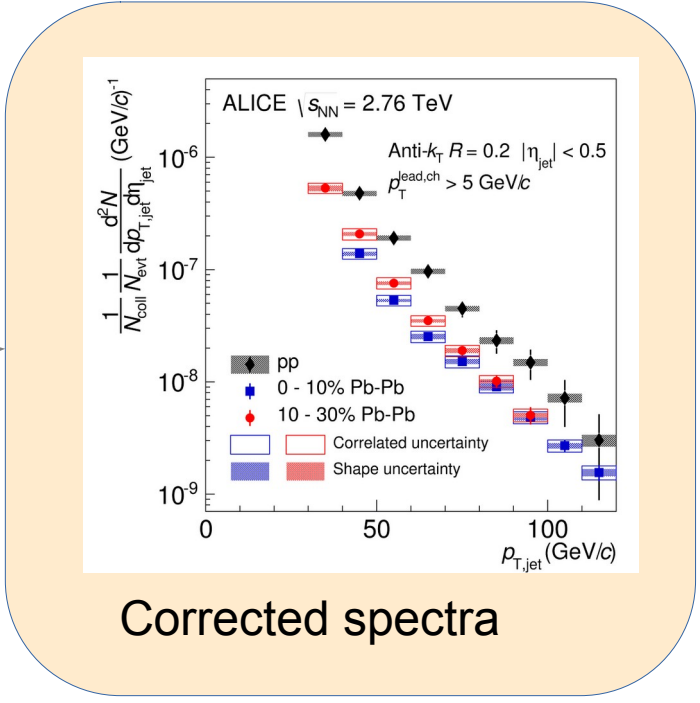
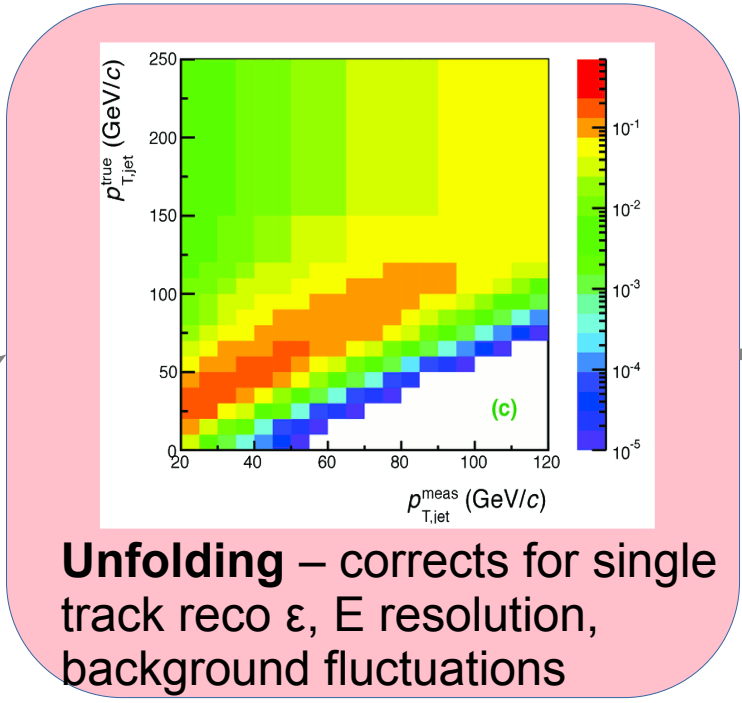
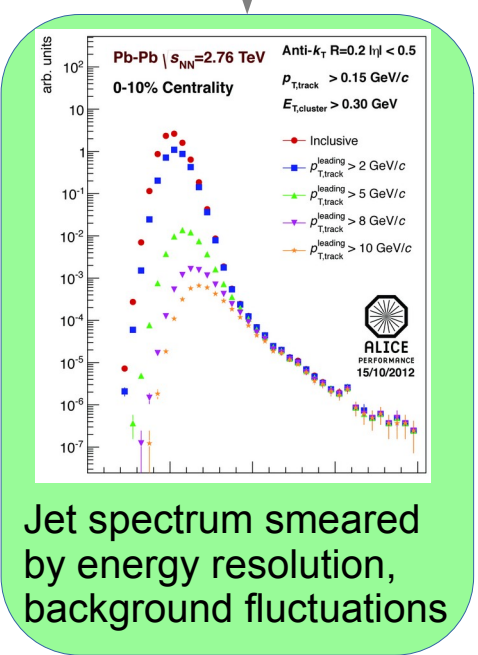
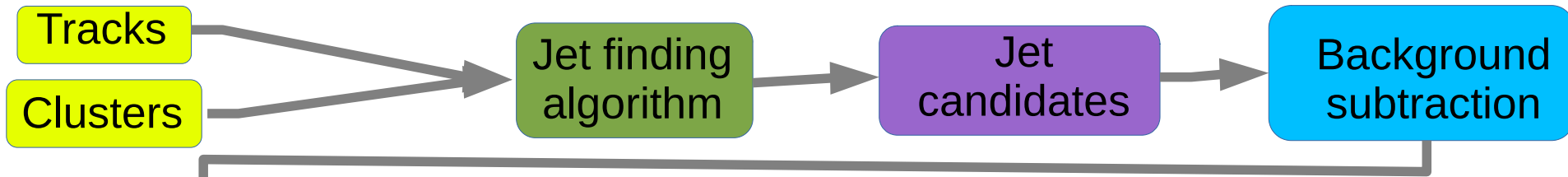


Image from <http://www.gk-eichtheorien.physik.uni-mainz.de/Dateien/Zeppenfeld-3.pdf>

- Jet finder: groups final state particles into jet candidates
 - Anti- k_T algorithm
JHEP 0804 (2008) 063 [arXiv:0802.1189]
- Combinatorial jet candidates
- Energy smearing from background
- Sensitive to methods to suppress combinatorial jets and correct energy
- Focus on narrow/high energy jets

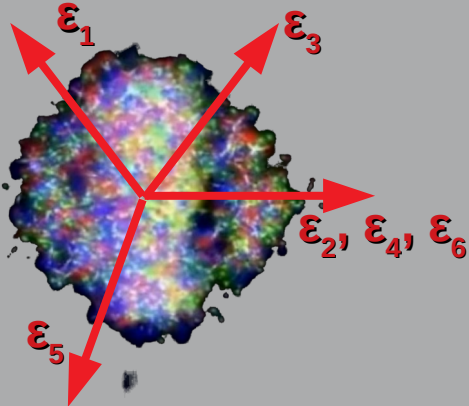
Analysis steps



Understanding the background

TennGen background generator

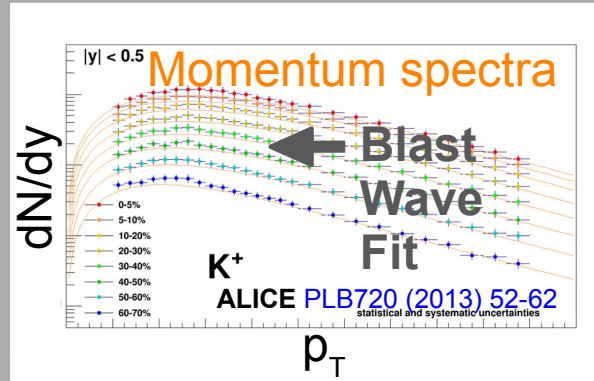
Event properties



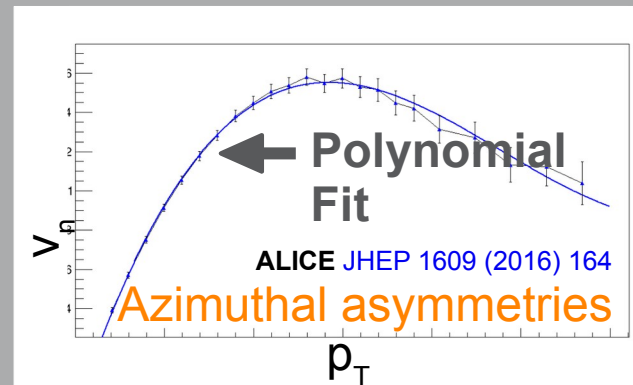
- Even event planes fixed at $\Psi=0$
- Odd planes at random ϕ
- Multiplies from ALICE PRC88 (2013) 044910

**No jets! No resonances
Emulates hydro correlations**

Track properties



→ Random p_T



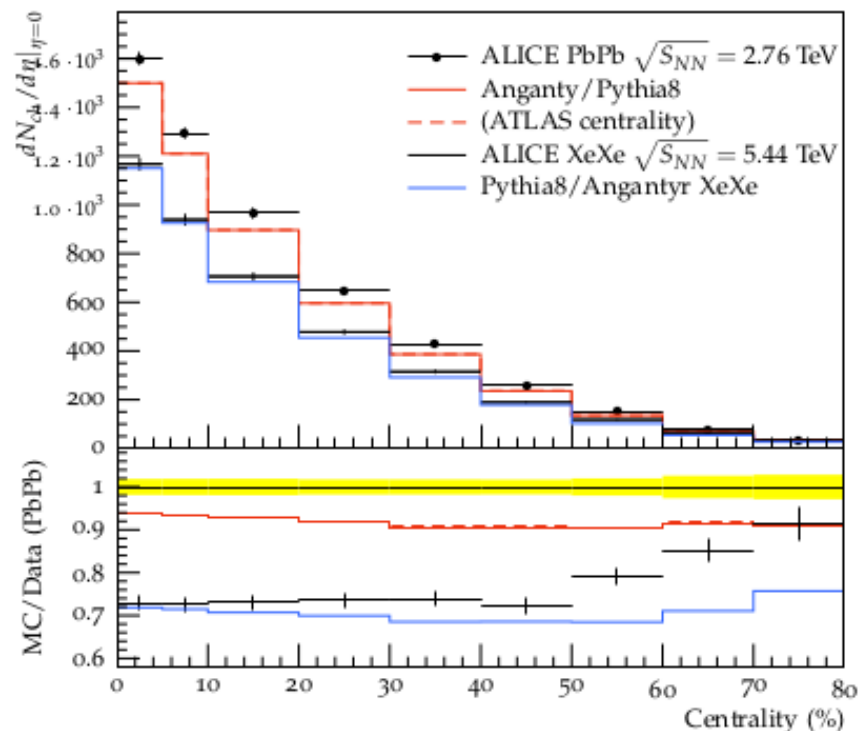
→ v_n
→ Random ϕ

PYTHIA Angantyr

JHEP (2018) 2018: 134

- Based on PYTHIA 8
Sjöstrand, Mrenna & Skands,
JHEP05 (2006) 026
Comput. Phys. Comm. 178 (2008) 852.
- Based on Fritiof & wounded nucleons
- N-N collisions w/fluctuating radii
→ fluctuating σ

**Lots of jets! And resonances!
No hydrodynamics, no jet quenching**



Area-based background subtraction

Cacciari & Salam, [PLB659:119–126,2008](#)

Particles, clusters

k_T algorithm

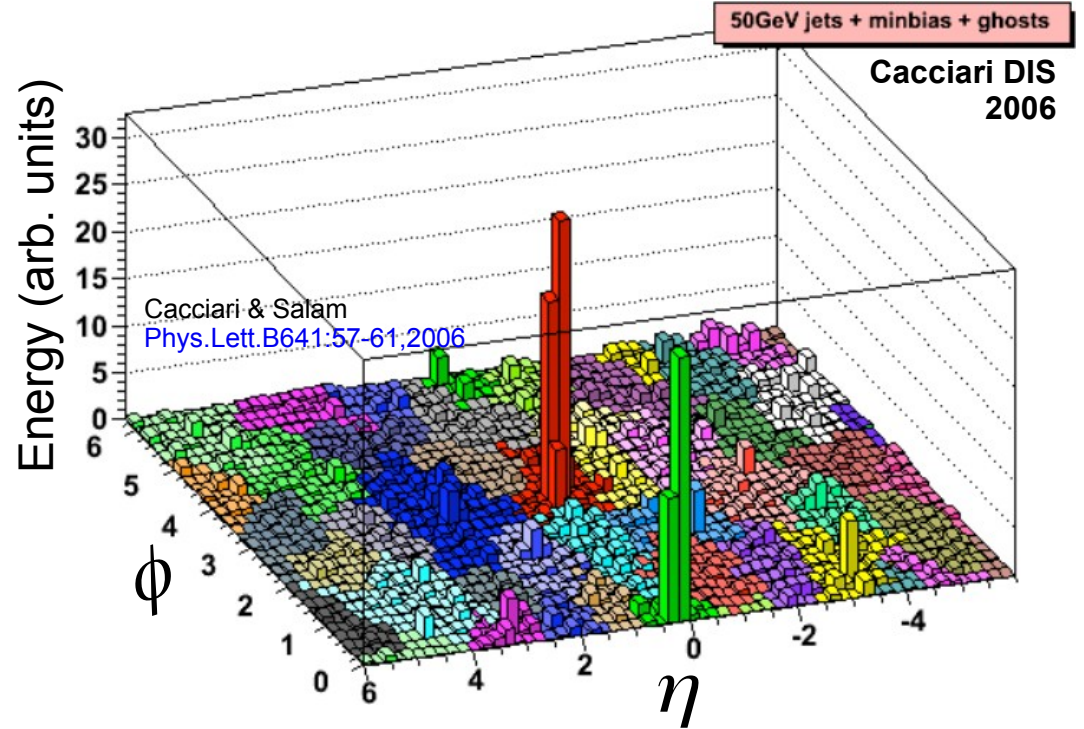
$$k_T = p_T, \Delta R_{ij} = \sqrt{(\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2}$$

- For all i, j calculate:
$$d_{ij} = \min(p_{T,i}^2, p_{T,j}^2) \Delta R_{ij}^2$$
 - $$d_{iB} = p_{T,i}^2$$
 - Combine smallest d_{ij} .
If d_{iB} smallest, $d_{iB} \rightarrow$ jet
- Repeat until no particles left

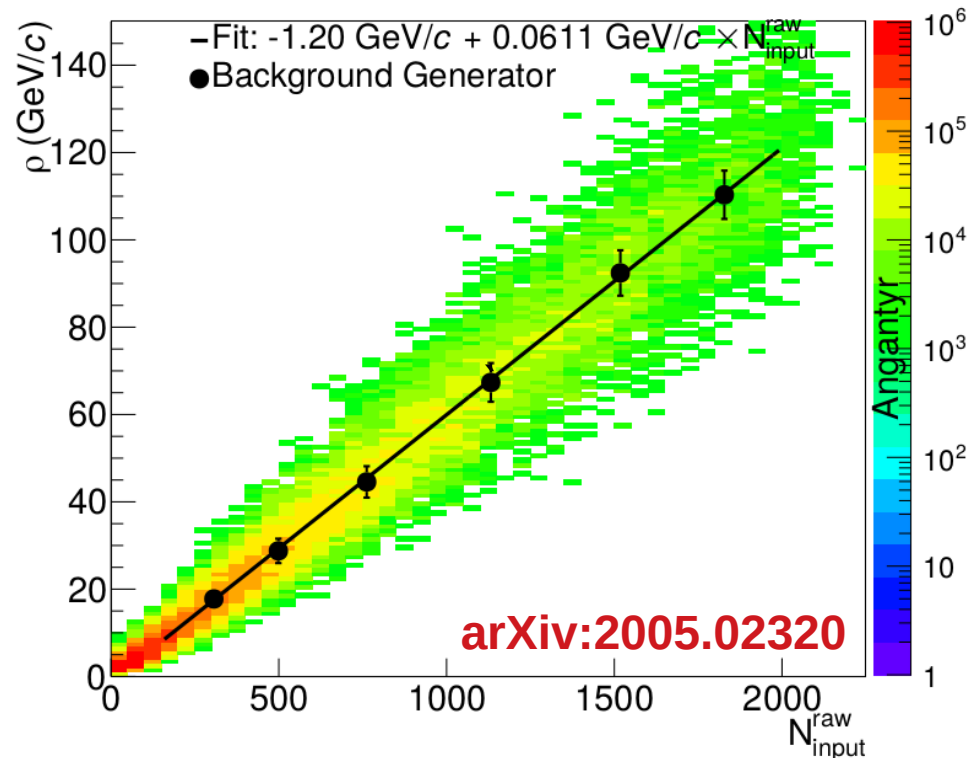
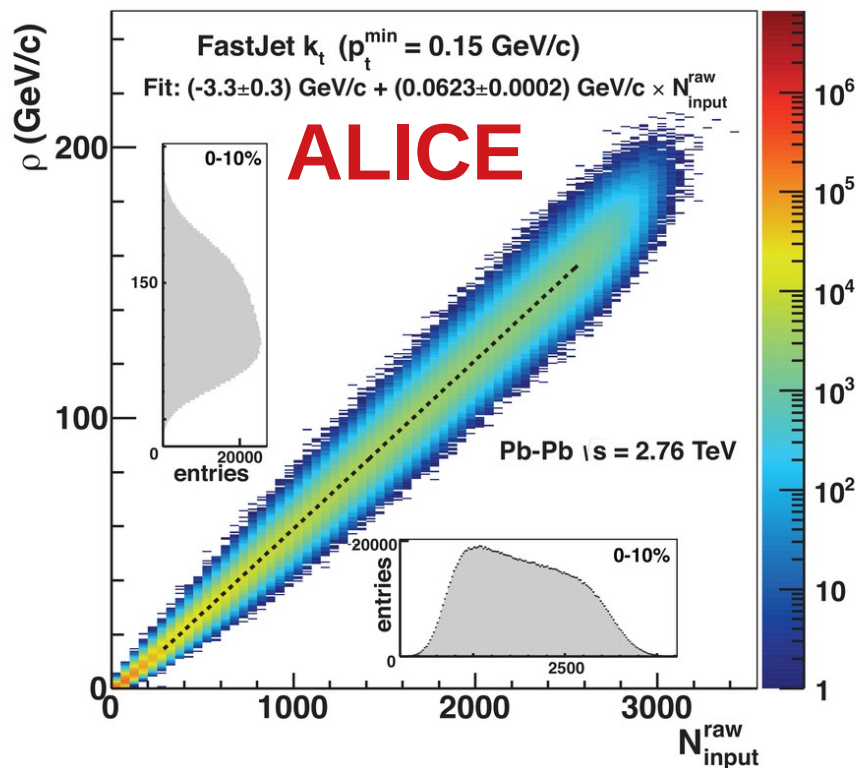
Jet candidates

Median $\rho = p_T / A$

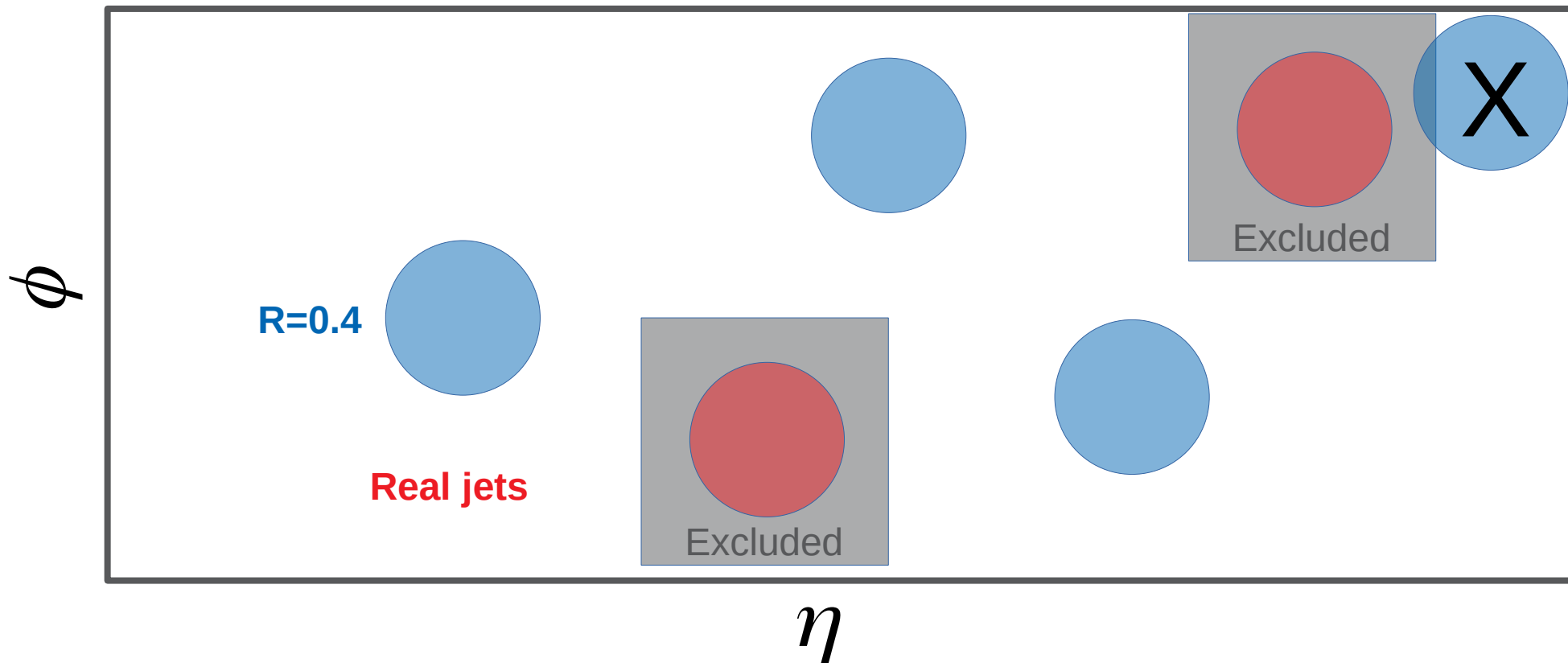
$$p_T^{jet} = p_T^{reco} - \rho_{median} A^{jet}$$



Background density ρ



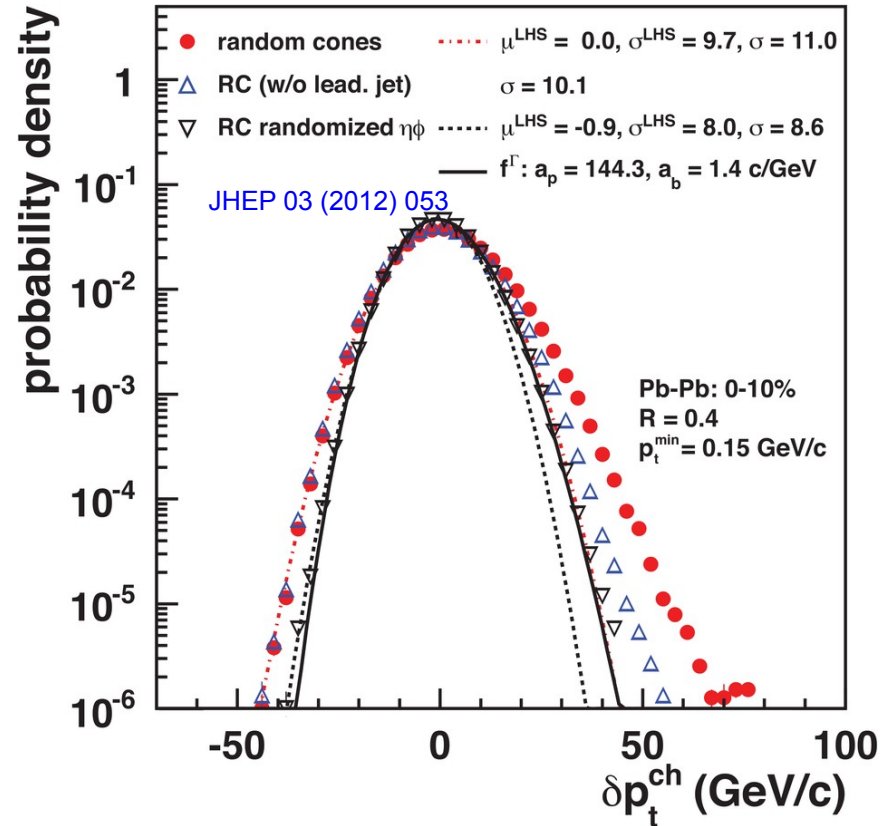
Random cones



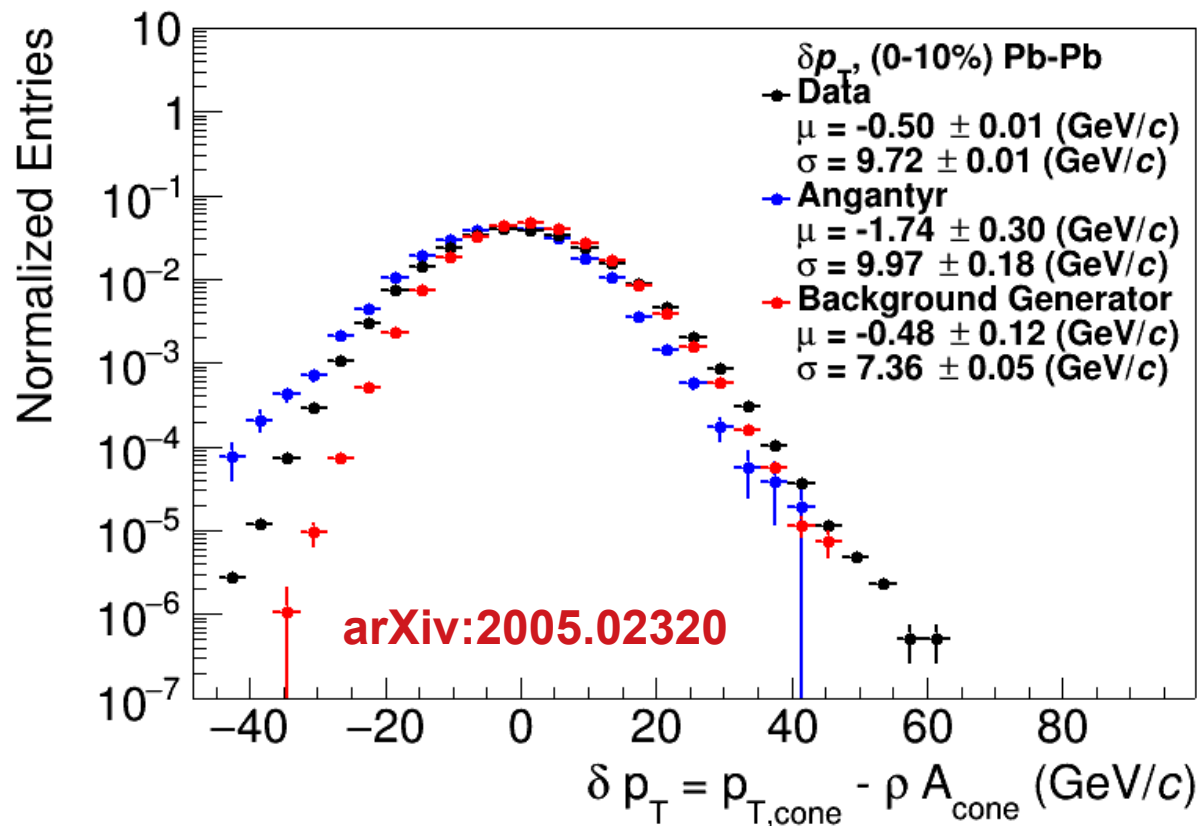
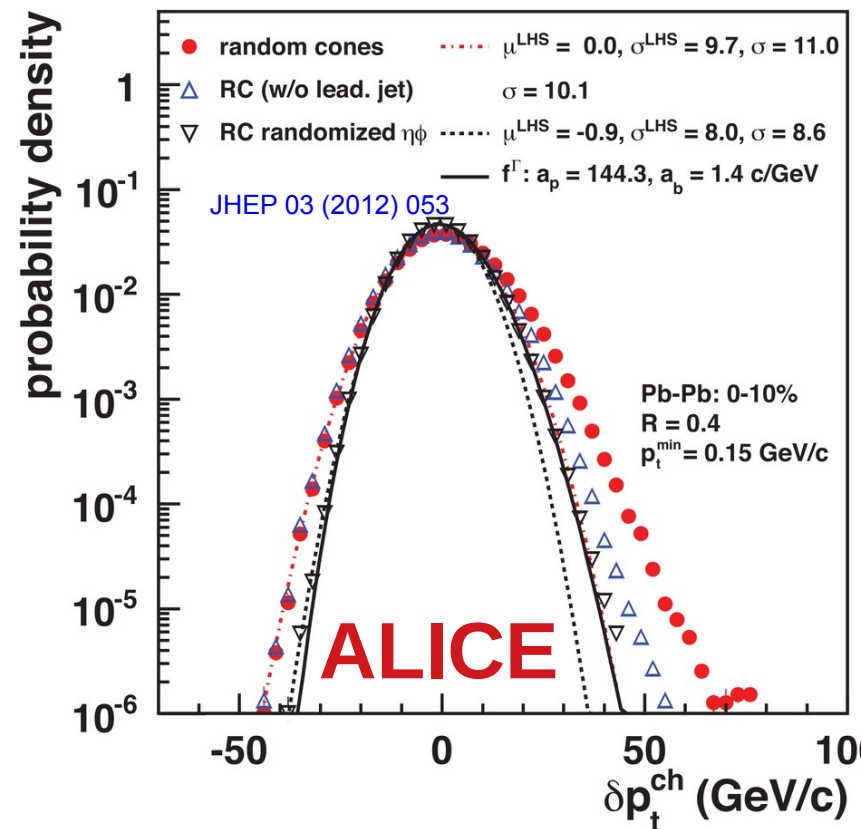
Random cones in ALICE

- Estimate ρ
 - k_T jet finder \rightarrow jet candidates
 - $\rho = \text{Median}(p_T/A)$
- Draw Random cone

$$\delta p_T = p_T^{reco} - \rho A$$



Random cones



Shape of width of the distribution

Single particle spectra

$$f_{\Gamma}(p_T, p, b) = \frac{b}{\Gamma(p)} (b p_T)^{p-1} e^{-b p_T}$$

$$\frac{dN}{dy} \propto f_{\Gamma}(p_T, 2, b) = b^2 p_T e^{-b p_T}$$

$$\mu_{p_T} = \frac{p}{b}, \sigma_{p_T} = \frac{\sqrt{p}}{b}$$

Tannenbaum, PLB(498),1-2,Pg.29-34(2001)

Σp_T of N particles \rightarrow N-fold convolution:

$$f_N(p_T, p, b) = f_{\Gamma}(p_T, Np, b) \quad \frac{dp_T^{total}}{dy} \propto f_N(p_T, Np, b)$$

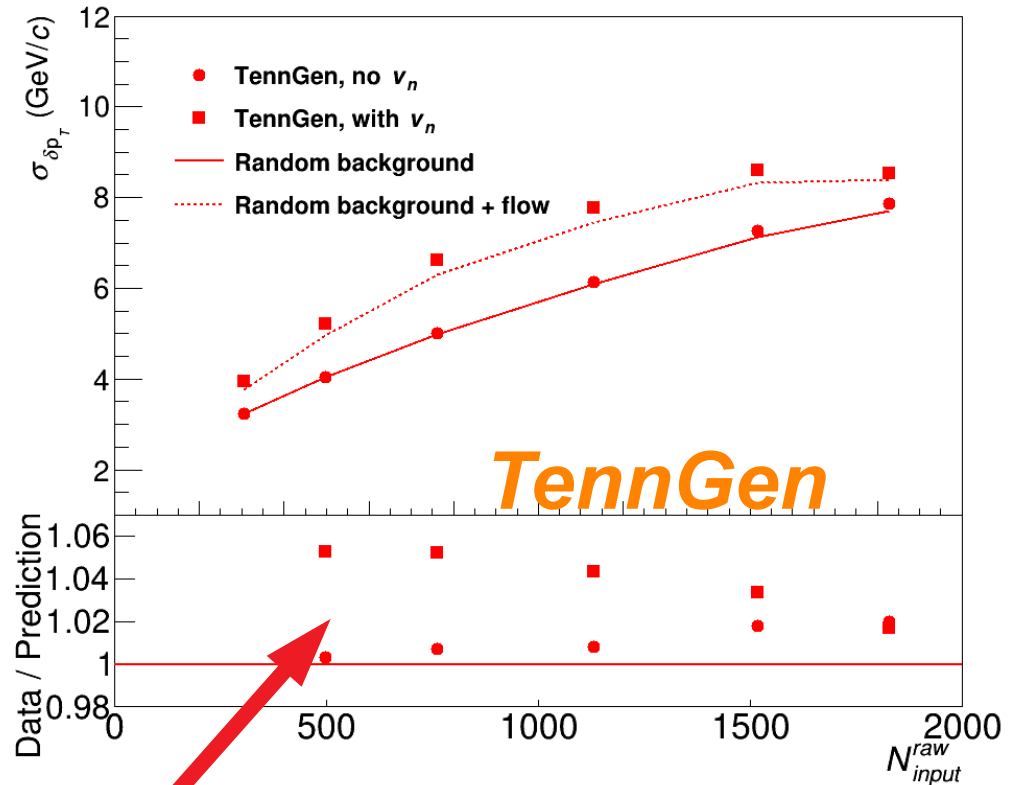
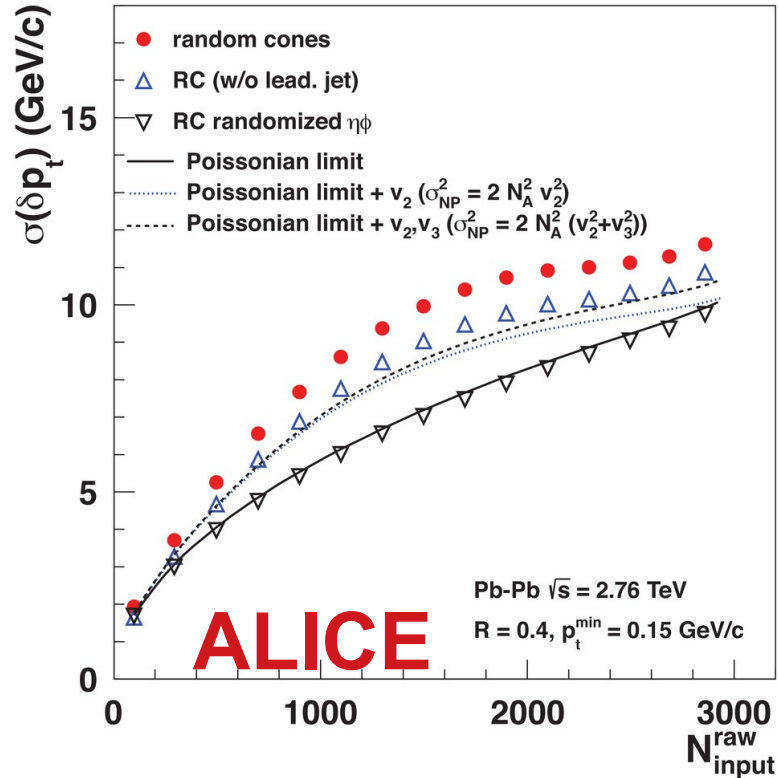
$$N = \frac{N_{total}}{A_{total}} \pi R^2 \quad \mu_{total} = \frac{Np}{b} = N \mu_{p_T}, \sigma_{total} = \frac{\sqrt{Np}}{b} = \sqrt{N} \sigma_{p_T}$$

Add Poissonian fluctuations in N: $\sigma_{total} = \sqrt{N \sigma_{p_T}^2 + N \mu_{p_T}^2}$

Add non-Poissonian fluctuations in N due to flow

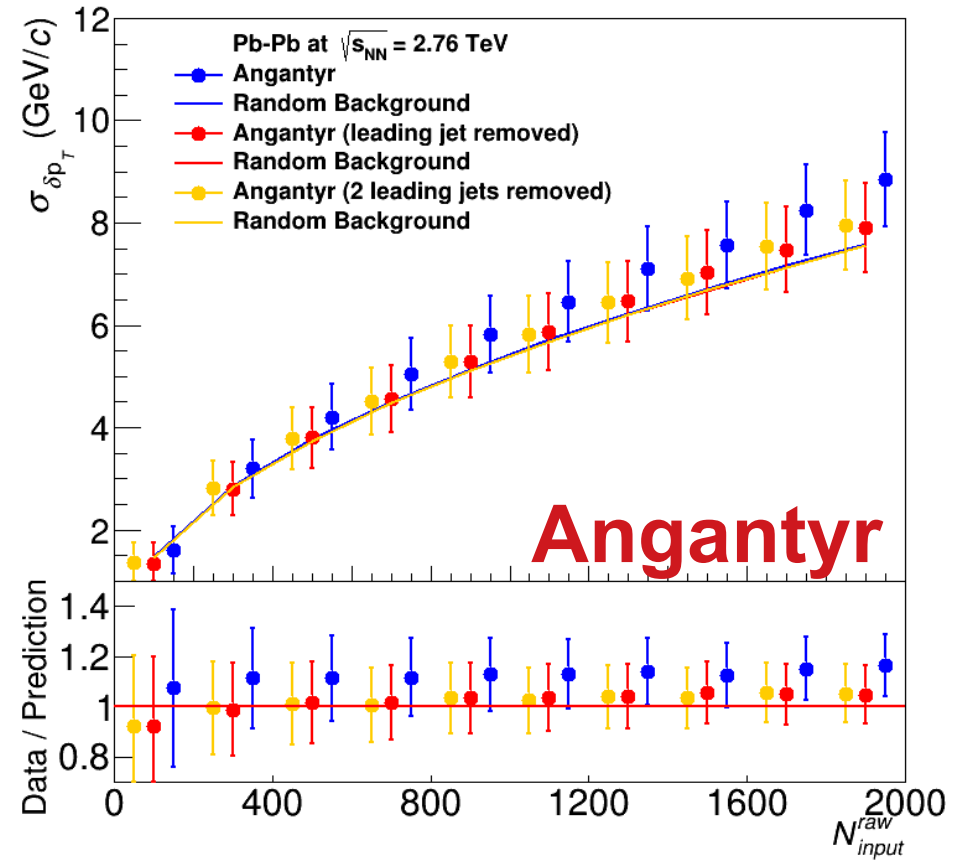
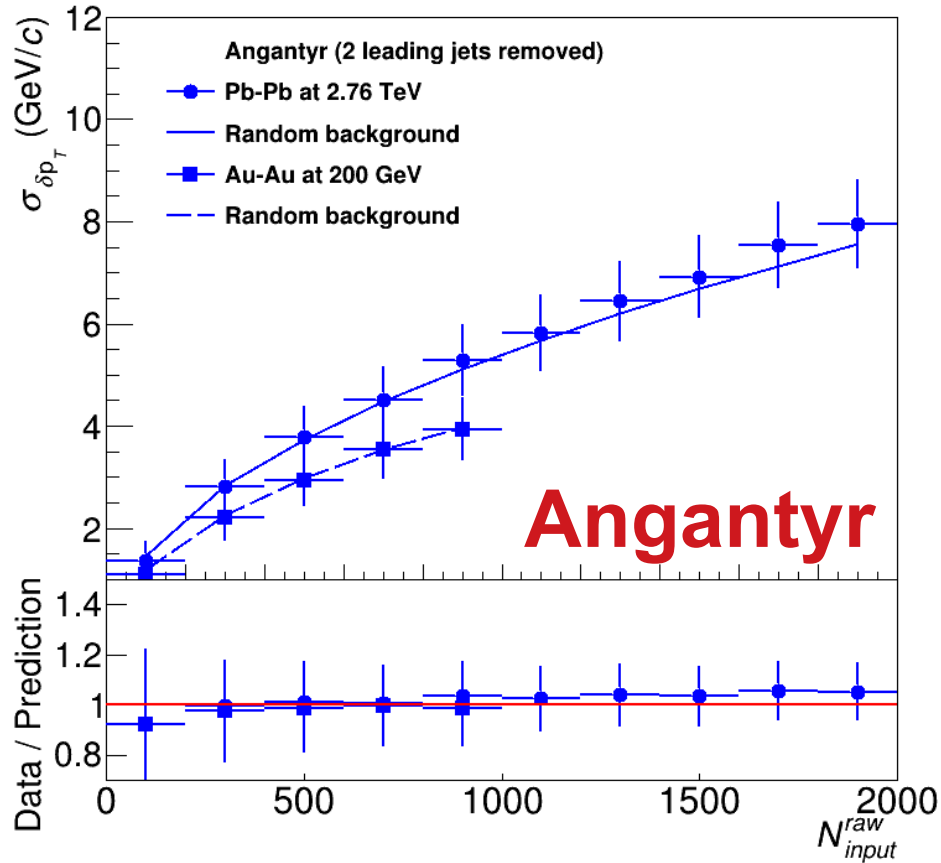
$$\sigma_{total} = \sqrt{N \sigma_{p_T}^2 + (N + 2N^2 \sum_n v_n^2) \mu_{p_T}^2}$$

Width vs multiplicity



Small deviations

Width vs multiplicity



Shape of width of the distribution

Single particle spectra

$$f_{\Gamma}(p_T, p, b) = \frac{b}{\Gamma(p)} (b p_T)^{p-1} e^{-b p_T}$$

$$\frac{dN}{dy} \propto f_{\Gamma}(p_T, 2, b) = b^2 p_T e^{-b p_T}$$

$$\mu_{p_T} = \frac{p}{b}, \sigma_{p_T} = \frac{\sqrt{p}}{b}$$

Tannenbaum, PLB(498),1-2,Pg.29-34(2001)

Assumes shape

Σp_T of N particles \rightarrow N-fold convolution:

$$f_N(p_T, p, b) = f_{\Gamma}(p_T, Np, b) \quad \frac{dp_T^{total}}{dy} \propto f_N(p_T, Np, b)$$

$$N = \frac{N_{total}}{A_{total}} \pi R^2 \quad \mu_{total} = \frac{Np}{b} = N \mu_{p_T}, \sigma_{total} = \frac{\sqrt{Np}}{b} = \sqrt{N} \sigma_{p_T}$$

$$\text{Add Poissonian fluctuations in N: } \sigma_{total} = \sqrt{N \sigma_{p_T}^2 + N \mu_{p_T}^2}$$

Add non-Poissonian fluctuations in N due to flow

$$\sigma_{total} = \sqrt{N \sigma_{p_T}^2 + (N + 2N^2 \sum_n v_n^2) \mu_{p_T}^2}$$

Assumes uncorrelated number fluctuations

Combinatorial jets are mostly random!

$$\sigma_{total} = \sqrt{N \sigma_{p_T}^2 + (N + 2N^2 \sum_n v_n^2) \mu_{p_T}^2} \approx 8.5 \text{ GeV}/c$$

Flow

$$\sigma_N = N \mu_{p_T} \sqrt{2 \sum_n v_n^2} \approx 5.1 \text{ GeV}/c$$

Fluctuations in p_T

$$\sigma_{p_T \text{ fluctuations}} = \sqrt{N} \sigma_{p_T} \approx 2.5 \text{ GeV}/c$$

Fluctuations in N

$$\sigma_N = \sqrt{N} \mu_{p_T} \approx 4.4 \text{ GeV}/c$$

Realistic values

At LHC, 0-10% Pb-Pb, $R=0.2$

$$N \approx \frac{2000}{2\pi} \quad A = \frac{2000}{2} \quad R^2 = 40$$

$$\mu_{p_T} = \frac{p}{b} \approx 0.7 \text{ GeV}/c$$

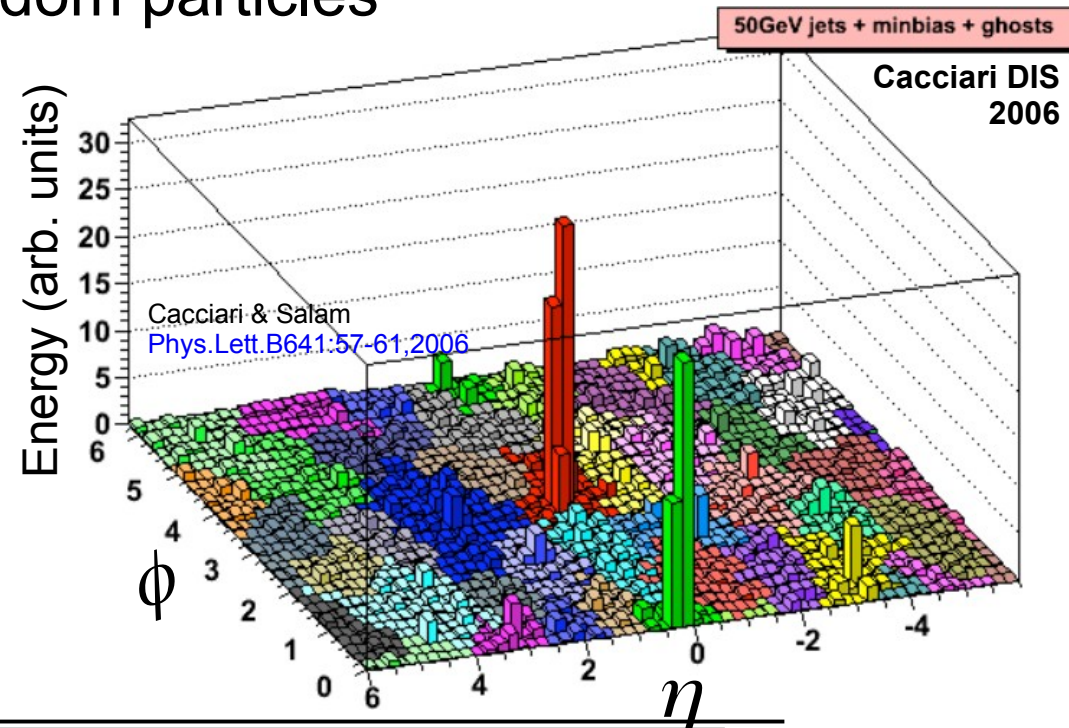
$$\sigma_{p_T} = \frac{\sqrt{p}}{b} = \frac{\mu_{p_T}}{\sqrt{p}} \approx 0.4 \text{ GeV}/c$$

$$v_1 \approx 0.1, v_2 \approx 0.1, v_3 \approx 0.05$$

Note that this is for **random cones!**
Jet finders are peak finders.

Mini-summary

- Jet finders put all input clusters, tracks in a jet candidate
- Background is *dominated* by random particles
- Models have background too!
 - And it doesn't agree with data!
 - Sensitive to multiplicity, shape of spectrum



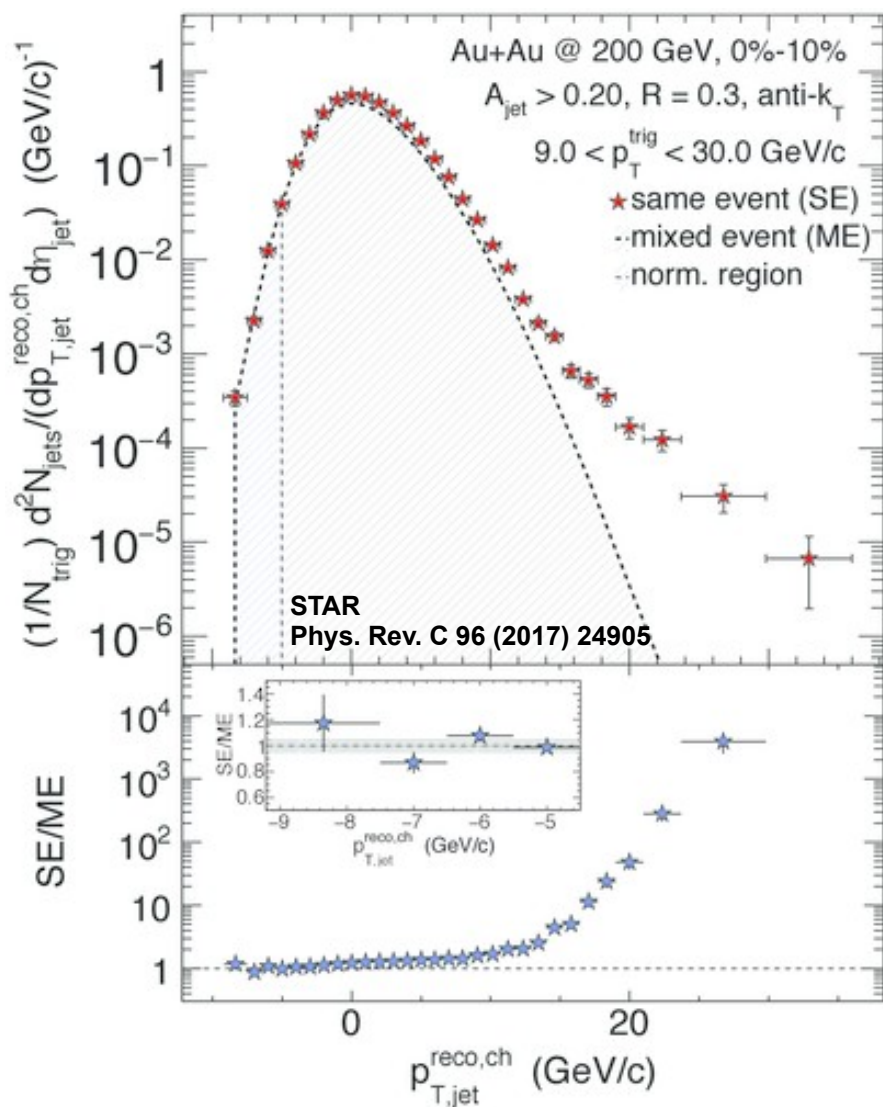
Jets in A+A collisions: Dealing with background

Problems caused by background

- Combinatorial jets: unknown fraction of jets → estimate fraction, suppress
- Background in “real” jets: fluctuations in background distort reconstructed spectrum make unfolding unstable

Background subtraction methods

- Area-based (STAR, ALICE)
- Mixed events (STAR)
- Neural net (ALICE)
- Iterative (ATLAS, CMS)
- Reflection about $\eta=0$ (CMS)



Mixed events

- Gets background up to a normalization factor
- Good agreement with the data... but 20% discrepancies still within uncertainties
- In measurement with background suppressed (h-jet correlations)
- Did not see such agreement at the LHC

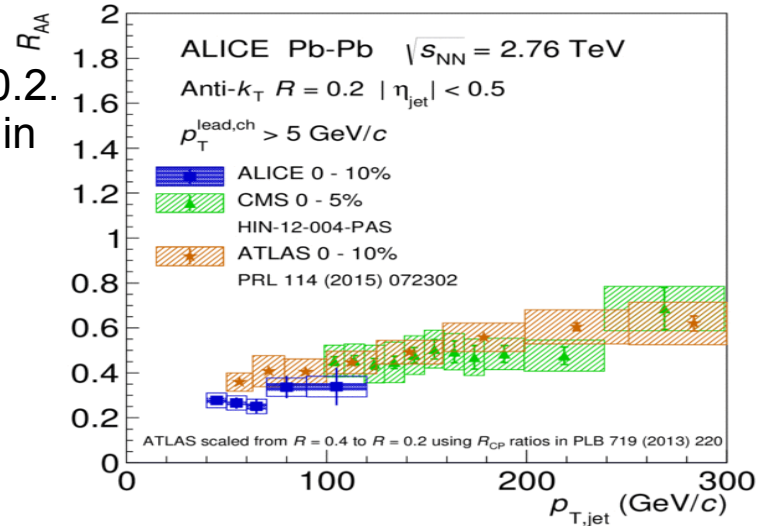
ATLAS

Background subtraction method:

- Iterative procedure
 - **Calorimeter jets:** Reconstruct jets with $R=0.2$. v_2 modulated $\langle \text{Bkgd} \rangle$ estimated by energy in calorimeters excluding jets with at least one tower with $E_{\text{tower}} > \langle E_{\text{tower}} \rangle$
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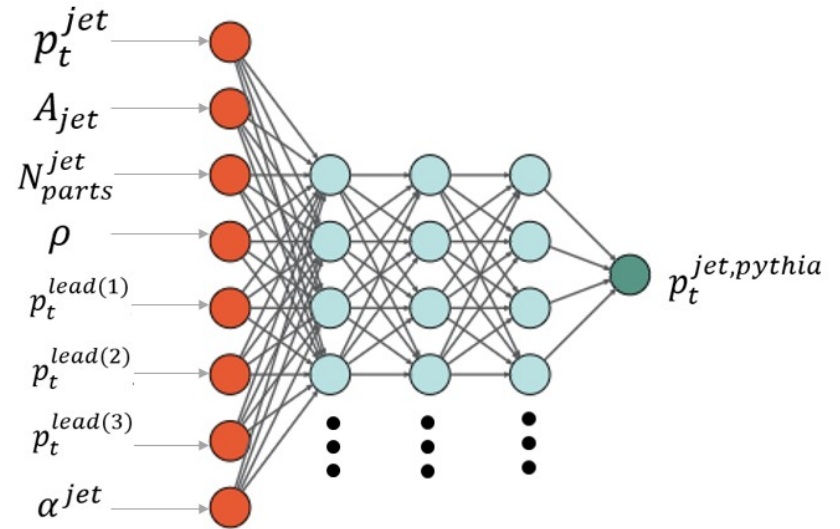
Phys. Lett. B 719 (2013) 220-241



ATLAS-CONF-2013-022

Neural net Background Subtraction

- Deep Neural Network
 - N,100,100,50,1
- Trained on 
- Trained with back propagation

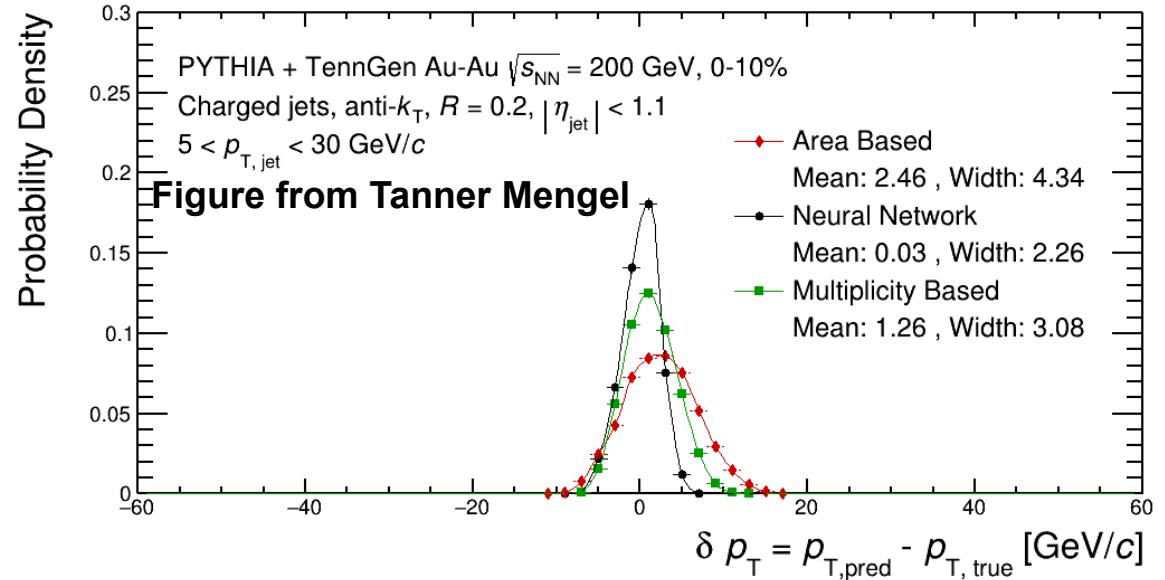


Phys. Rev. C 99, 064904 (2019)

Alternative to area-based subtraction

- Estimate $\langle p_T \rangle$
 - k_T jet finder \rightarrow jet candidates
 - $\langle p_T \rangle = \text{Median}(p_T/N)$

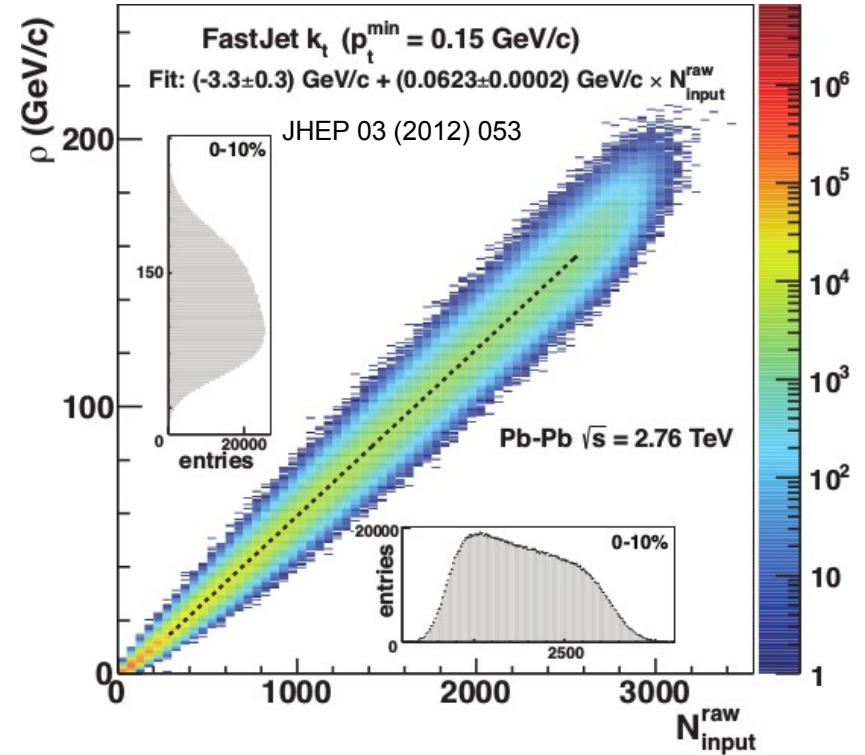
$$p_T = p_T^{tot} - \langle p_T \rangle N$$



Focus on smaller angles

- Pros
 - Background is smaller
 - Background fluctuations smaller
- Cons:
 - Modifications expected at higher R
 - Biases sample towards quarks

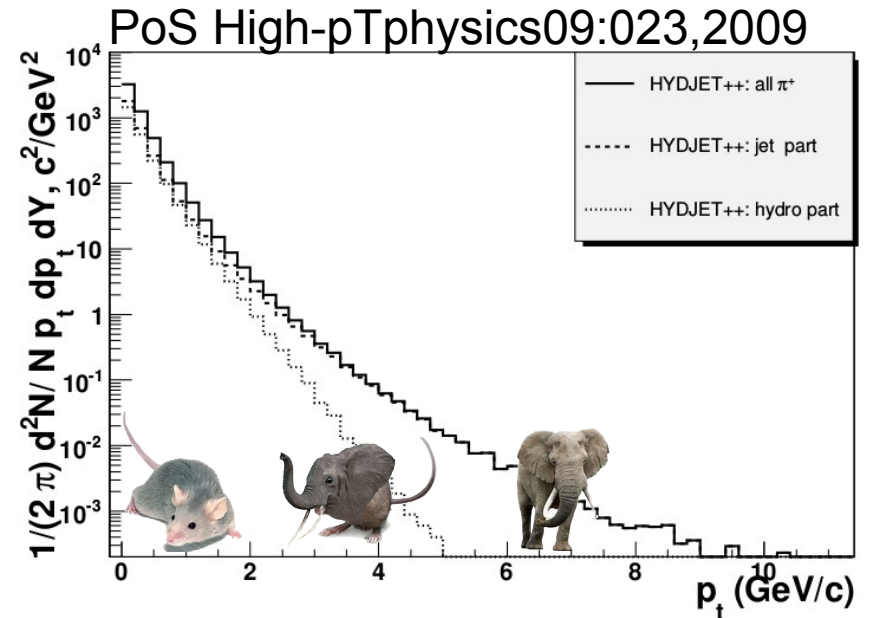
Aside: “quark” and “gluon” jet only defined at leading order.



Focus on high p_T

- Pros:
 - Reduces combinatorial background
- Cons:
 - Cuts signal where we expect modifications
 - Could bias towards partons which have not interacted
 - Biases sample towards quark jets

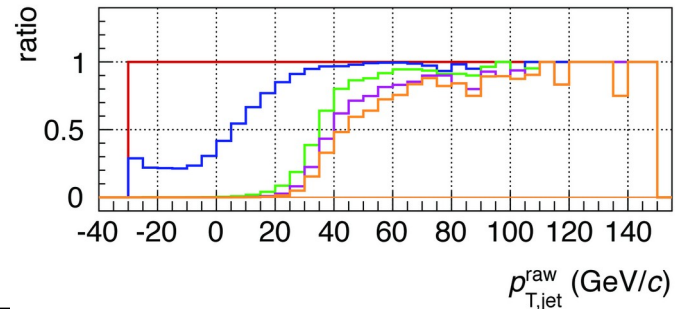
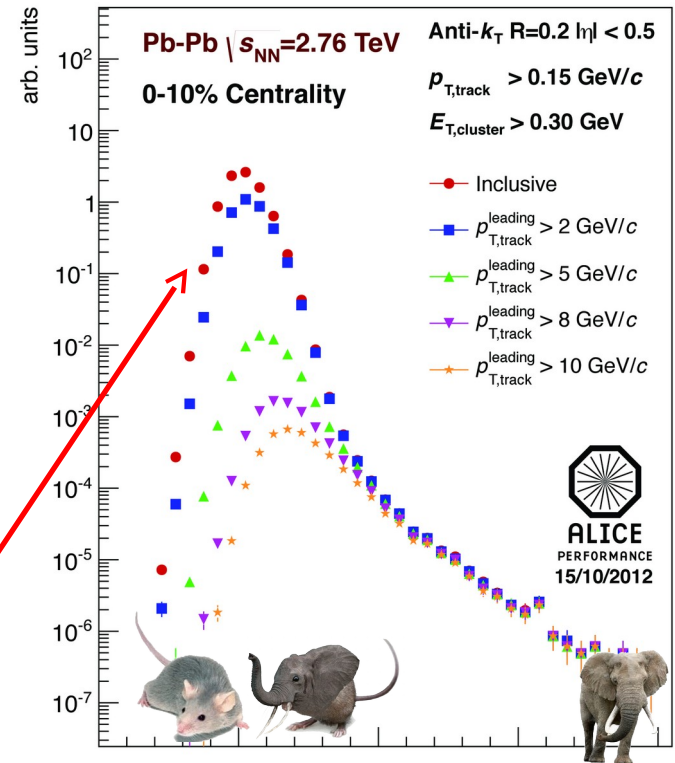
“Quark” and “gluon” jets only defined at leading order!



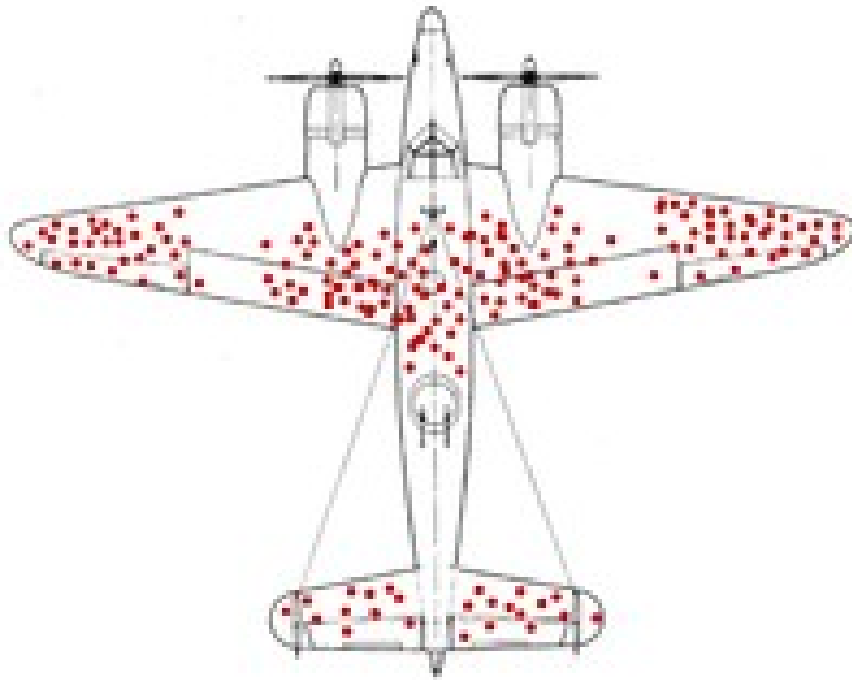
Area-based subtraction

- ALICE/STAR
- Require leading track $p_T > 5 \text{ GeV}/c$
 - Suppresses combinatorial “jets”
 - Biases fragmentation
- No threshold on constituents
- Limited to small R

Combinatorial “jets”



Survivor bias



- **WWII Example:** holes planes returning indicate where it's *safer* to get hit
- We're looking at the jets which *remain*





**What you see depends on what you're
looking for**

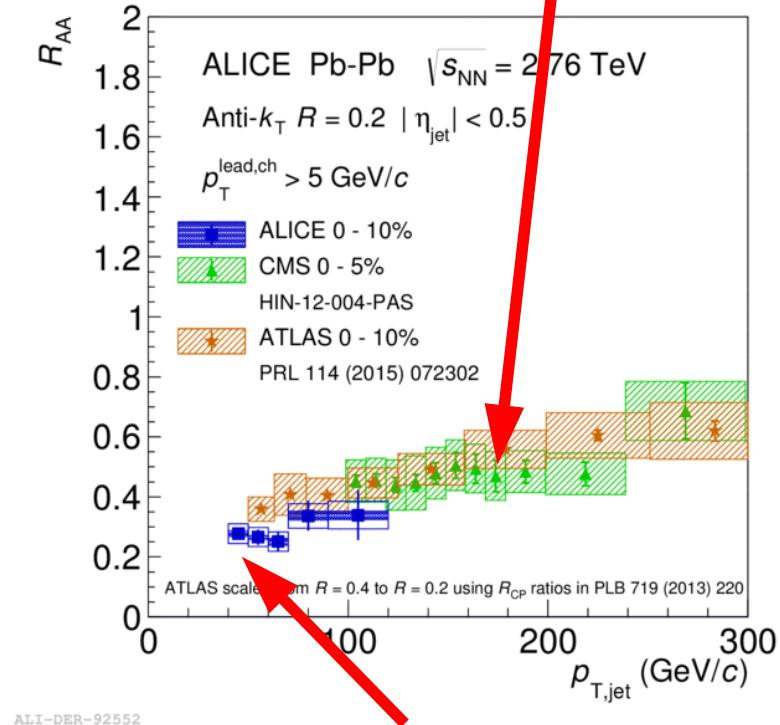
Bias & background

- **Experimental background subtraction methods:** complex, make assumptions, apply biases
- **Survivor bias:** Modified jets probably look more like the medium
- **Quark/Gluon bias:**
 - Quark jets are narrower, have fewer tracks, fragment harder [Z Phys C 68, 179-201 (1995), Z Phys C 70, 179-196 (1996),]
 - Gluon jets reconstructed with k_T algorithm have more particles than jets reconstructed with anti- k_T algorithm [Phys. Rev. D 45, 1448 (1992)]
 - Gluon jets fragment into more baryons [EPJC 8, 241-254, 1998]
- **Fragmentation bias:** Experimental measurements explicitly select jets with hard fragments

Iterative procedure

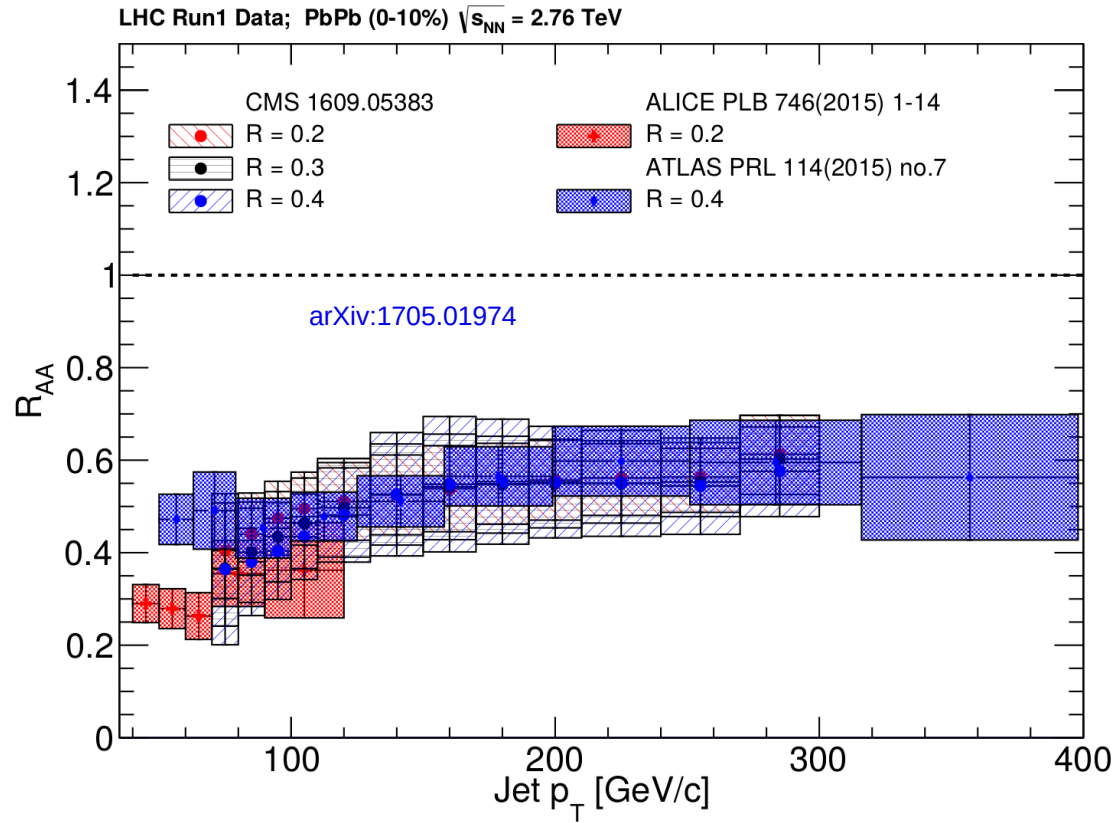
- Used by ATLAS & CMS
- ATLAS
 - **Calorimeter jets:** Reconstruct jets with $R=0.2$. v_2 modulated $\langle \text{Bkgd} \rangle$ estimated by energy in calorimeters excluding jets with at least one tower with $E_{\text{tower}} > \langle E_{\text{tower}} \rangle$
 - **Track jets:** Use tracks with $p_T > 4$ GeV/c
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Constituent biases
don't matter that much
up here

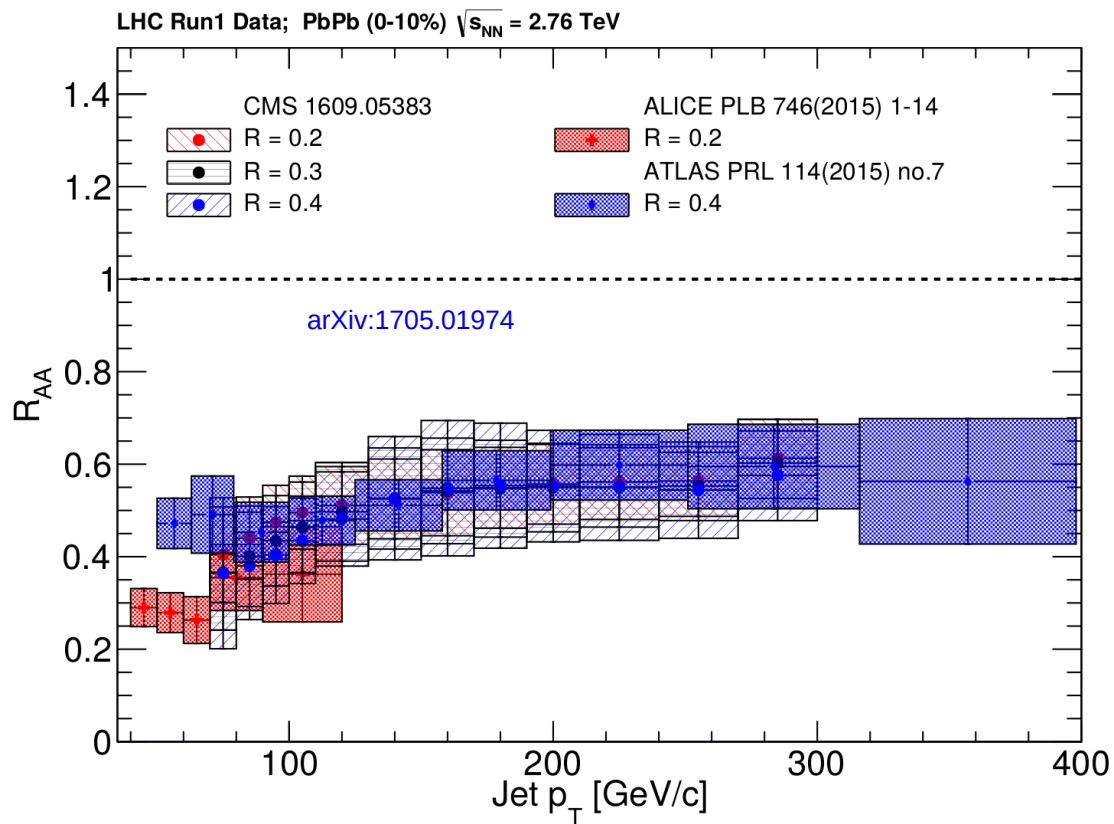


But they do matter
down here!

Jet R_{AA}



Jet R_{AA}

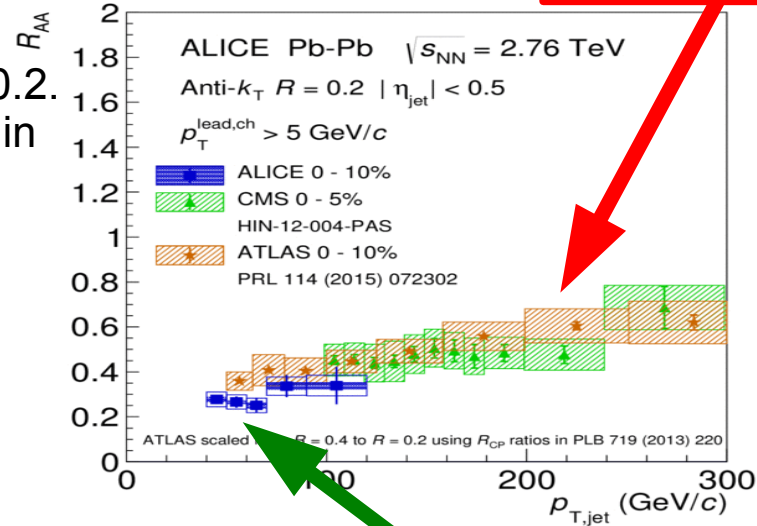


Tension between ATLAS & ALICE/CMS

ATLAS



Constituent biases don't matter that much up here



But they do matter down here!



Background subtraction method:

- Iterative procedure

- Calorimeter jets:** Reconstruct jets with $R=0.2$. v_2 modulated $\langle Bkgd \rangle$ estimated by energy in calorimeters excluding jets with at least one tower with

$$E_{tower} > \langle E_{tower} \rangle$$

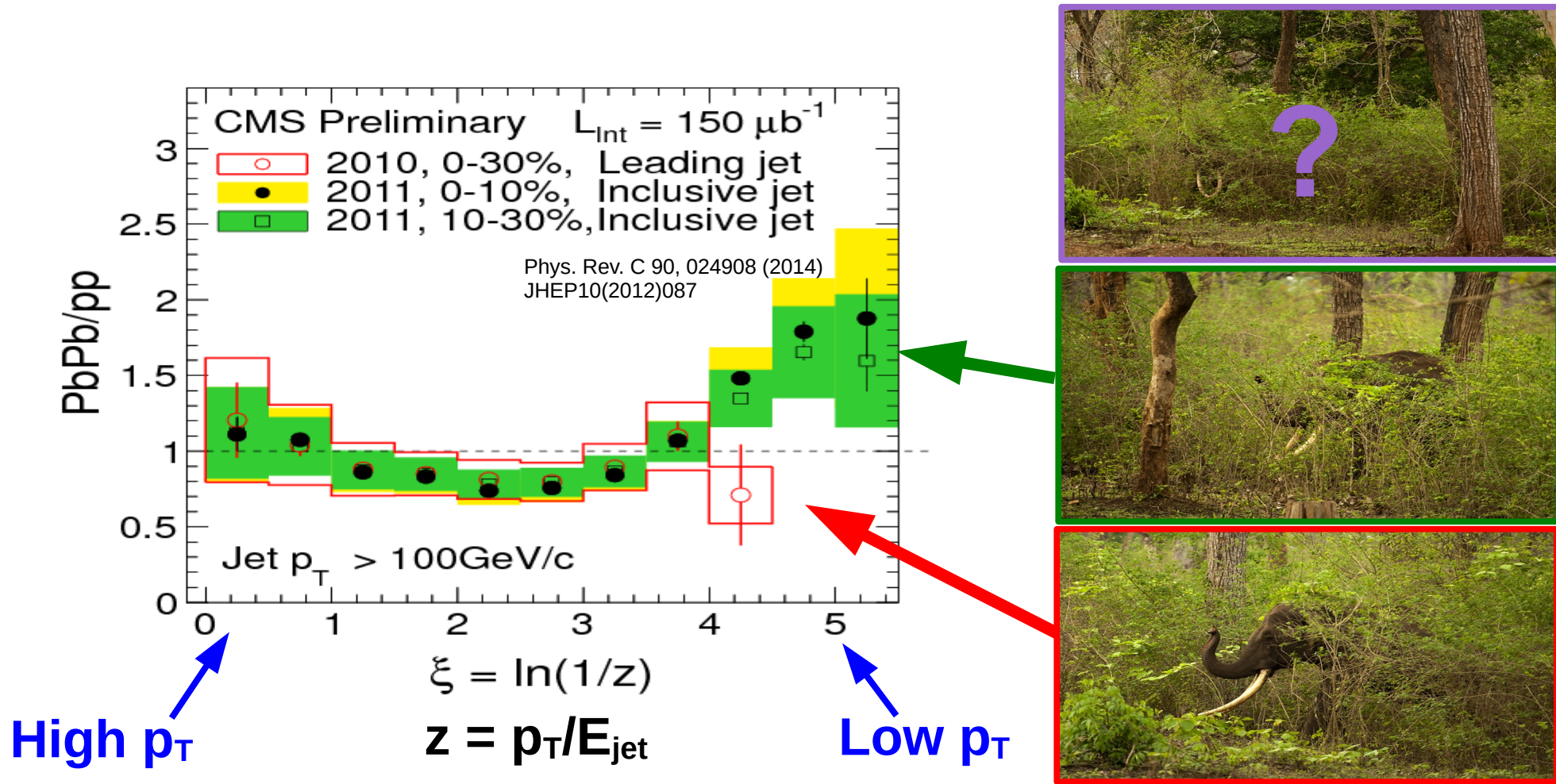
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Phys. Lett. B 719 (2013) 220-241

What you see depends on where you look

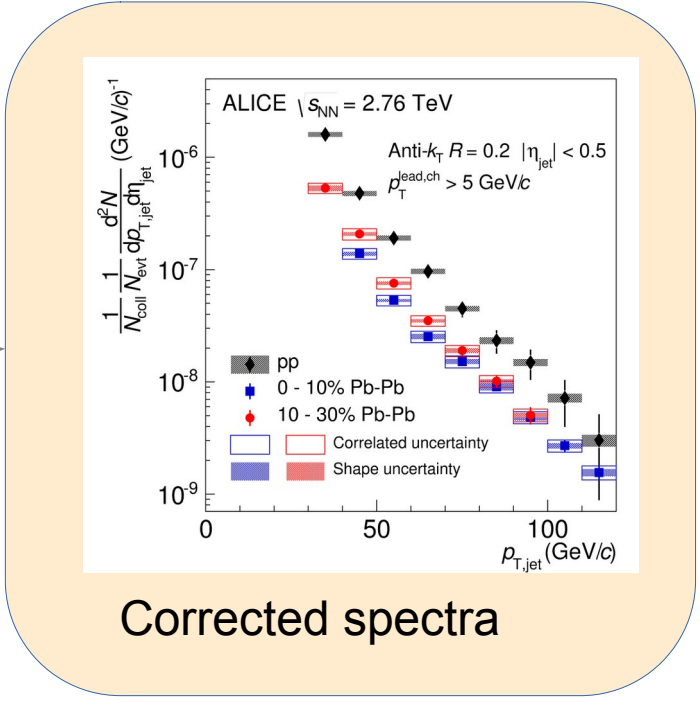
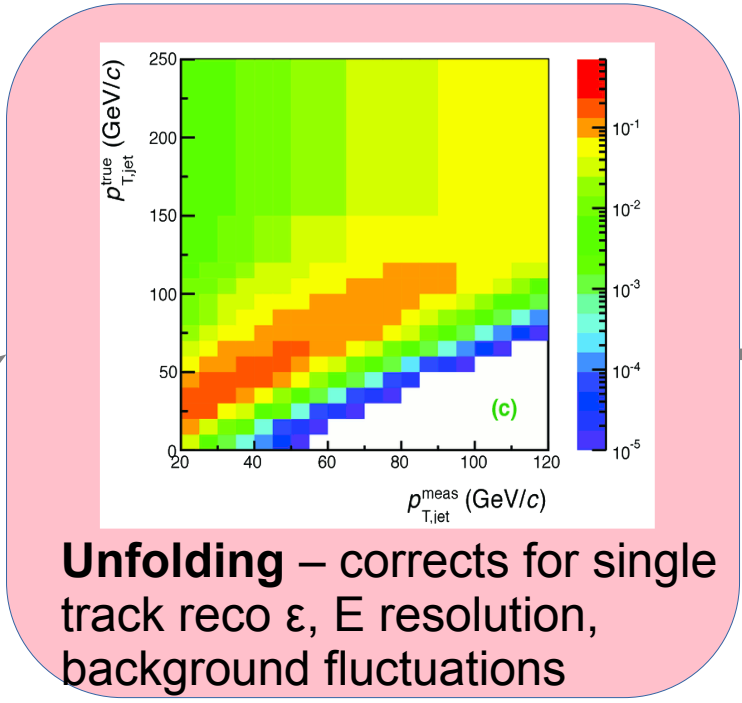
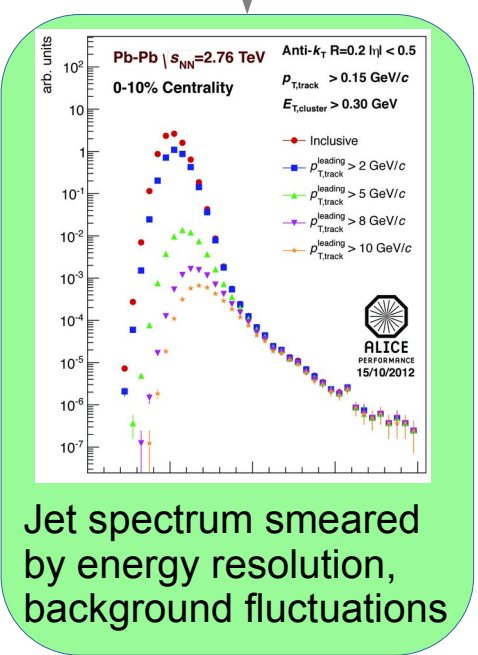
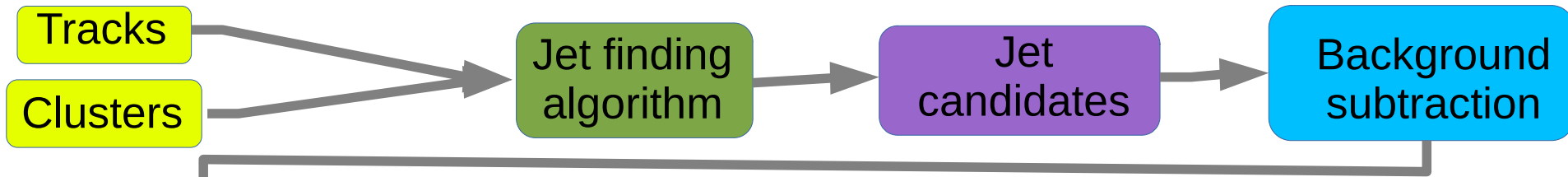


Mini-summary

- Most studies do one or more of the following:
 - Explicitly apply a (non-perturbative) bias
 - *Implicitly* apply a (non-perturbative) bias
 - Focus on small R
 - Focus on high pT
- May also → survivor bias
- Background subtraction should be part of definition of algorithm

What are the dominant uncertainties?

Analysis steps



Unfolding

$$\vec{v} = R\vec{\mu} + \vec{\beta}$$

$$v_i = \sum_{j=1}^M (R_{ij}\mu_j) + \beta_i$$

- $\vec{\mu}$: the “true” histogram
- \vec{v} : the actual data we measure
- $\vec{\beta}$: background
- R : the response matrix

Simple Solution (Inversion)

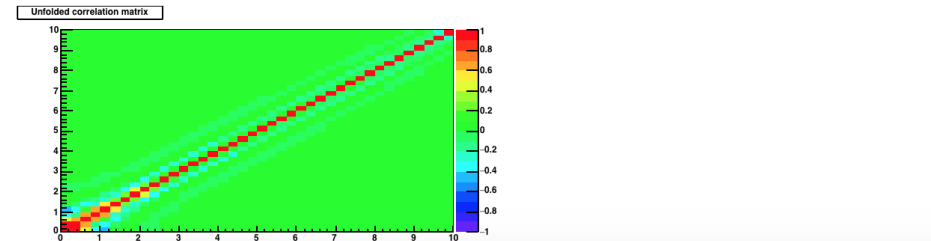
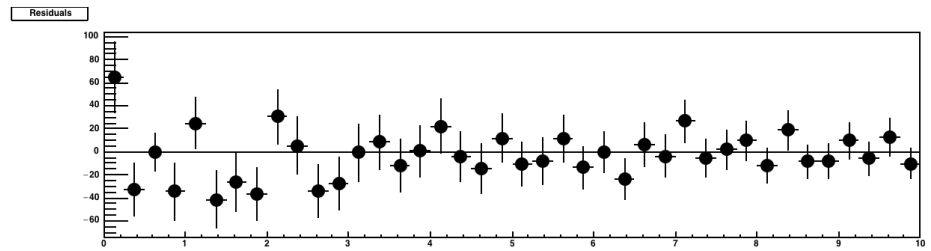
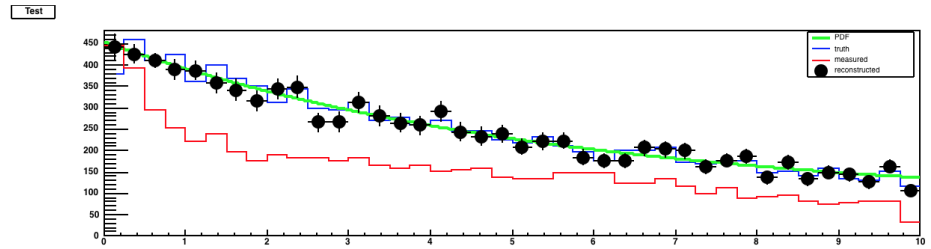
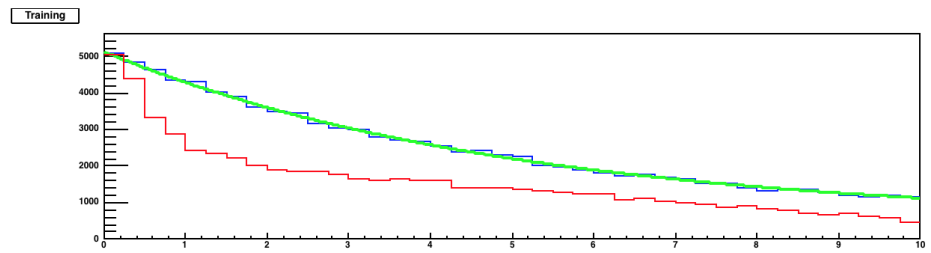
- Rearrange $\vec{v} = R\vec{\mu} + \vec{\beta}$ to get $\vec{\mu} = R^{-1}(\vec{v} - \vec{\beta})$
- Problem: we don't have \vec{v} , we have \vec{n} , the measured data, which is subject to statistical fluxuations.
- We assume n_i is the maximum likelihood estimator for v_i , then solve for the estimator $\hat{\mu} = R^{-1}(\vec{n} - \vec{\beta})$.
- R^{-1} is obtained from R through simple matrix inversion

Iterative Bayesian Method

- Using prior knowledge, start with an initial guess for the distribution of true histograms $P^0(\hat{\mu})$
- Use Bayes' Theorem to invert the response matrix $P(\hat{\mu}_i | v_j^{sig}) = \frac{P(v_j^{sig} | \hat{\mu}_i) P^0(\hat{\mu}_i)}{\sum_{l=1}^M P(v_j^{sig} | \hat{\mu}_l) P^0(\hat{\mu}_l)}$
- $\hat{\mu}_i = \frac{1}{\epsilon_i} \sum_{j=1}^N v_j^{sig} P(\hat{\mu}_i | v_j^{sig})$ where ϵ_i is the detector efficiency
- Plug in the newly obtained $P(\hat{\mu}_i | v_j^{sig})$ and $\hat{\mu}_i$ as new priors, then repeat
- Terminate before the wildly oscillating true inverse is reached (usually ~ 4 iterations) to preserve some smoothness

RooUnfold-Bayes

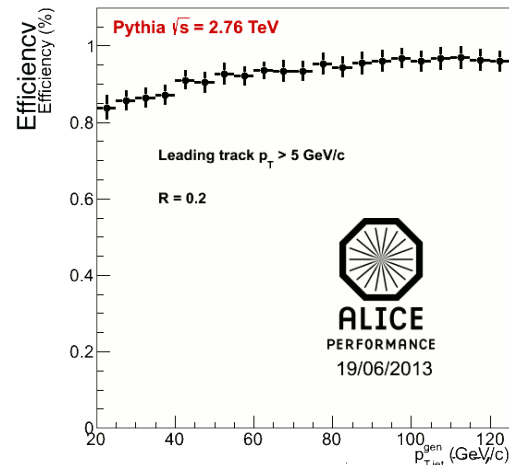
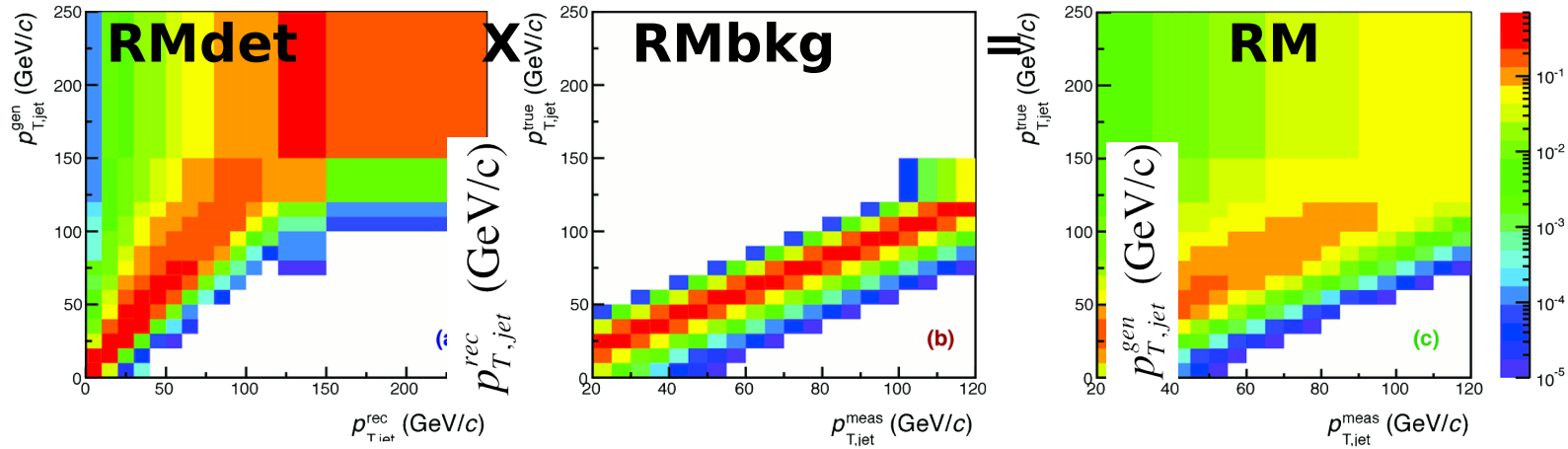
- RooUnfoldTest.cxx
- method = Bayes
- Exponential training and testing



About unfolding...

- d'Agostini (author of Bayesian unfolding algorithm) says you should avoid it if you can
- Necessary when experimental resolution is poor
 - Ex: Single particle spectra $\frac{\sigma_p}{p} \ll w_{bin} \rightarrow$ unfolding unnecessary
 - Ex: Jet spectra $\frac{\sigma_p}{p} \approx w_{bin} \rightarrow$ unfolding necessary
- Algorithm assumes response matrix is correct
 - Matching reconstructed and simulated jets is non-trivial!
- Corrects for multiple experimental effects simultaneously
 - Difficult to disentangle different effects
 - Leads to non-trivial uncertainty correlations between data points due to algorithm
 - May not handle systematic correlations between effects correctly

Jets in ALICE: Response Matrix Construction



Anti- k_T R=0.2

- $p_{T,track} > 0.15$ GeV/c
- $E_{T,cluster} > 0.30$ GeV
- $p_{T,track}^{leading} > 5$ GeV/c

(a) **RM_{det}** Detector response matrix
 (b) **RM_{bkg}** Background fluctuation matrix
 (c) **RM_{tot} = RM_{bkg} × RM_{det}**

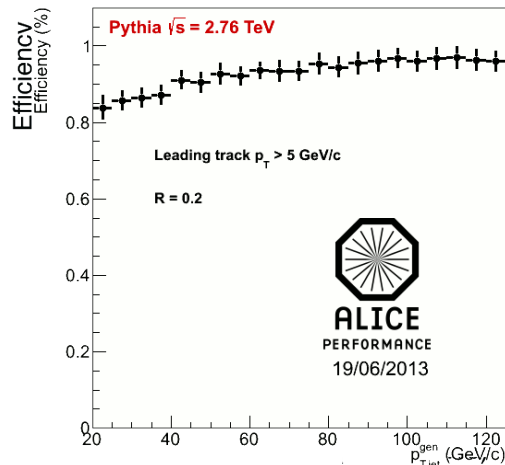
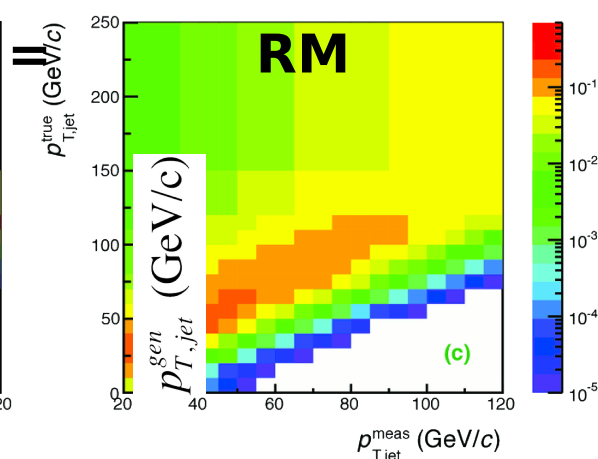
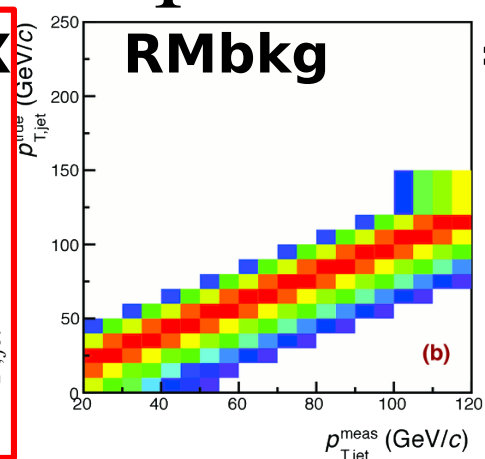
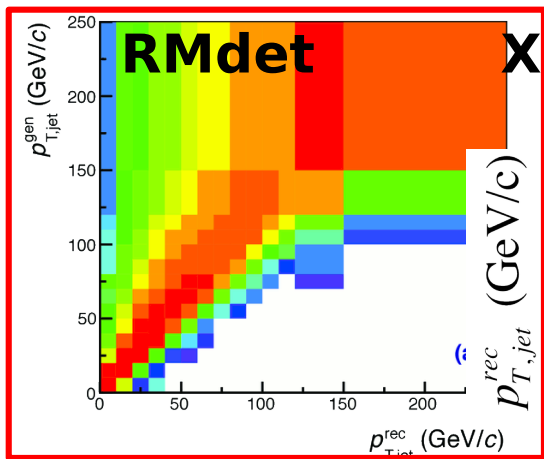
Pb-Pb $\sqrt{s_{NN}} = 2.76$ TeV
0-10% Centrality

ALICE PERFORMANCE
 15/10/2012

RM_{bkg} and RM_{det} are approximately factorizable

Jets in ALICE: Response Matrix Construction

DETECTOR EFFECT



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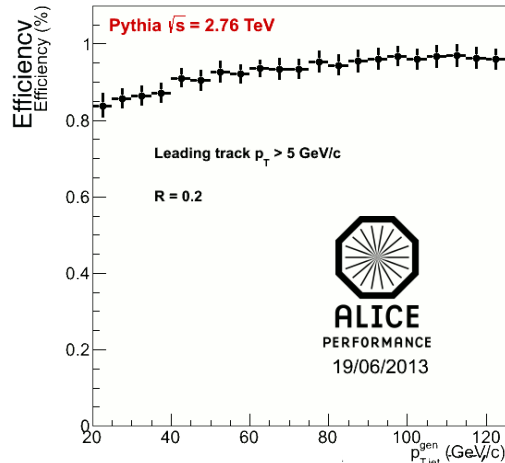
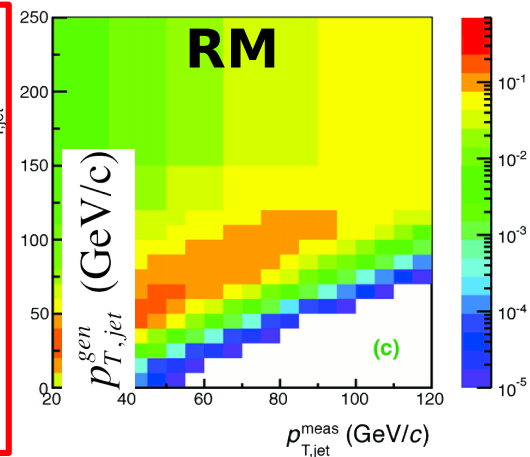
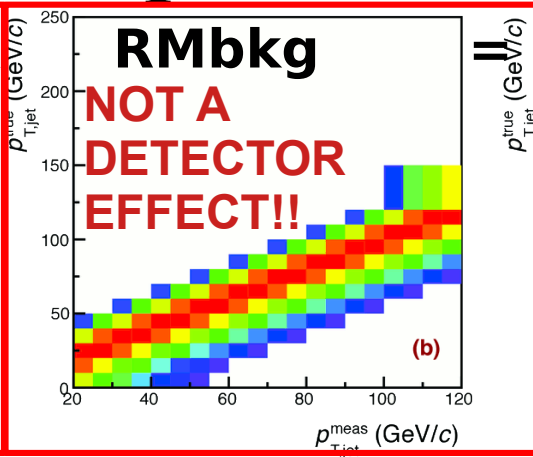
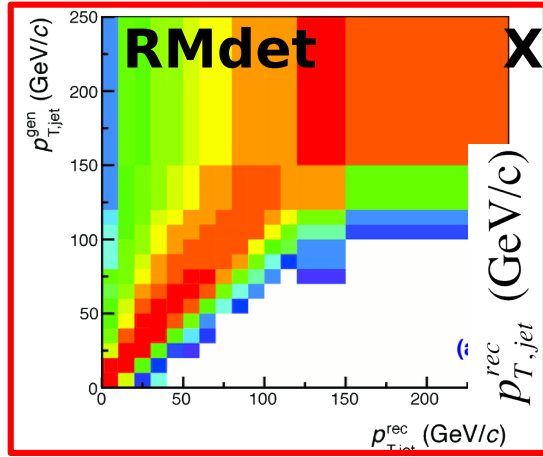


ALICE
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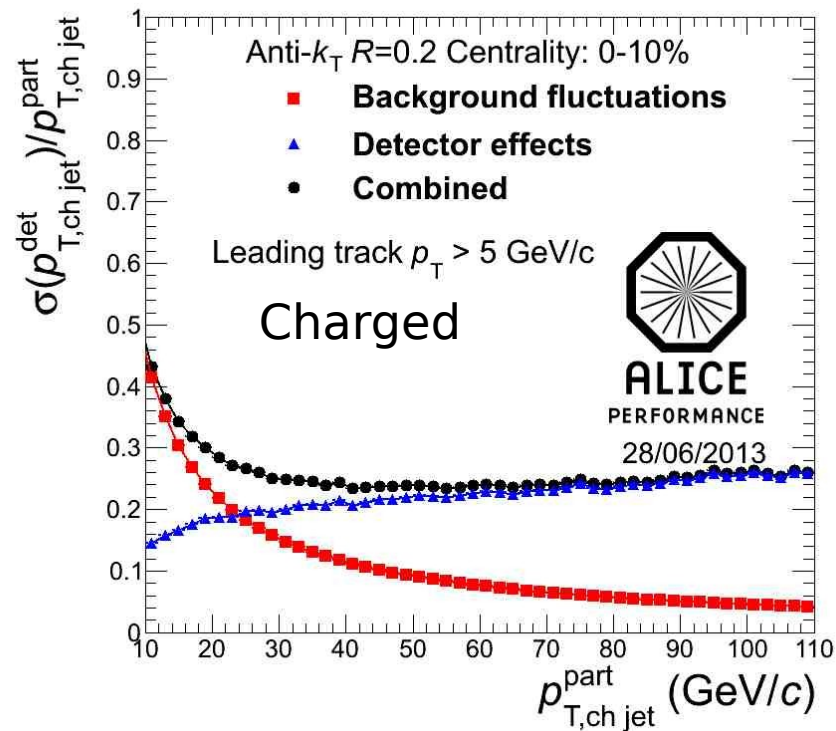
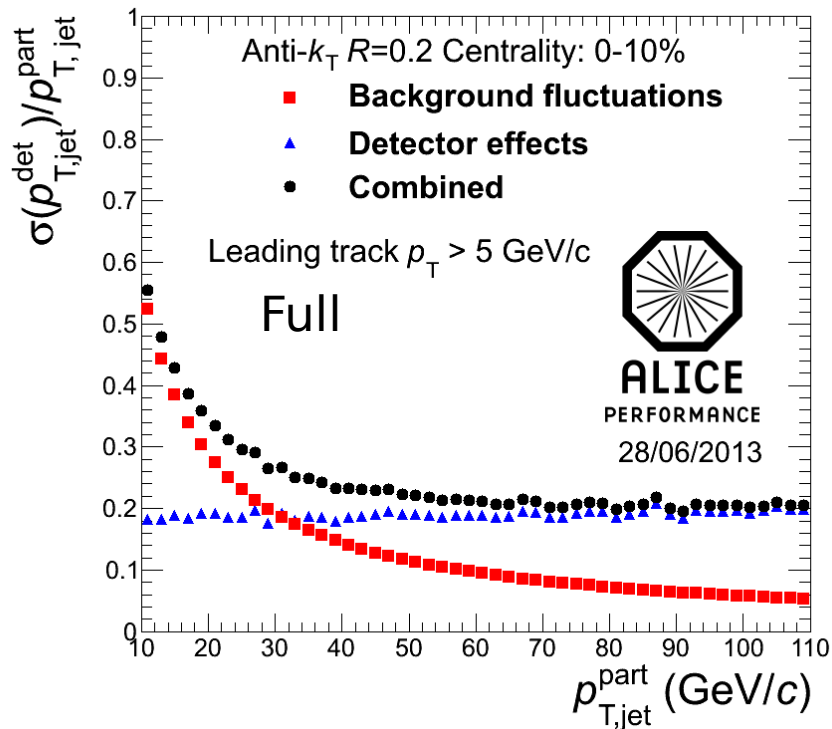
ALICE
PERFORMANCE
15/10/2012

RM_{bkg} and RM_{det} are approximately factorizable

Response matrix includes assumptions about

- Detector response
 - Including particle composition of jets!
- Fragmentation and hadronization
 - How does hadronization influence the width of your jet?
- Background and/or background fluctuations
- How you match reconstructed (“detector level”) and true (“particle level”) jets

Jet Momentum Resolution



• Jet resolution

- Dominated by background fluctuations at low momentum
- Dominated by detector effects at high momentum

Mini-summary

- Jet energy resolution is fundamentally large
 - Measuring multiple correlated particles!
 - Be skeptical of jet measurements with $<10\%$ uncertainties
- Unfolding is complicated, often unstable, and hard
- Construction of response matrix includes several assumptions

Jets in A+A collisions: How to compare to models

Snowmass Accord: Apply the same algorithm to data and your model. Then the measurement and the calculation are the same.

Rivet: Apply the same algorithm to data and your model. Then the measurement and the calculation are the same.

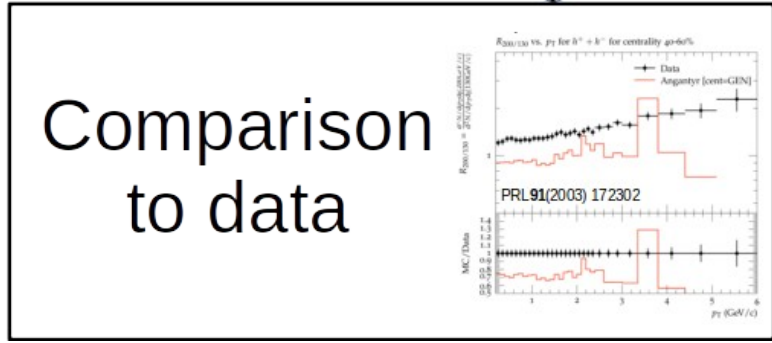
What is Rivet?



HepMC

HEPData

Rivet



Why use Rivet?

- Facilitates comparisons between Monte Carlos and data
- It's not that hard
- It preserves analysis details

Rivetizing Heavy Ion Collisions at RHIC 2020

November 30, 2020 to December 4, 2020

Online

US/Eastern timezone

Overview

Remote connection

Announcement

Registration

Participant List

Organizing Committee

Code of Conduct

HEPData@RHIC

Support

✉ christine.natgrass@utk.edu

✉ antonio.silva@cern.ch

Workshop to implement RHIC analyses in Rivet



Starts Nov 30, 2020, 9:00 AM

Ends Dec 4, 2020, 12:00 PM

US/Eastern



Online



[Antonio Carlos Oliveira da Silva](#)

[Christine Natgrass](#)



There are no materials yet.



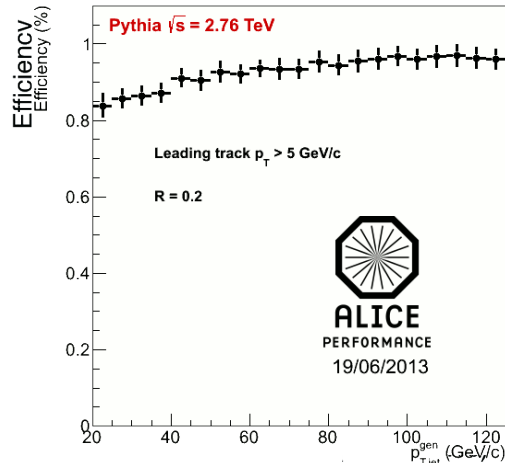
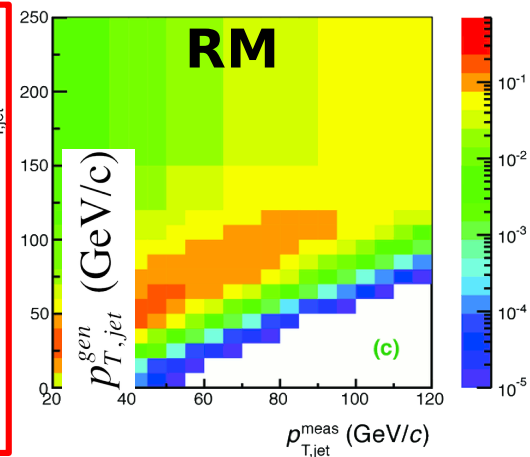
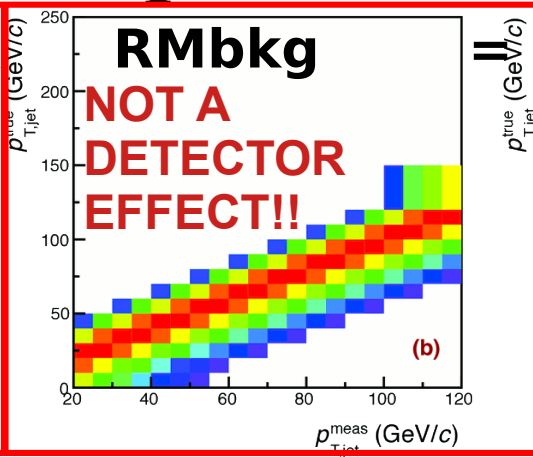
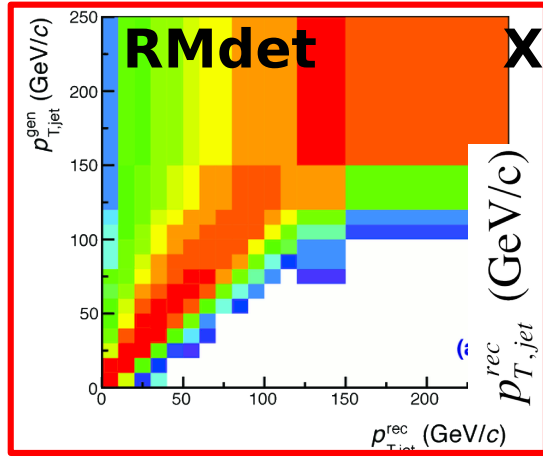
Registration

Registration for this event is currently open.

[Register now >](#)

Jets in ALICE: Response Matrix Construction

DETECTOR EFFECT



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ALICE
PERFORMANCE
15/10/2012

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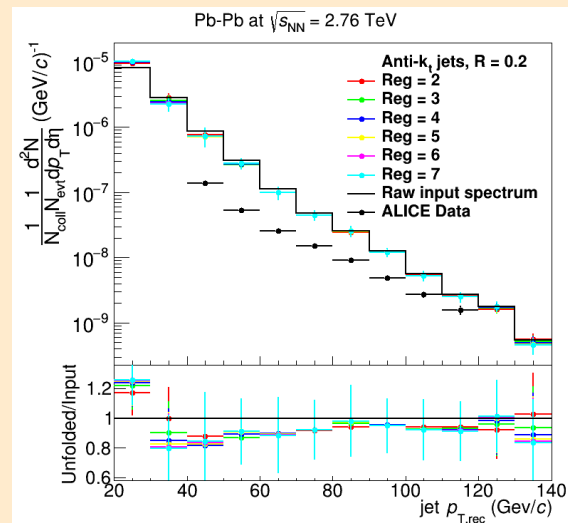
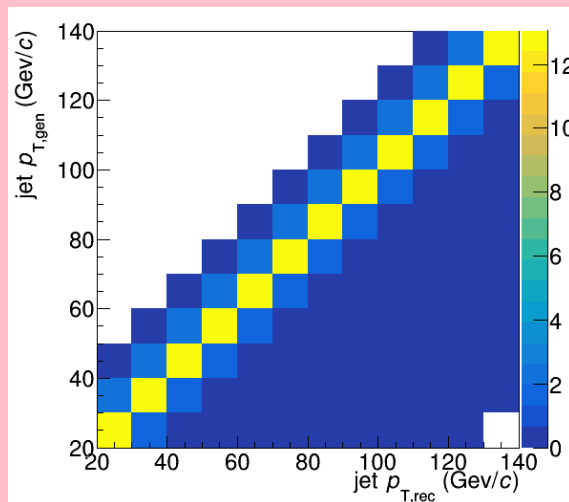
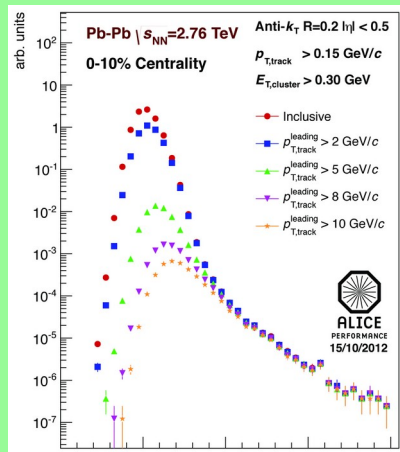
Analysis steps: Full Monte Carlo

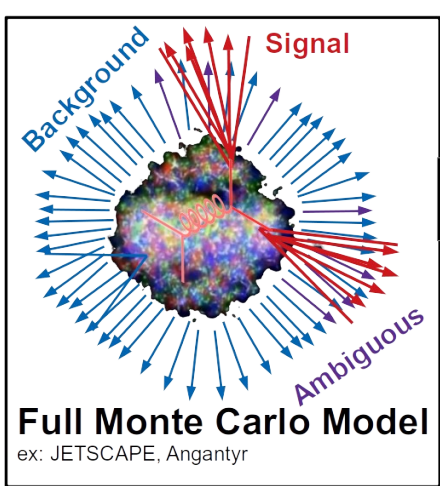
Particles

Jet finding algorithm

Jet candidates

Background subtraction





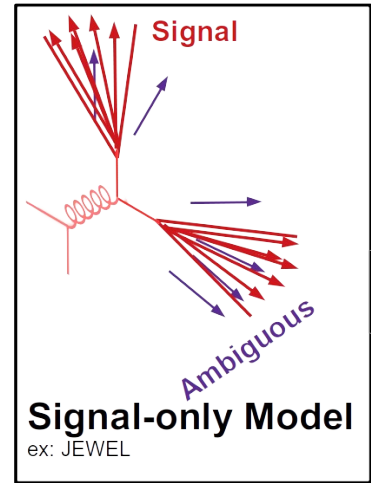
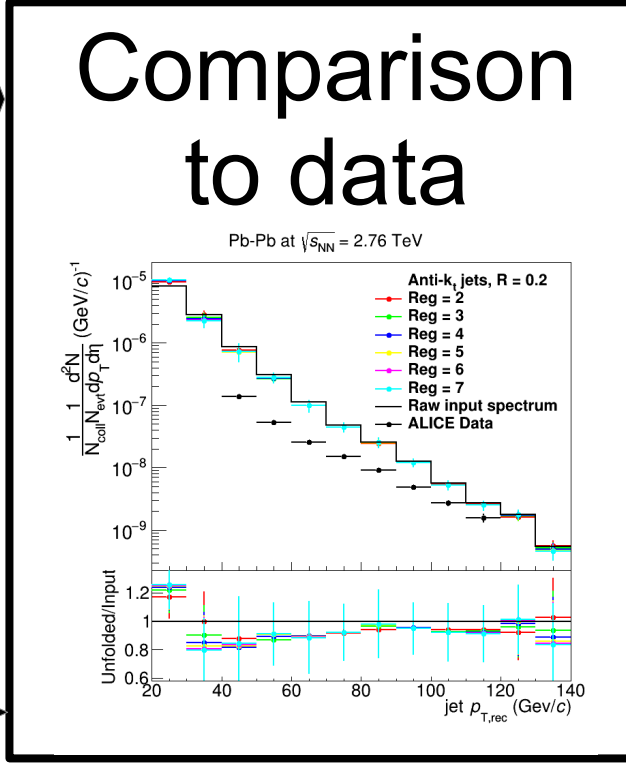
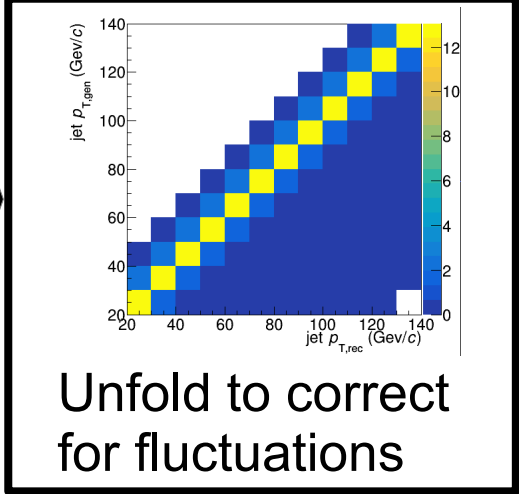
HepMC

Rivet

HEPData

HepMC

Rivet

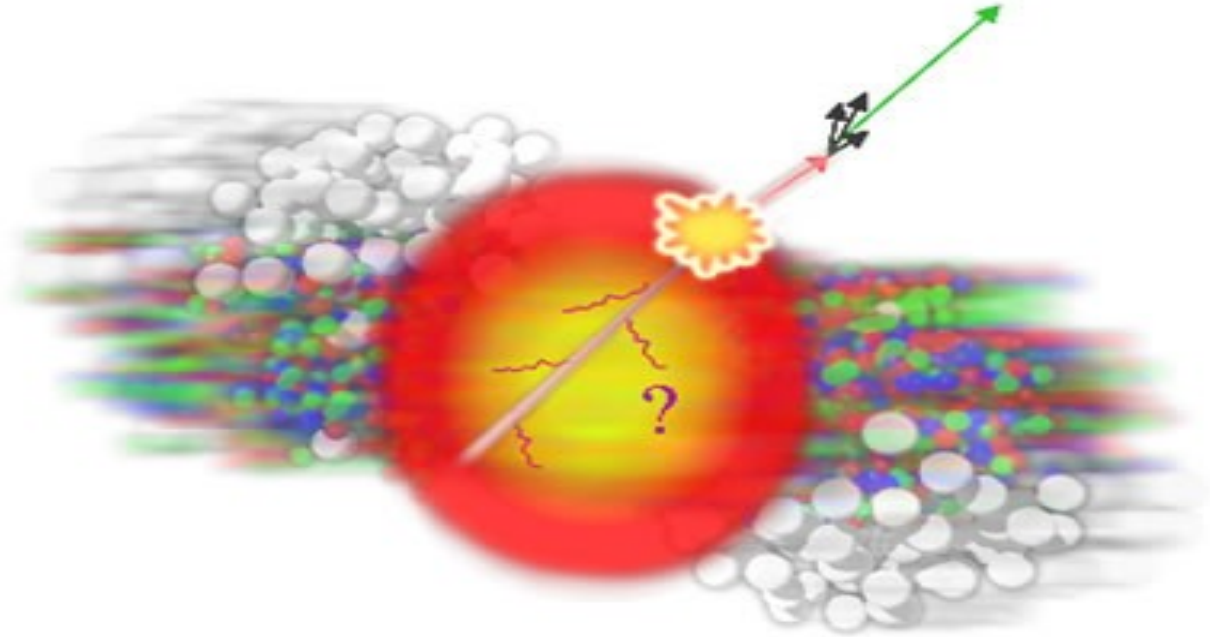


Mini-summary

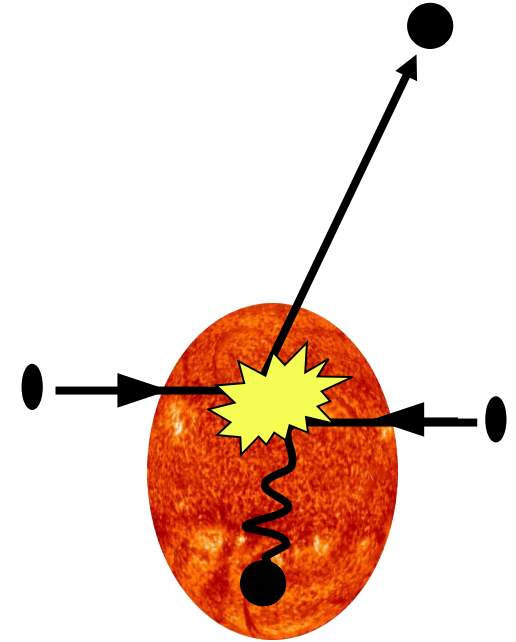
- Experimental techniques can bias measurement in subtle ways
 - Background subtraction
 - Kinematic cuts
 - Choice of jet finder, R
 - Centrality determination
 - Technique for finding reaction plane
- Unclear how these influence the measurement
- Safest to do the same analysis on data and model
 - But unfolding is necessary in a full Monte Carlo model!

A skeptic's guide to jets

Part 2: Where we are going



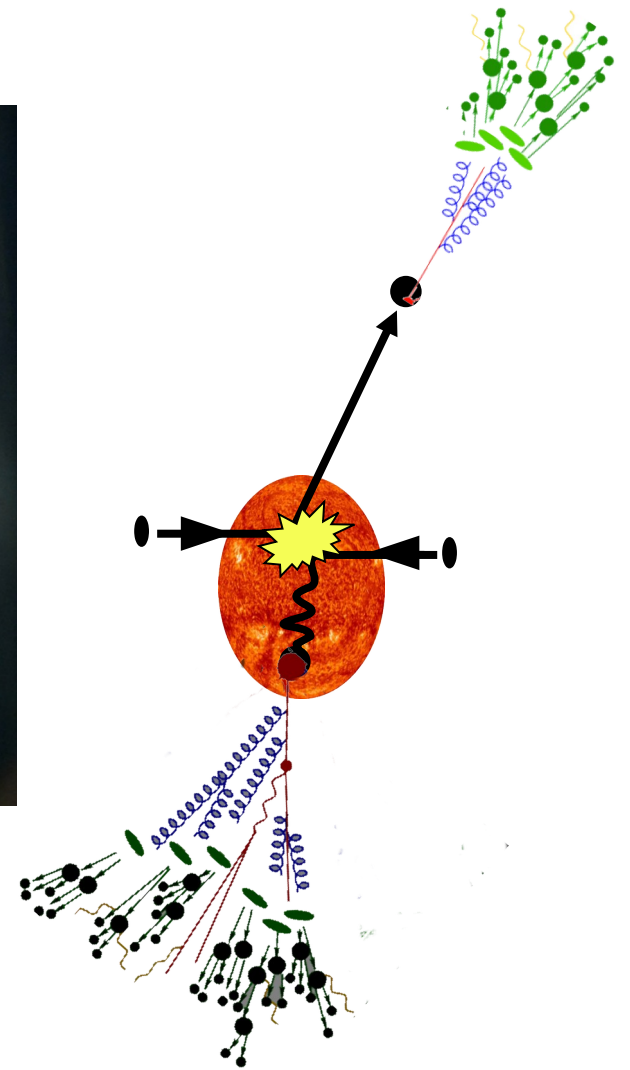
Christine Nattrass
University of Tennessee, Knoxville



There is no partionic energy loss.



There is only partonic energy redistribution.



What is jet (sub)structure?

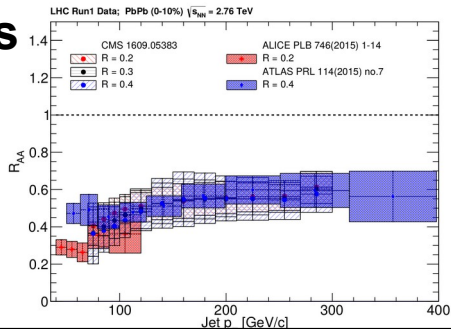
- A Whatever I am measuring!
- B Any new jet observable
- C Any observable which measures the structure of jets.
- D A cool buzzword
- E I don't know but it sounds cool and gets me talks/grants

Types of observables

I. Minimally sensitive to structure

Observables

- (Jet) R_{AA}
- A_j
- I_{AA}
- (Jet) v_2



Jet properties:

- E

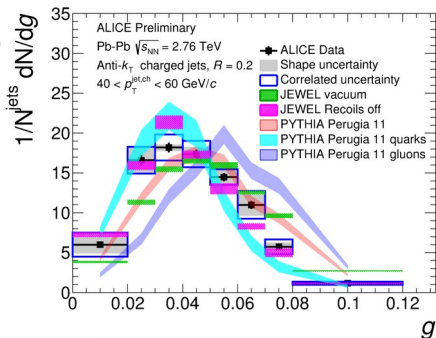
Higher precision

Higher/different sensitivity?

III. Sensitive to distribution of structures

Observables

- Girth
- Dispersion
- p_{TD}
- Jet mass
- ...



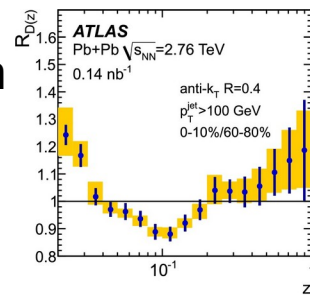
Jet properties:

- E
- Const. p_T
- ϕ, η

II. Sensitive to <structure> of <jets>

Observables

- Fragmentation functions
- Jet shapes
- Correlations
- ...



Jet properties:

- E
- Const. p_T , ϕ, η

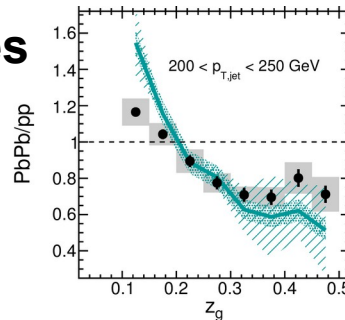
Average background subtraction OK

Need new background subtraction technique

IV. Sensitive to parton shower structure

Observables

- Grooming
- $N_{\text{subjettness}}$
- ...



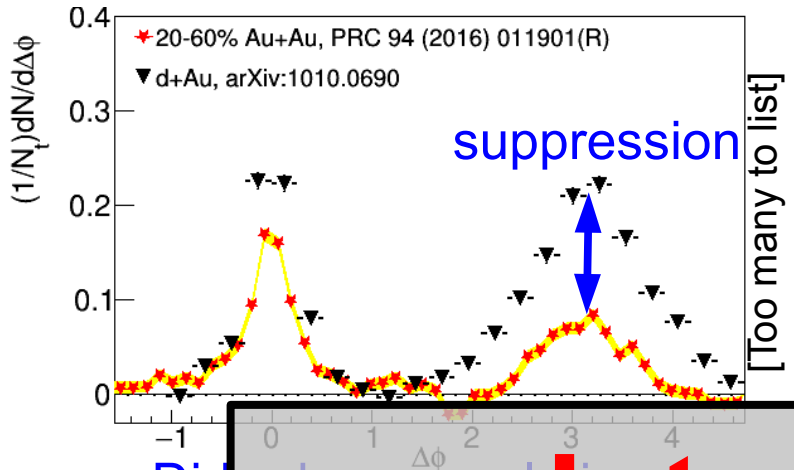
Jet properties:

- E
- Const. p_T , ϕ, η
- Multi-const. correlations

Jets not required

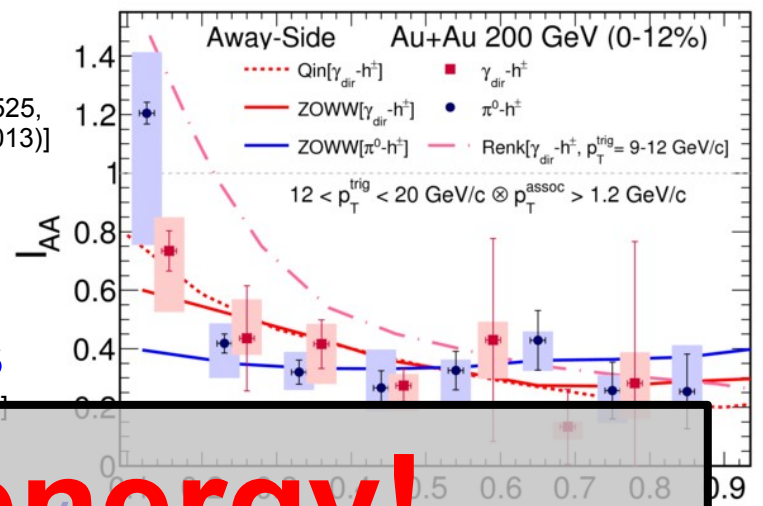
Jets required

Type I: Energy loss



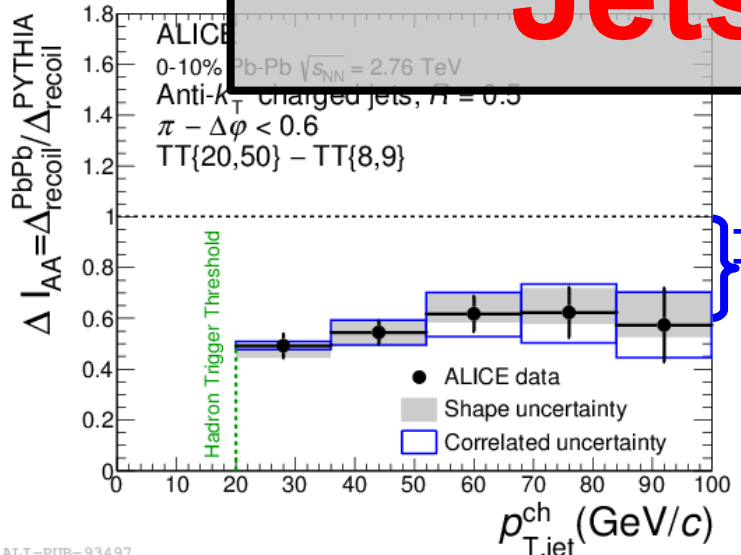
Jet v_2
 [Phys. Lett. B 753 (2016) 511-525,
 Phys. Rev. Lett. 111 152301 (2013)]

γ -jet correlations



uoiissærdnns
 [Phys. Rev. C 80:024908, 2009,
 Phys. Rev. D 82:072001, 2010,
 Phys. Rev. C 82:034909, 2010
 Physics Letters B 760 (2016)]

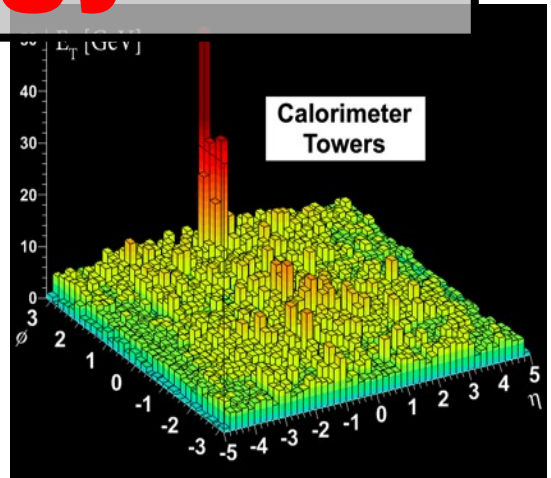
Jets lose energy!



uoiissærdnns

[JHEP 09 (2015) 170,
 Phys. Rev. C 96, 024905 (2017)]

Au+Au $\sqrt{s_{NN}}=200$ GeV
 $\hat{q} = 1.2 \pm 0.3 \text{ GeV}^2$
Pb+Pb $\sqrt{s_{NN}}=2.76$ TeV
 $\hat{q} = 1.9 \pm 0.7 \text{ GeV}^2$
 [Phys. Rev. C 90, 014909 (2014)]



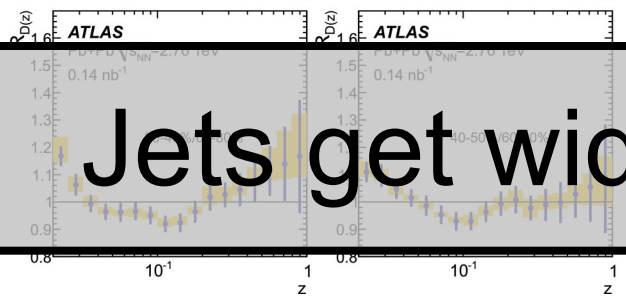
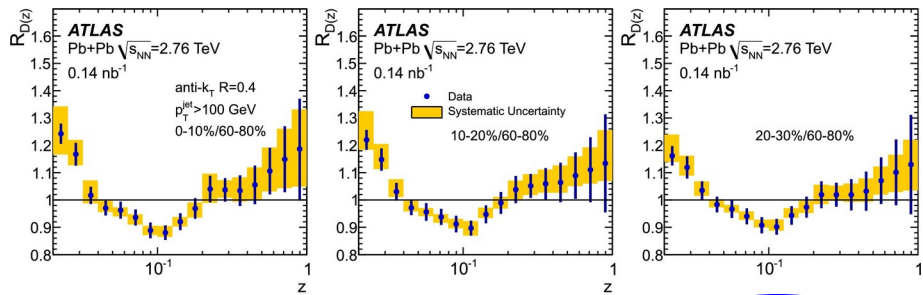
[Phys. Rev. C 84:024906, 2011,
 Phys. Lett. B 712 (2012) 176,
 Phys. Rev. Lett. 105:252303, 2010,
 Phys. Rev. Lett. 119, 062301 (2017)]

Hadron-jet correlations

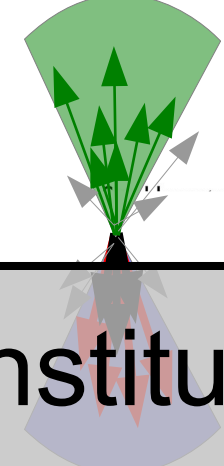
Dijet asymmetry

Type II: Fragmentation

Fragmentation functions with jets



Leading jet



Subleading jet

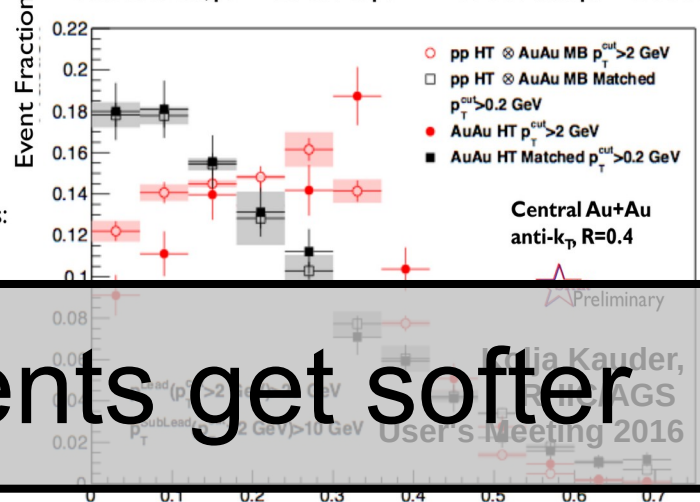


Jet-hadron correlations

Di-jet asymmetry

arXiv:1609.03878

Anti-k_T R=0.4, $p_{T,Lead} > 20$ GeV & $p_{T,SubLead} > 10$ GeV with $p_{T,cut} > 2$ GeV/c



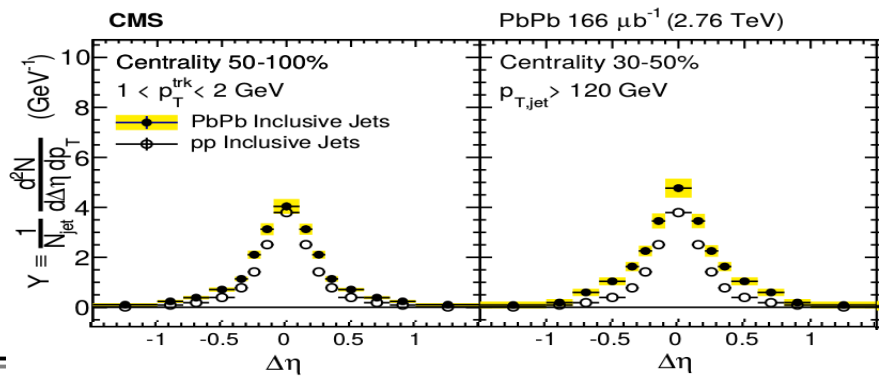
Jets get wider and constituents get softer

Di-hadron correlations

[Lots of papers]

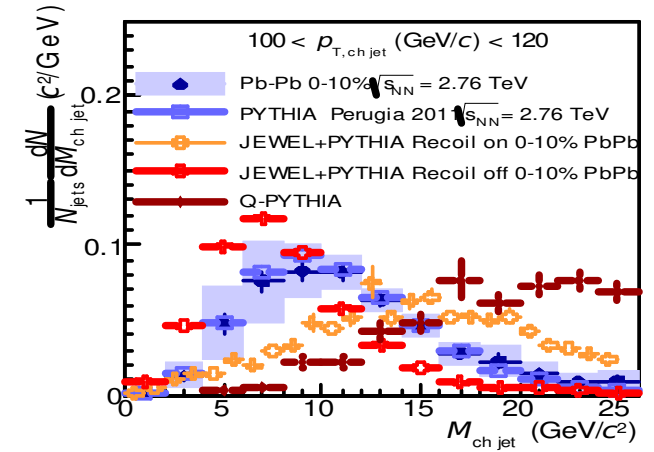
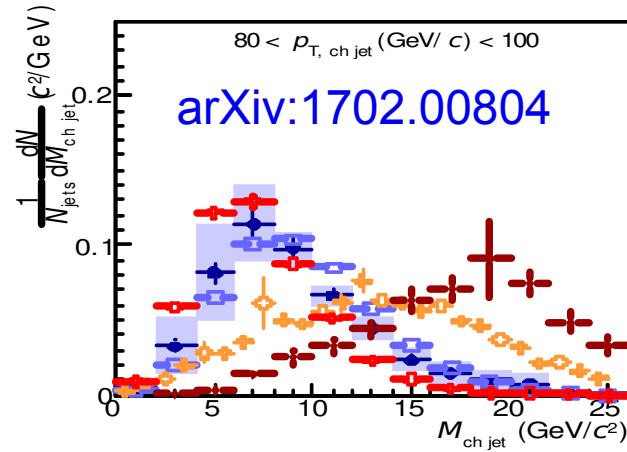
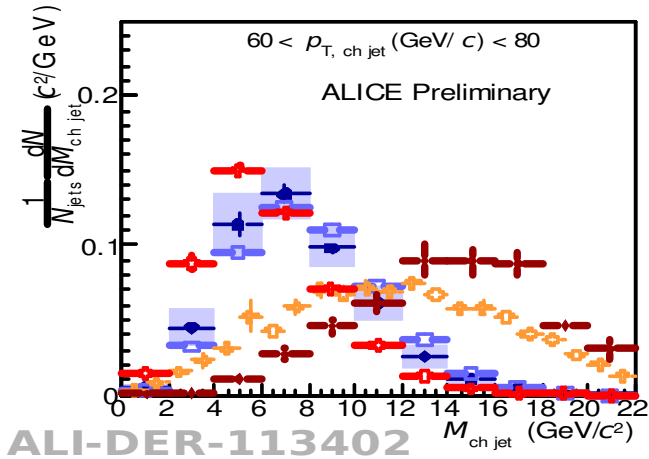
Jet shapes

[arXiv:1708.09429,
arXiv:1512.07882,
arXiv:1704.03046]



Type III: Distribution of properties

Jet mass



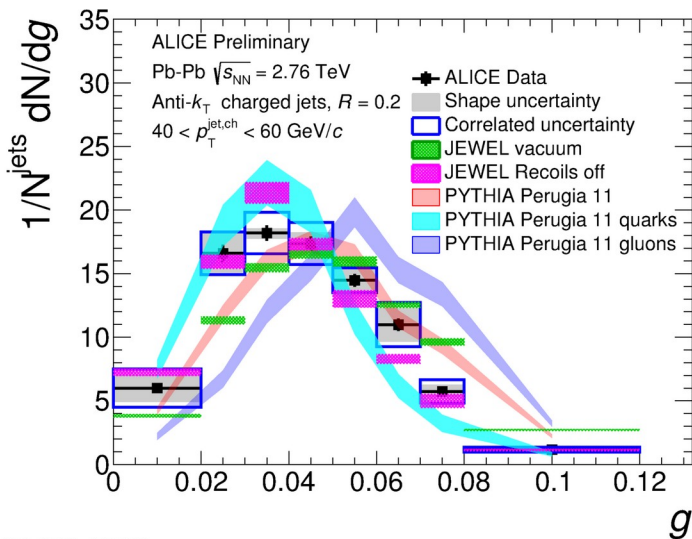
$$M = \sqrt{p^2 - p_T^2 - p_z^2}$$

$$p = \sum_{i=1}^n p_{T_i} \cosh \eta_i$$

$$p_z = \sum_{i=1}^n p_{T_i} \sinh \eta_i$$

- Quenching models (**JEWEL**, **Q-PYTHIA**) show a larger mass than pp-like **PYTHIA** jets
- Pb-Pb measurement can discriminate among these predictions

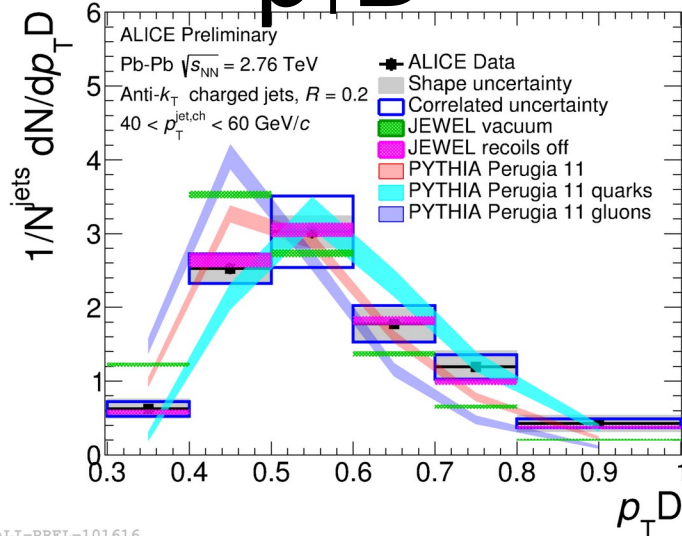
Girth g



ALI-PREL-101608

$$g = \sum_{i \in \text{jet}} \frac{p_T^i}{p_T^{\text{jet}}} r_i$$

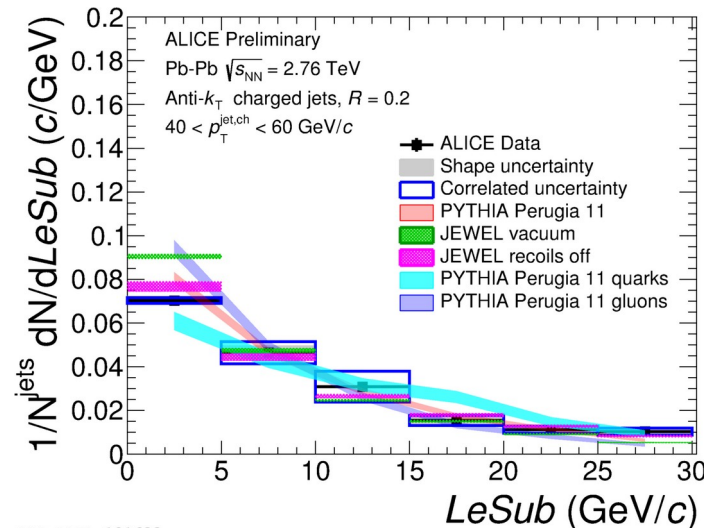
Dispersion $p_T D$



ALI-PREL-101616

$$p_T D = \frac{\sqrt{\sum_{i \in \text{jet}} (p_T^i)^2}}{\sum_{i \in \text{jet}} p_T^i}$$

LeSub



ALI-PREL-101633

$$LeSub = p_T^{\text{leading}} - p_T^{\text{subleading}}$$

Jets are slightly more collimated than in pp

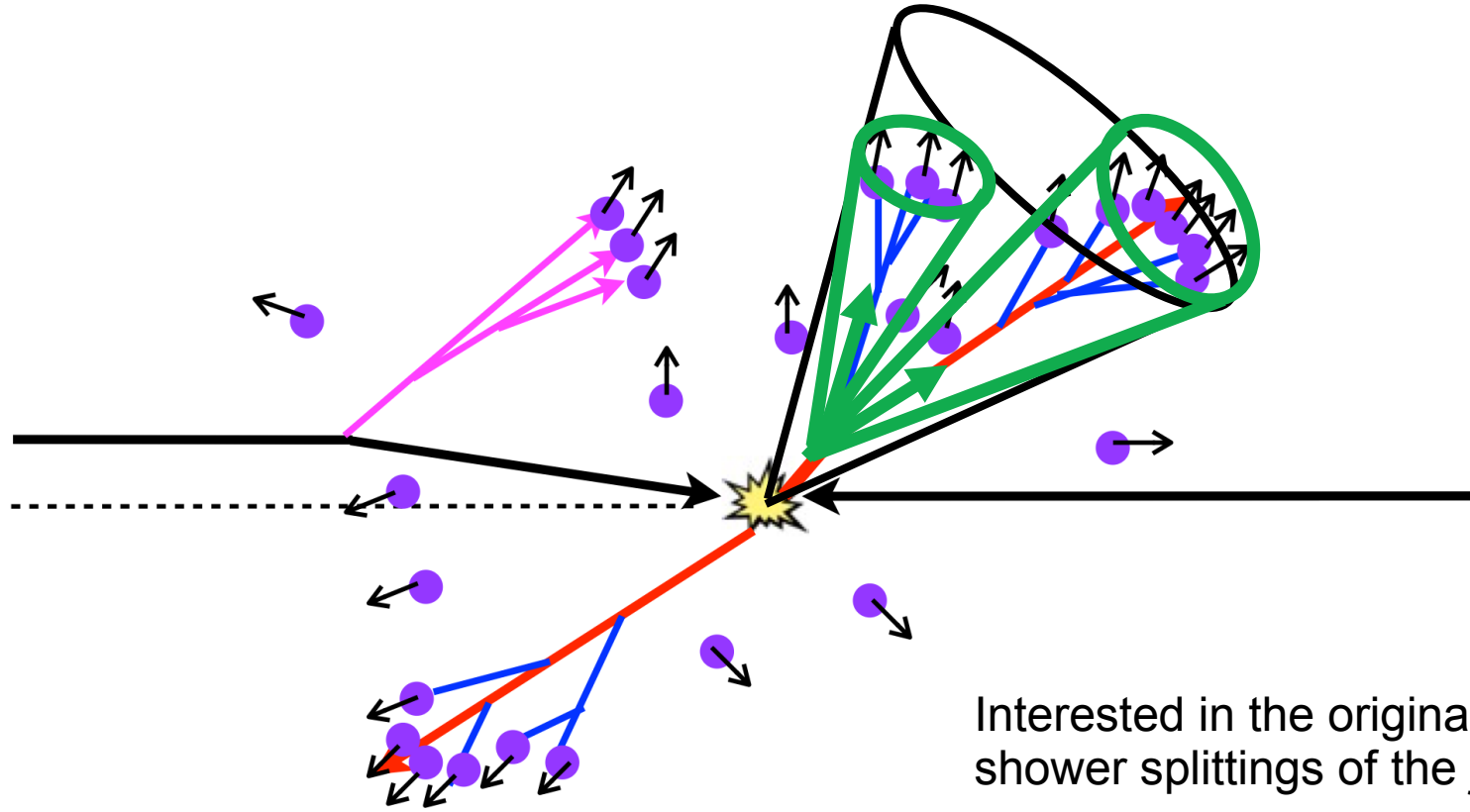
Agrees with PYTHIA

Type IV: Declustering

Note: These slides are from Laura Havener

*A selection. Don't be offended if I skip your favorite.

New tool: jet splittings

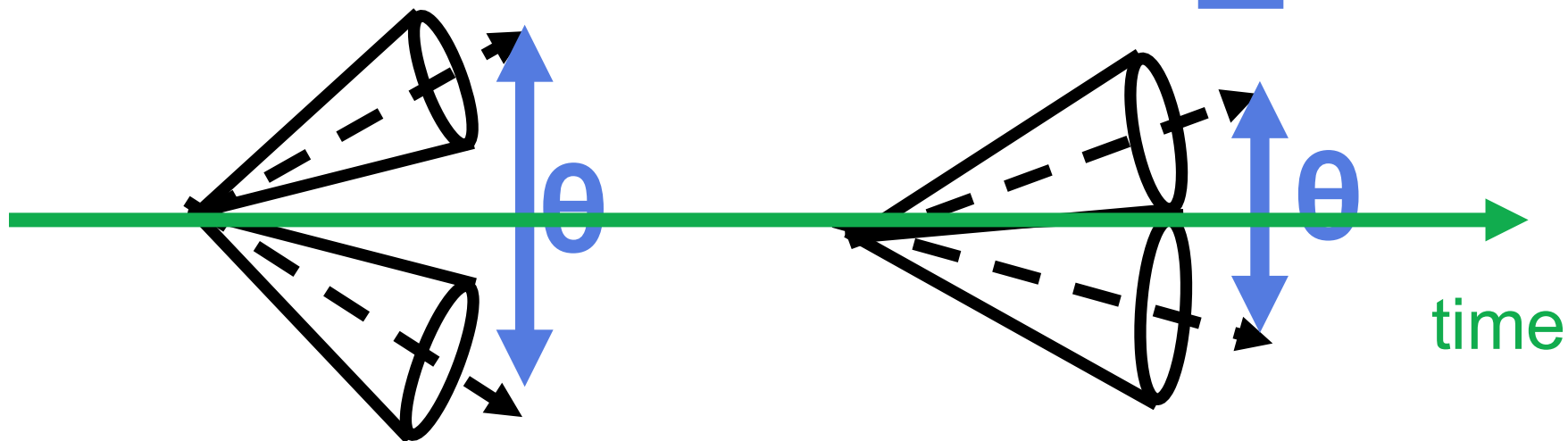


Interested in the original parton
shower splittings of the jet
Which form subjects inside the jet!

Jet splittings: in vacuum

Vacuum jets splittings form at different times

$$t_f^{\text{vac}} = \frac{1}{\theta^2 \omega}$$

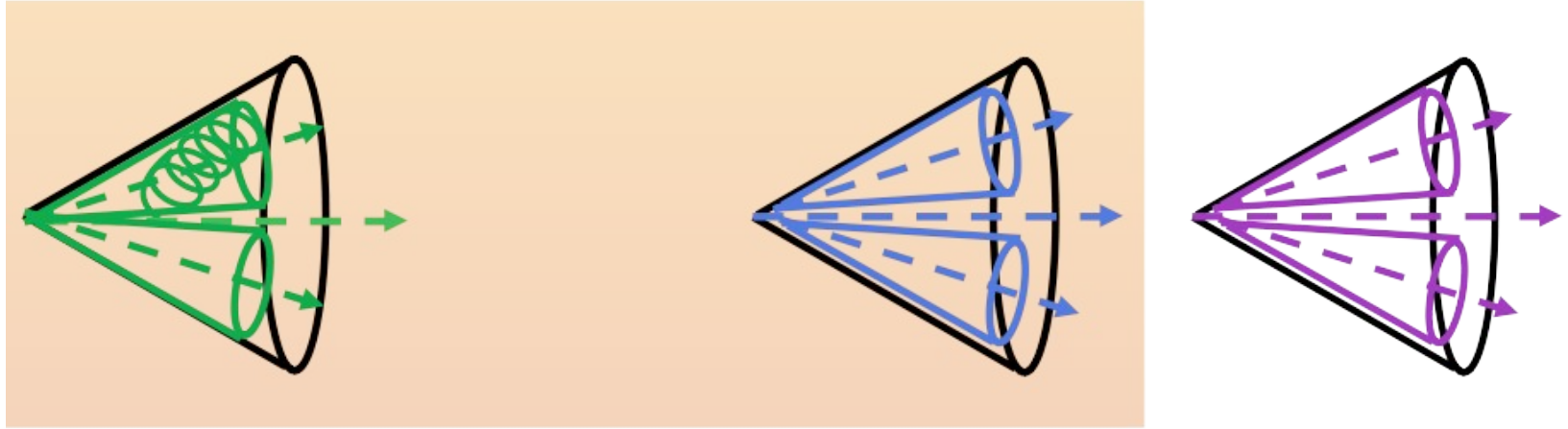


Wider jets form earlier and narrower jets form later

Jet splittings: in medium

Vacuum splittings **in/out** of the medium

$$t_f^{\text{vac}} = \frac{1}{\theta^2 \omega}$$



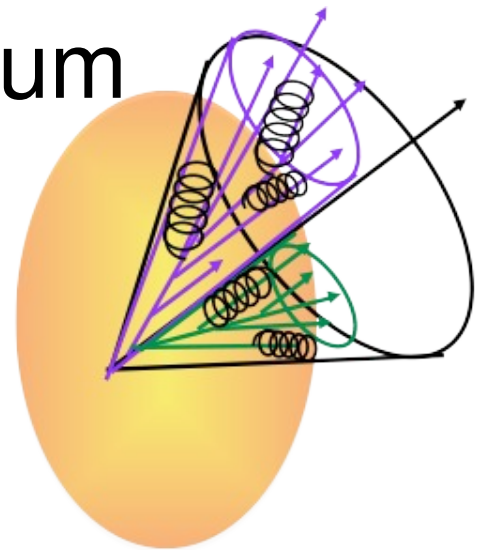
Medium-induced splittings from **gluon radiation**

$$t_g^{\text{med}} = \sqrt{\frac{\omega}{\hat{q}}}$$

Jet splittings: in medium

Coherence: subjects
unresolved and jet loses energy
as a whole

Decoherence: medium
resolves the subjects resulting in a
stronger e-loss

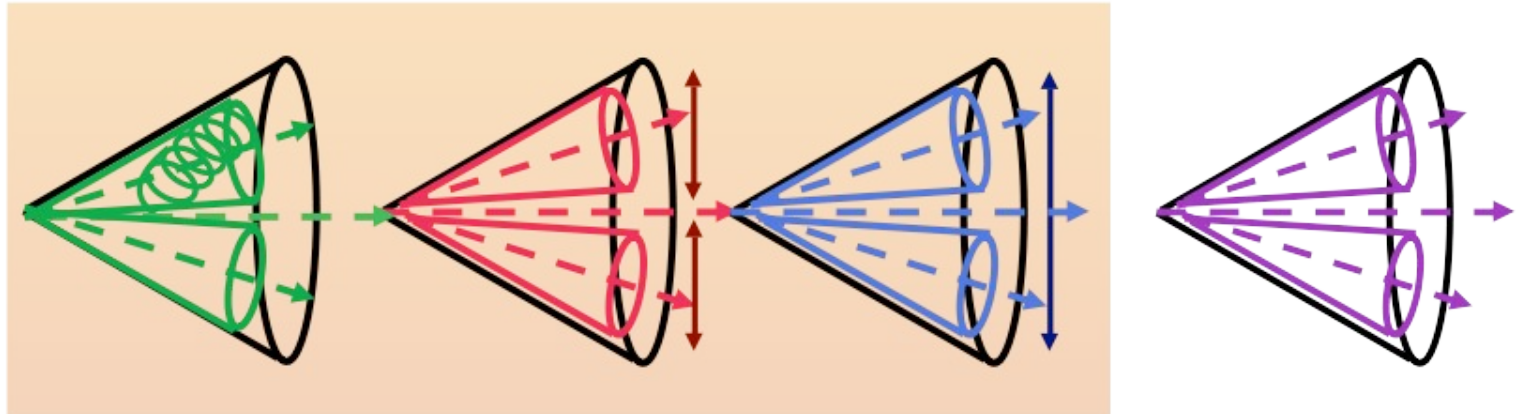


Medium-induced
splittings

Vacuum splittings
inside medium,
resolved

Vacuum splittings
inside medium,
unresolved

Vacuum splittings
outside medium



Exploring the Lund Plane: in vacuum

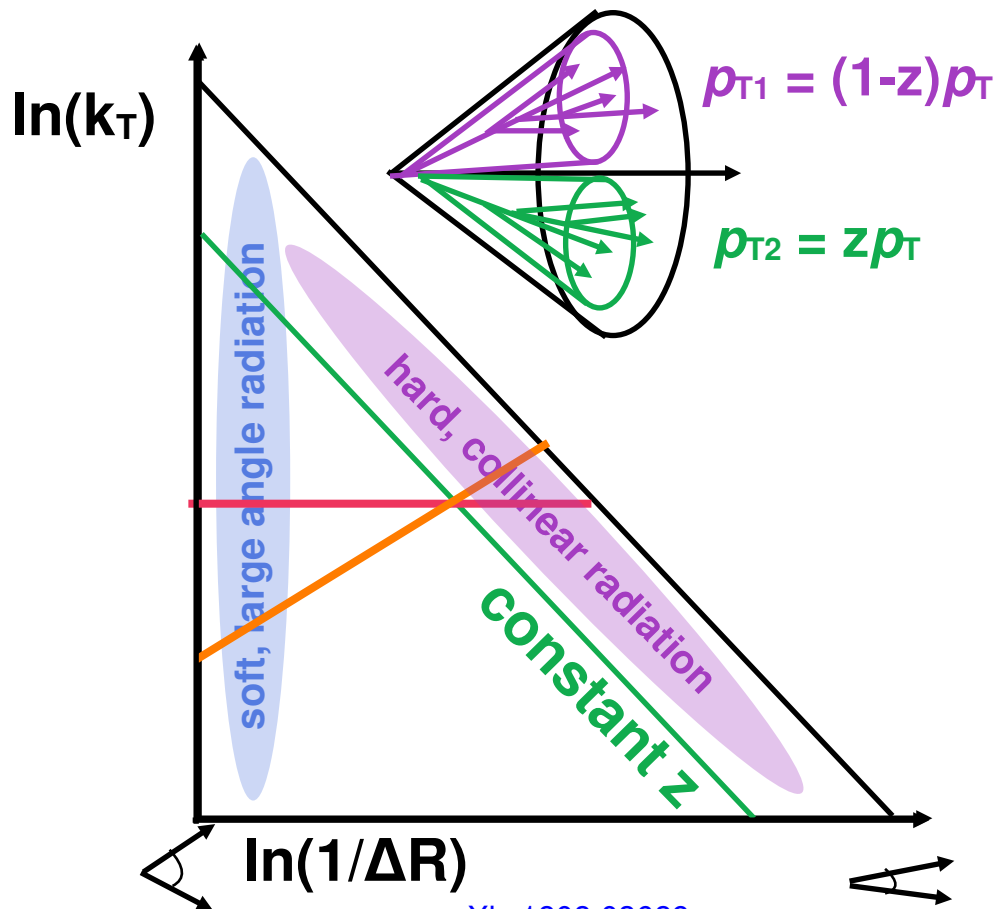
- Lund Diagram*: phase space of jet splitting

*Z. Phys. C43 (1989)

JHEP 12 (2018)

- $\log(k_T) > 0$ separates perturbative from non-perturbative regime
- Formation time: how long until the splitting occurred 1

$$t_f = \frac{1}{(1-z)k_T\Delta R}$$

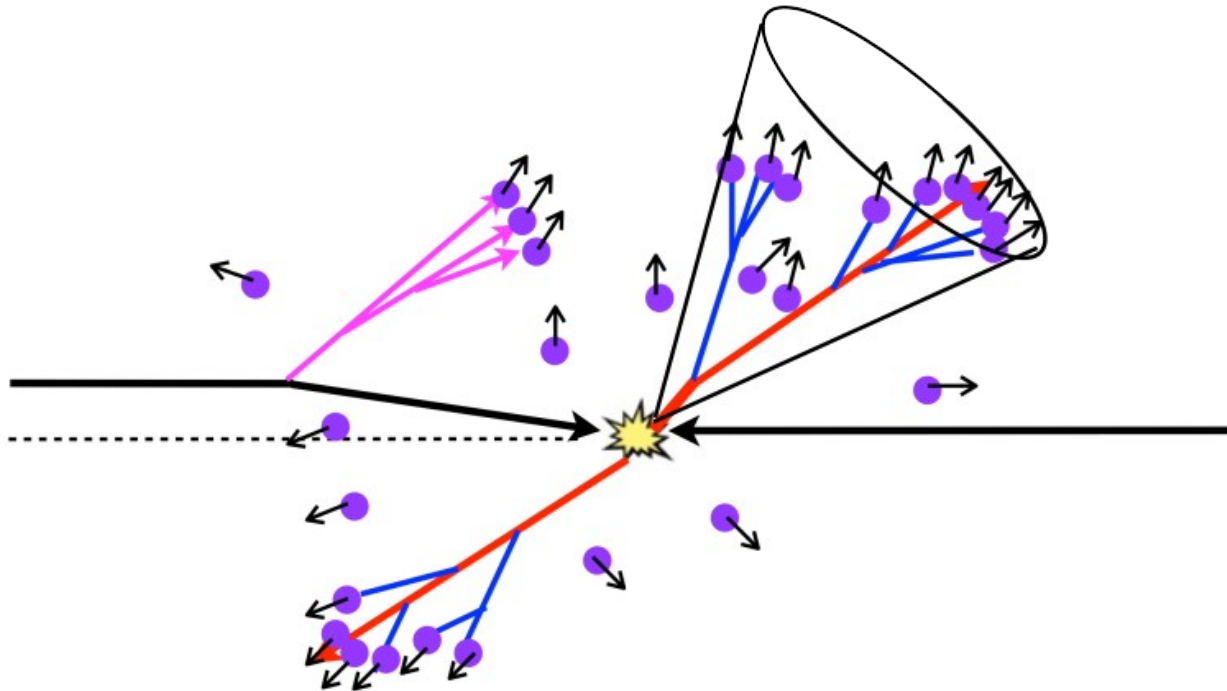


arXiv:1808.03689

Soft drop grooming

- Reconstruct anti- k_T $R=0.4$ charged jets with jet-by-jet constituent background subtraction*

[*JHEP 06 \(2014\) 092](#)



Soft drop grooming

- Reconstruct anti- k_T $R=0.4$ charged jets with *jet-by-jet constituent background subtraction**
*JHEP 06 (2014) 092

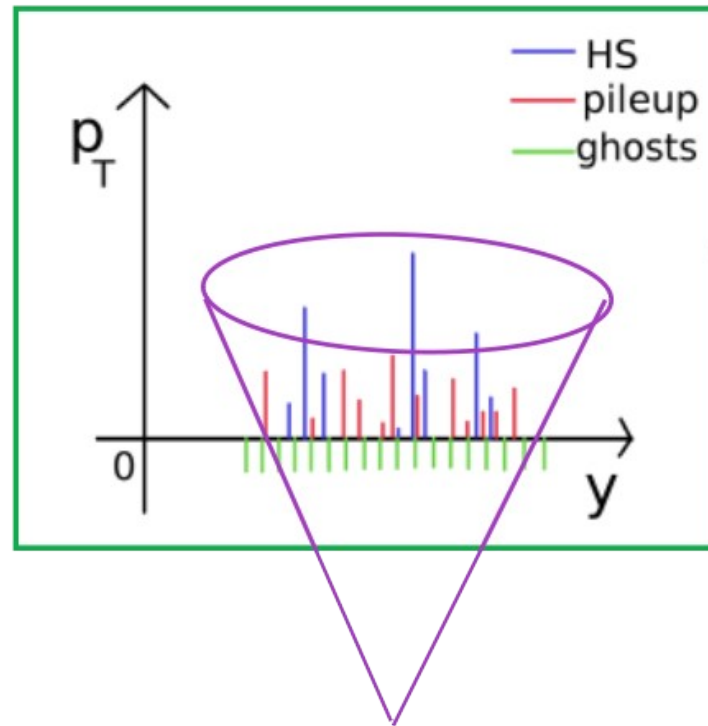
Remove from each constituent inside the jet instead of from the whole jet

Jet-by-jet:

$$p_T^{\text{jet,corr}} = p_T^{\text{jet}} - \rho A$$

Track-by-track (i) in jet:

$$p_T^{i,\text{corr}} = p_T^i - \rho A$$



Groomed variables

- Soft drop grooming variables probe jet splitting

→ z_g : shared momentum fraction between two hardest subjects in parton shower

$$z_g = \frac{\min(p_{Ti}, p_{Tj})}{p_{Ti} + p_{Tj}}$$

How symmetric is the jet splitting?

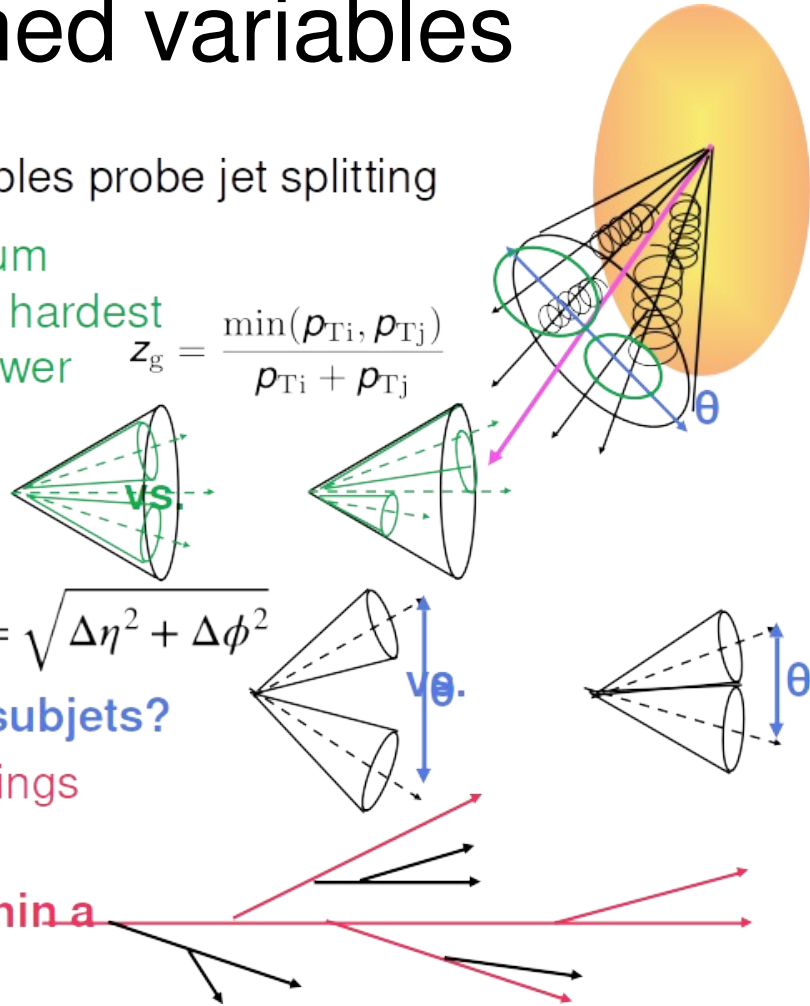
→ R_g : distance between subjects

$$R_g = \sqrt{\Delta\eta^2 + \Delta\phi^2}$$

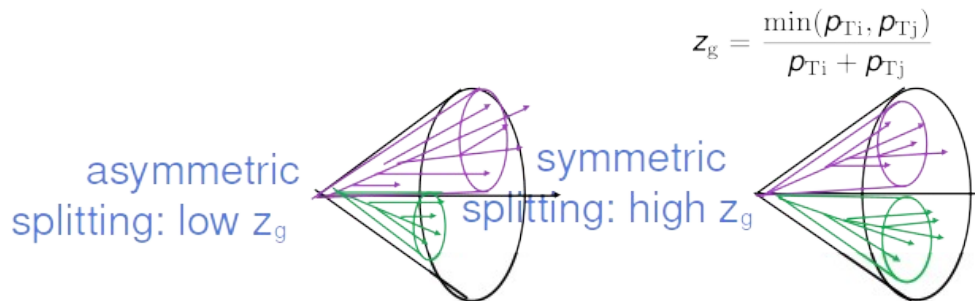
How far apart are the subjects?

→ n_{SD} : number of splittings passing Soft Drop

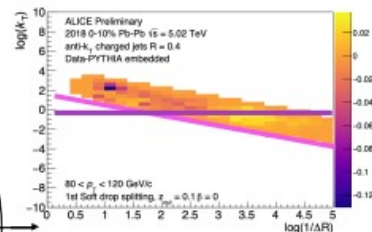
Number of subjects within a jet?



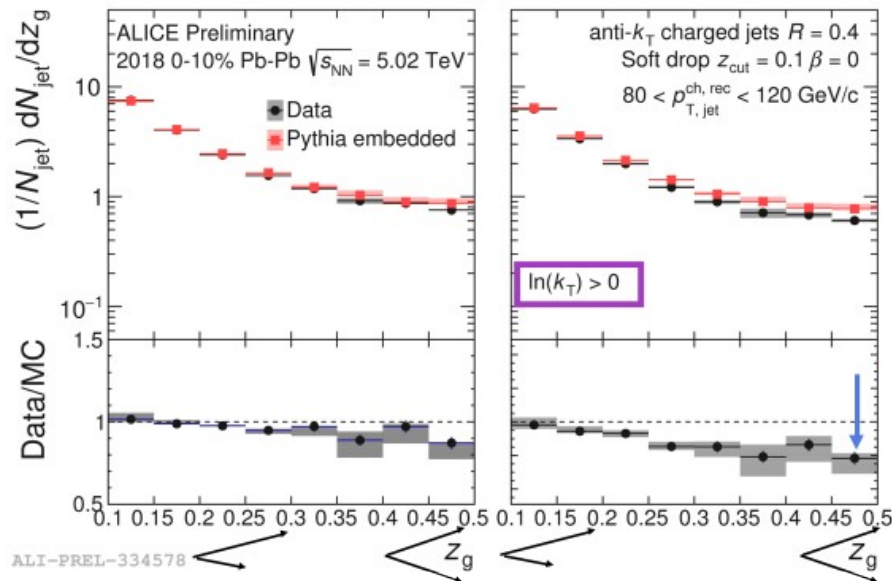
z_g : jet splitting



$$z_g = \frac{\min(p_{Ti}, p_{Tj})}{p_{Ti} + p_{Tj}}$$

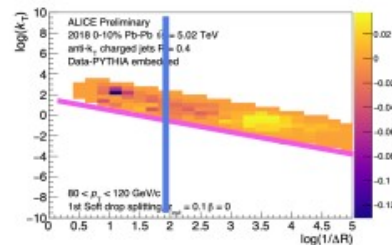
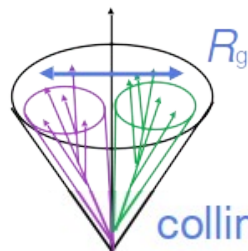


Suppression of symmetric splittings



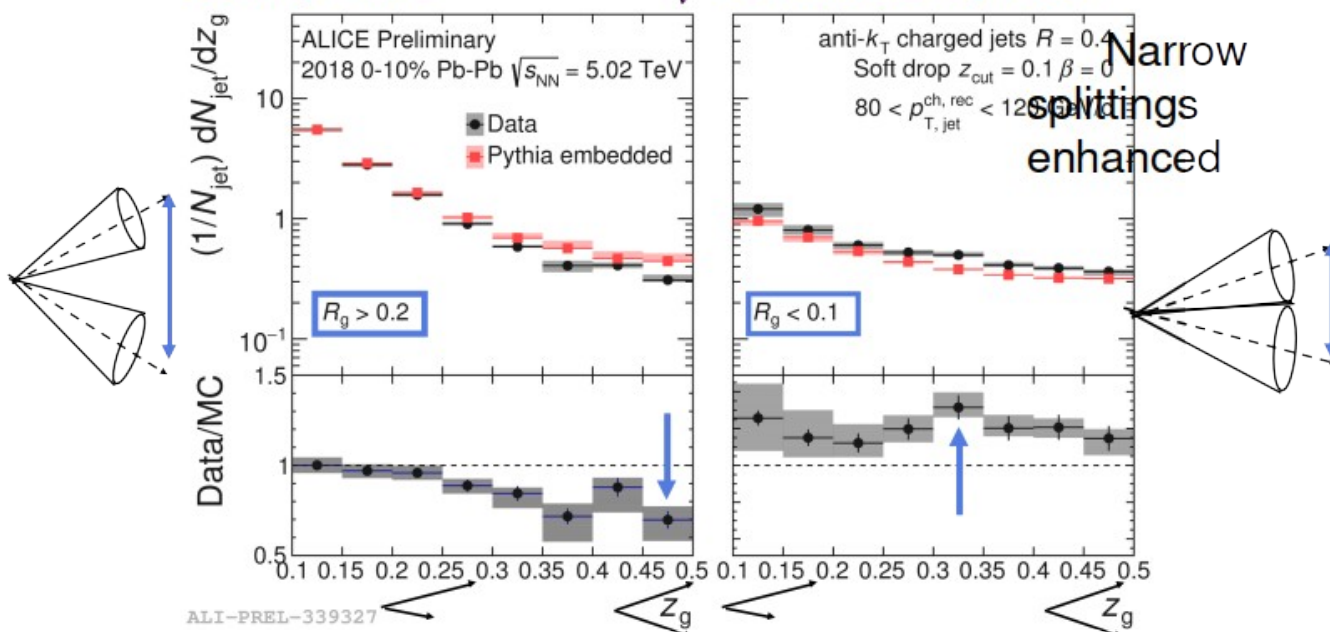
z_g : opening angle

Wide: more significant suppression of symmetric splittings



wide $R_g > 0.2$

collimated $R_g < 0.1$

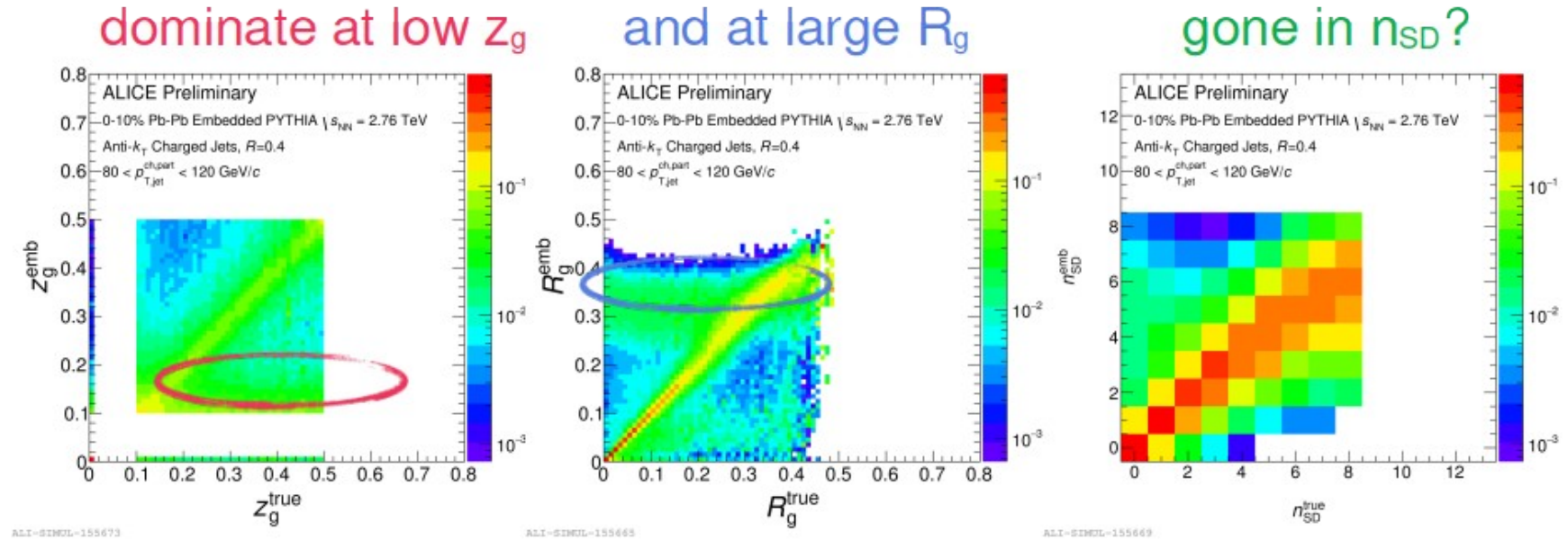


ALI-PREL-339327

Background

Unfolding: jet splitting

Uncorrelated background leads to subjets being picked up as incorrect or “fake” splittings



Non-diagonal response prohibits unfolding

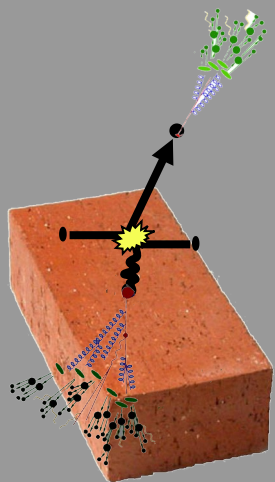
Mini-summary

- “Jet substructure” is used inconsistently
- Search for new observables
 - Haven’t really used most of the “old” ones!
- So far it’s a mixed bag
 - Many are insensitive
 - Some may have some promise
 - Background tricky

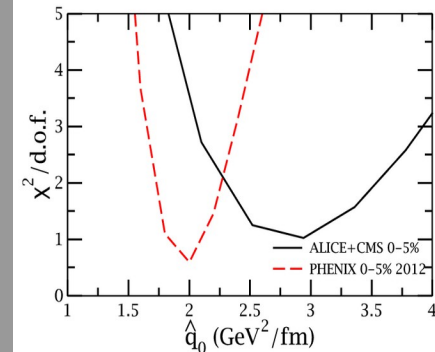
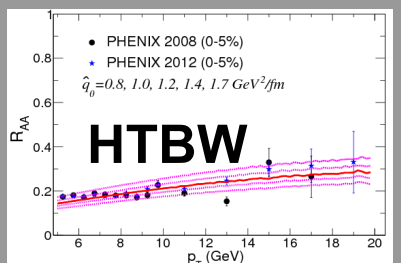
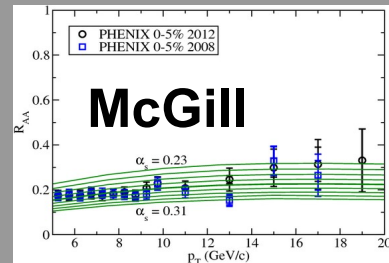
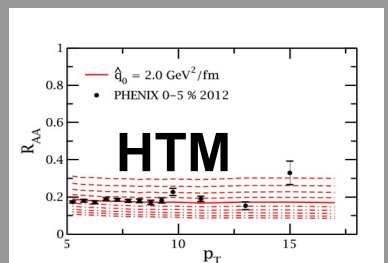
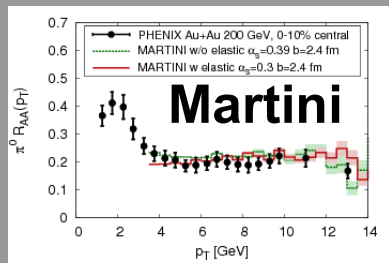
JETSCAPE

JET collaboration

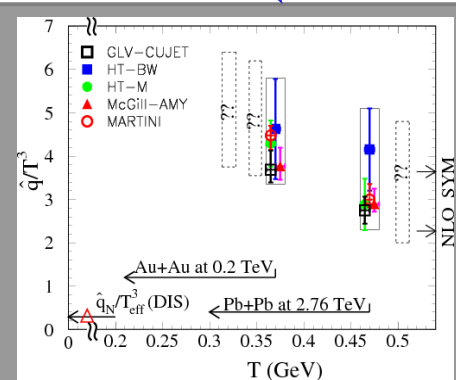
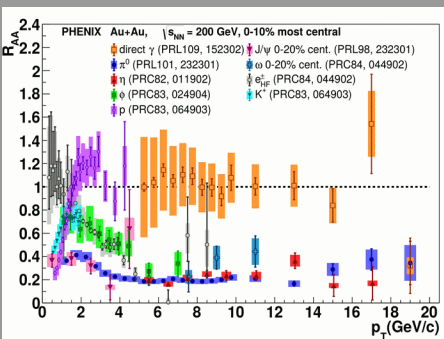
Phys. Rev. C 90, 014909 (2014)



QGP brick + jet



χ^2 minimization

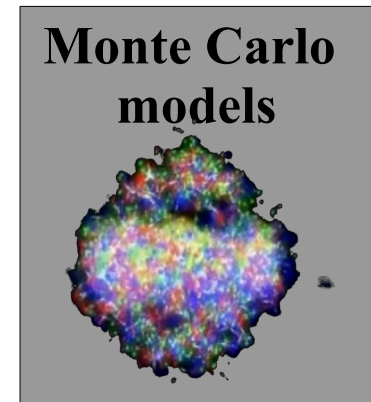
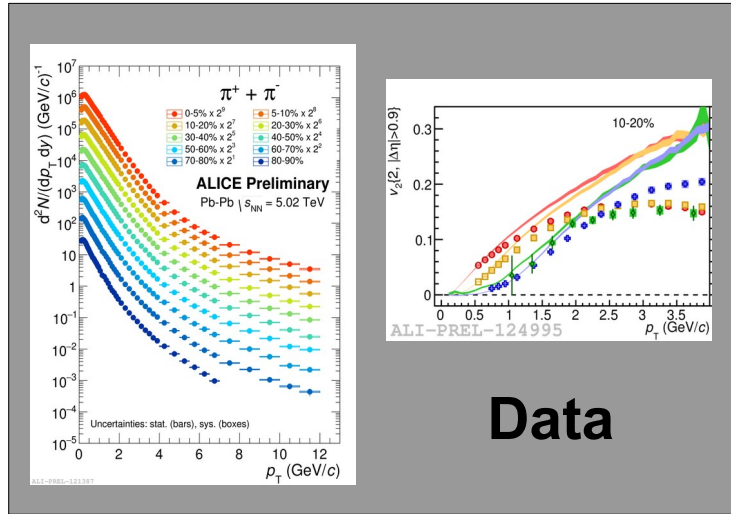


$\hat{q} = 1.2 \pm 0.3 \text{ GeV}^2$ 200 GeV Au+Au
 $\hat{q} = 1.9 \pm 0.7 \text{ GeV}^2$ 2.76 TeV Pb+Pb

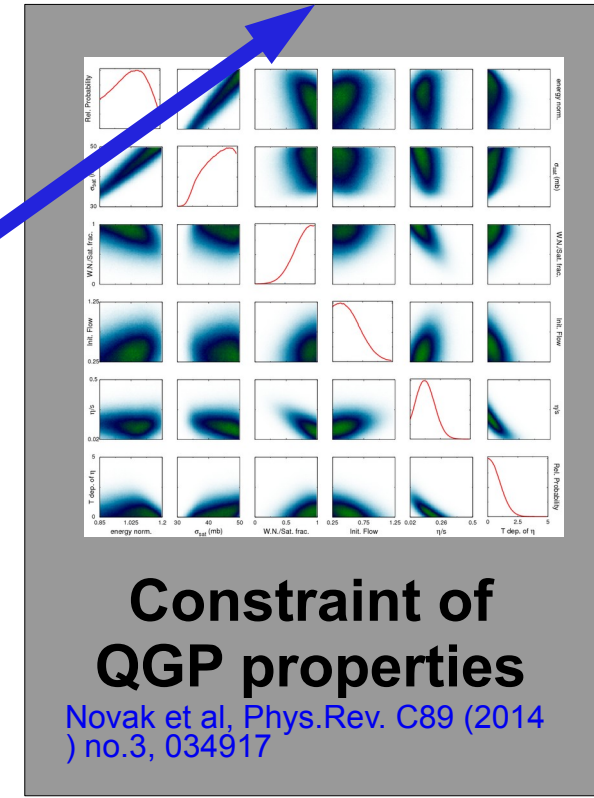
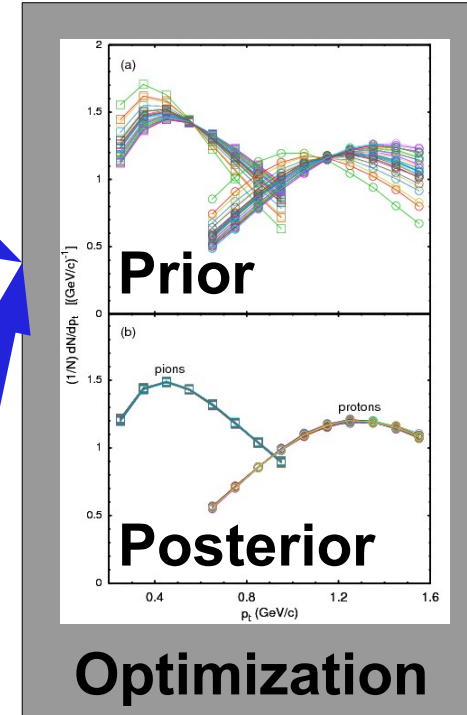
Bayesian Statistical Analysis

Models and Data Analysis Initiative

<http://madai.us>

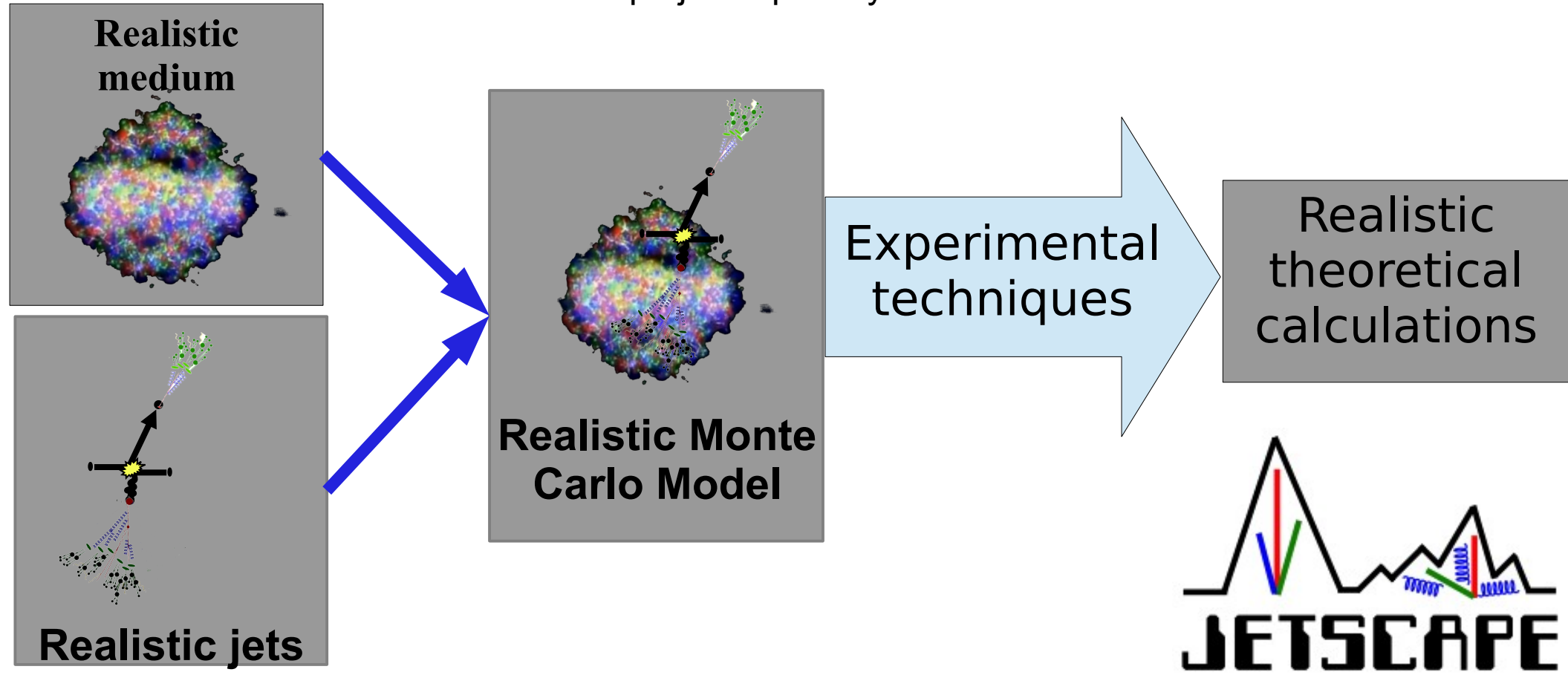


- Model emulation**
- 1) Run full model ~1000 times
 - 2) MCMC parameter search uses emulator (interpolator) in lieu of full model

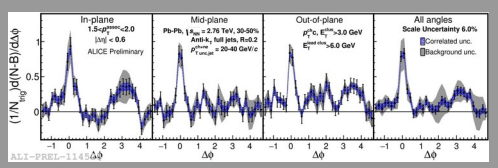
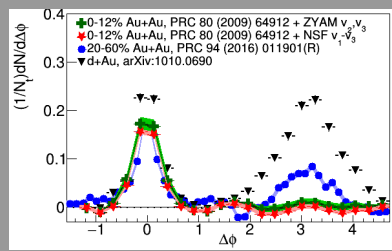
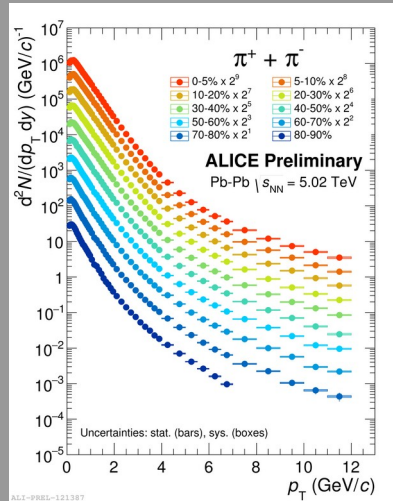
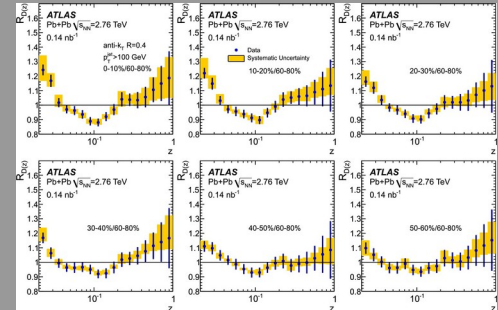
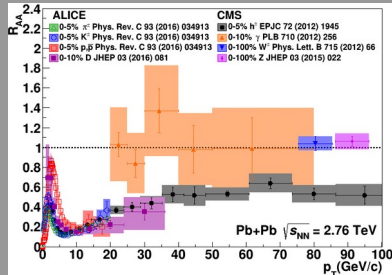


JETSCAPE Event generator

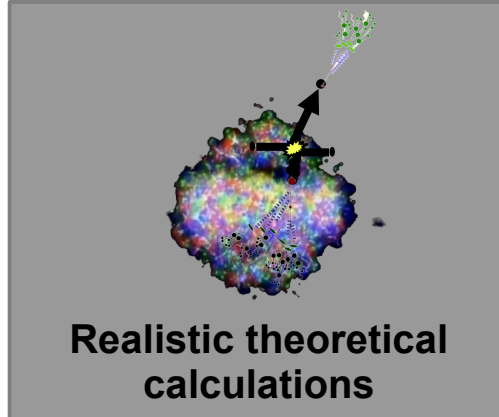
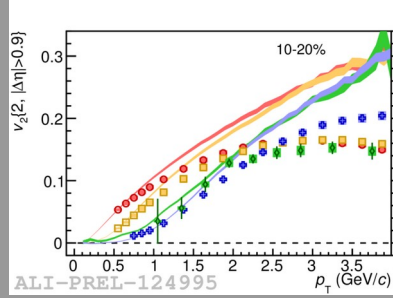
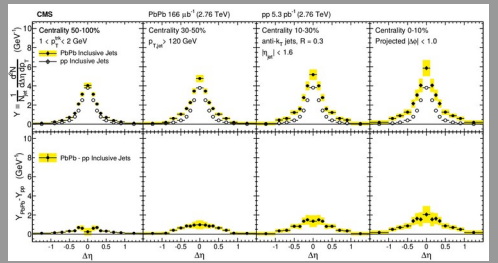
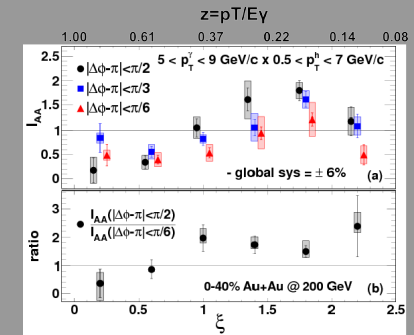
Jet Energy-loss Tomography with a **S**tatistically and **C**omputationally **A**dvanced **P**rogram **E**nvelope
<http://jetscape.wayne.edu/>



Event Generator + Bayesian Statistical analysis



Data



Conclusions

Conclusions

- Jets are complicated and hard to measure to high precision
- Much of the physics we want does not require them
- Extra insight from studying them anyways
- Be skeptical, especially of background subtraction
- Make sure the measurement is comparable to model

The End

Backup

Exploring the Lund Plane: in medium

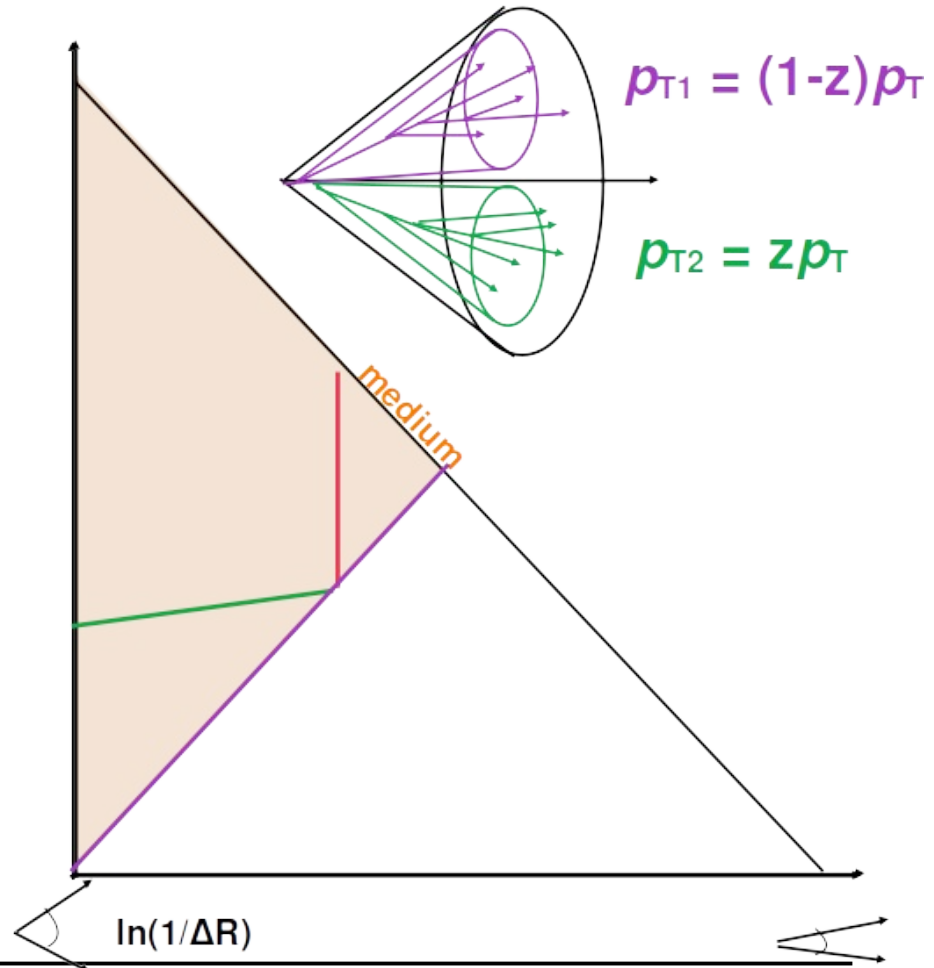
- Jet splittings in heavy-ion (HI) collisions

→ Splittings happen at different times

- ▶ Earlier/wider splittings experience more medium

→ Vacuum splittings vs. non-perturbative in-medium splittings

→ Coherence vs. decoherence



Exploring the Lund Plane: in medium

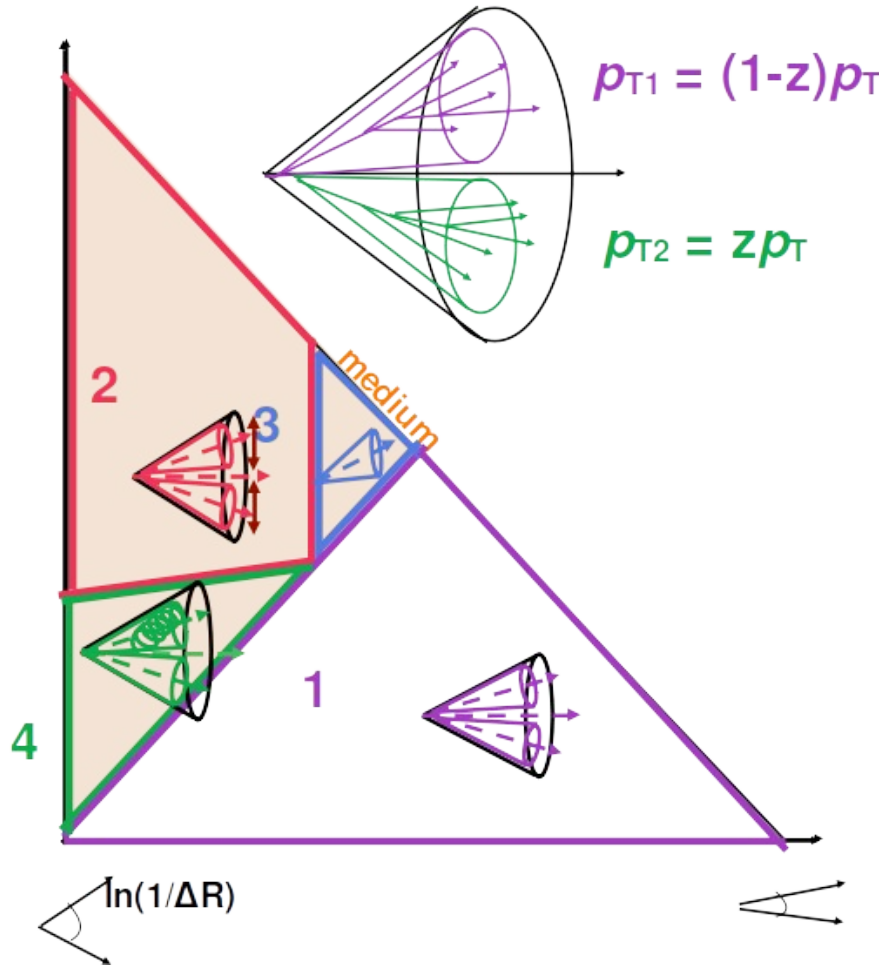
- Jet splittings in heavy-ion (HI) collisions

1: Vacuum splitting outside of medium

2: Vacuum splitting in-medium, resolved (decoherence)

3: Vacuum splittings in-medium, unresolved (coherence)

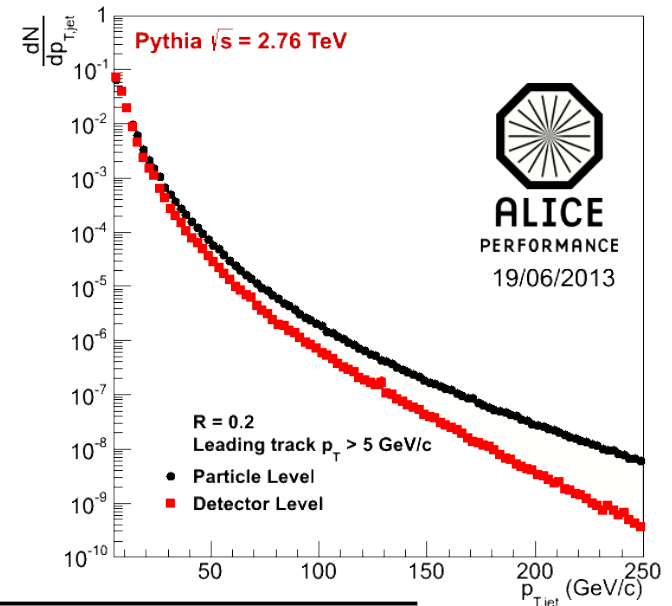
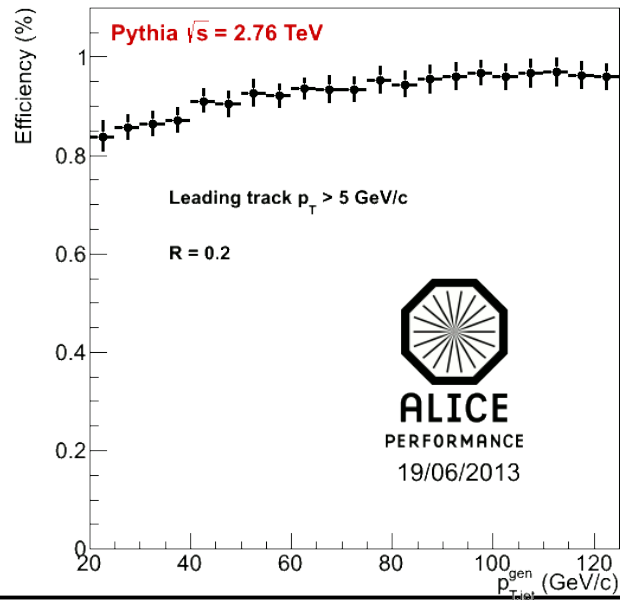
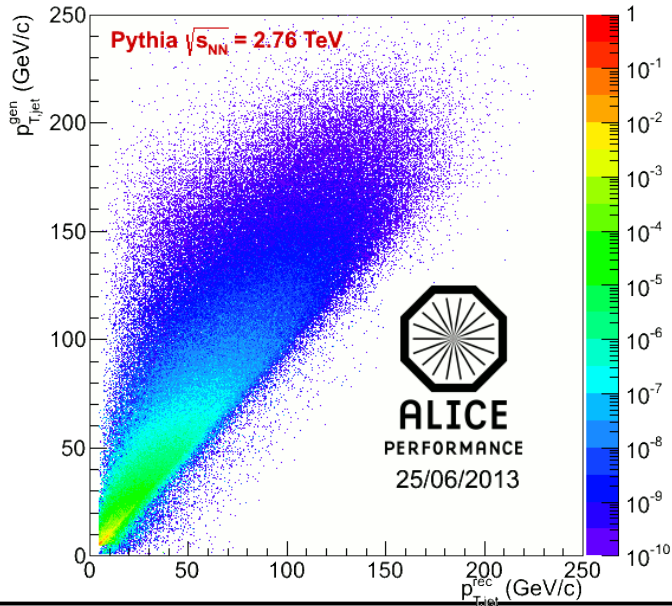
4: Medium-induced splittings



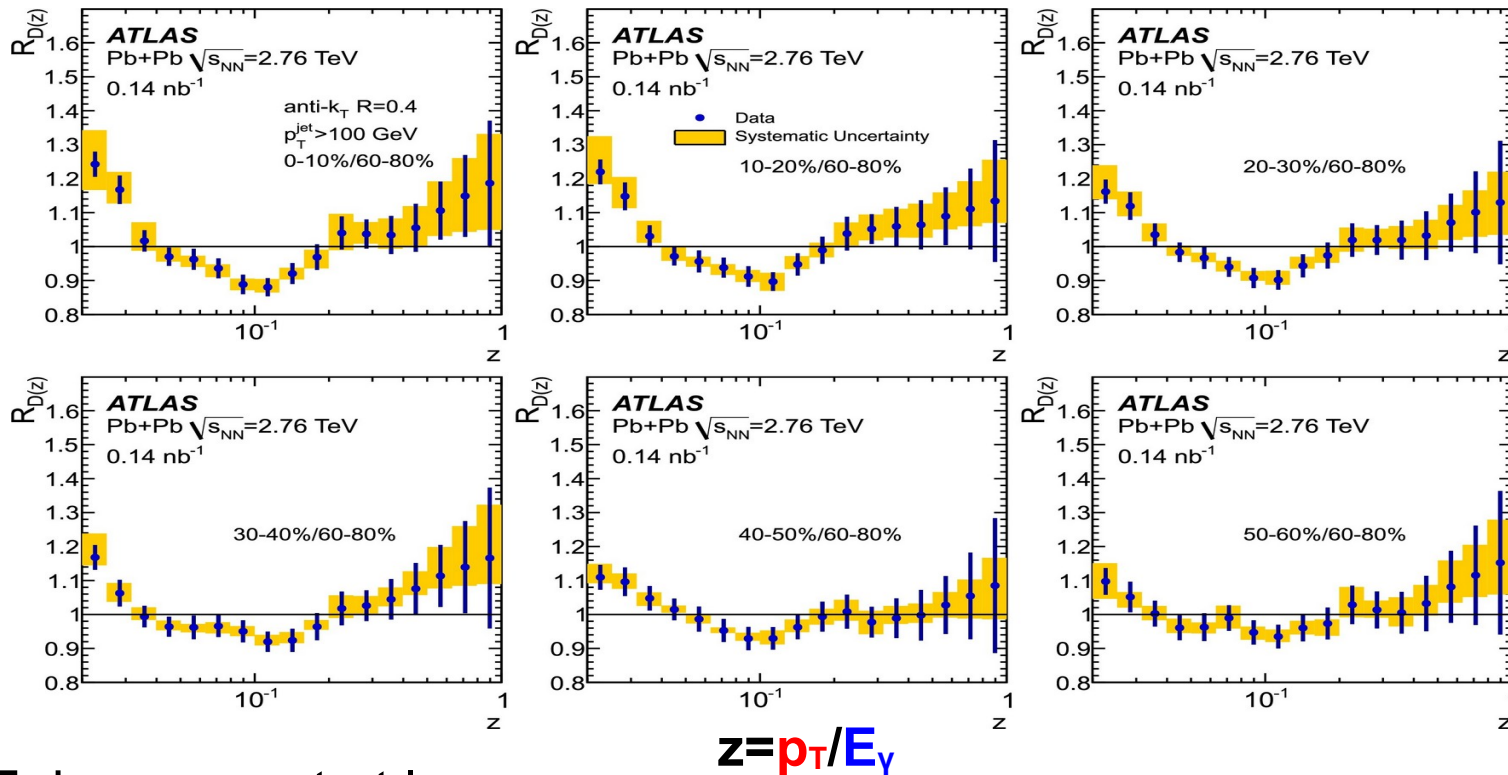
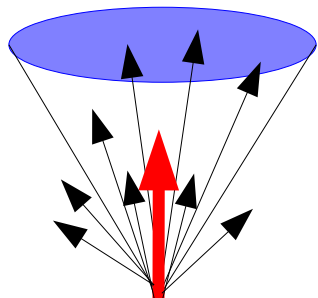
Jets in ALICE: Response matrix RM_{det}

RM_{det} quantifies detector response to jets

- “Particle” level jets – defined by jet finder on MC particles
- Pythia with Pb-Pb tracking efficiency
- “Detector” level jets – defined by jet finder after event reconstruction through GEANT
- Particle level jets are geometrically matched to detector level jets
- Matrix has a dependence on spectral shape and fragmentation
- Jet-finding efficiency is probability of a matched particle level jet



Modified fragmentation

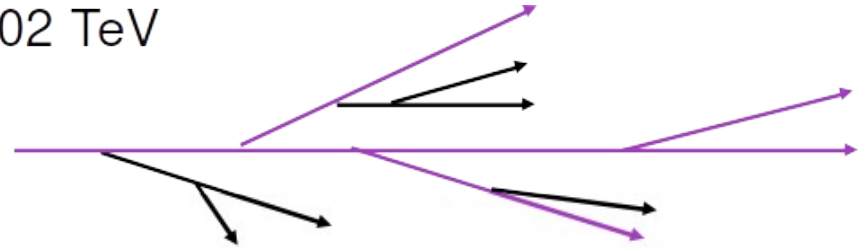


- Enhancement at low z
- No modification/enhancement at high z ?

n_{SD} : iterative declustering

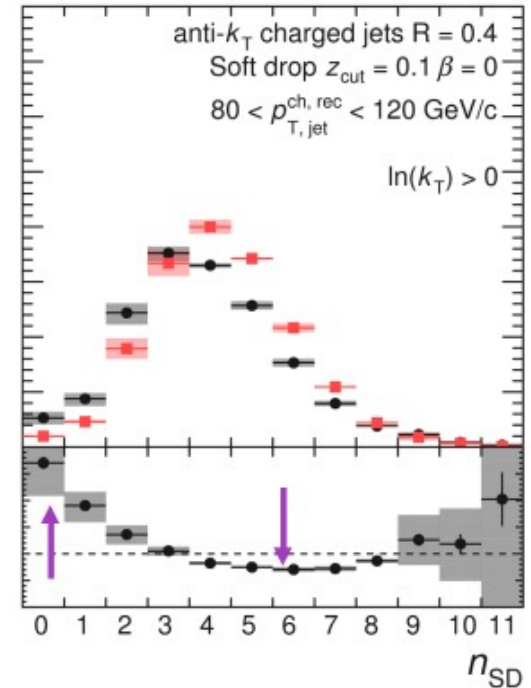
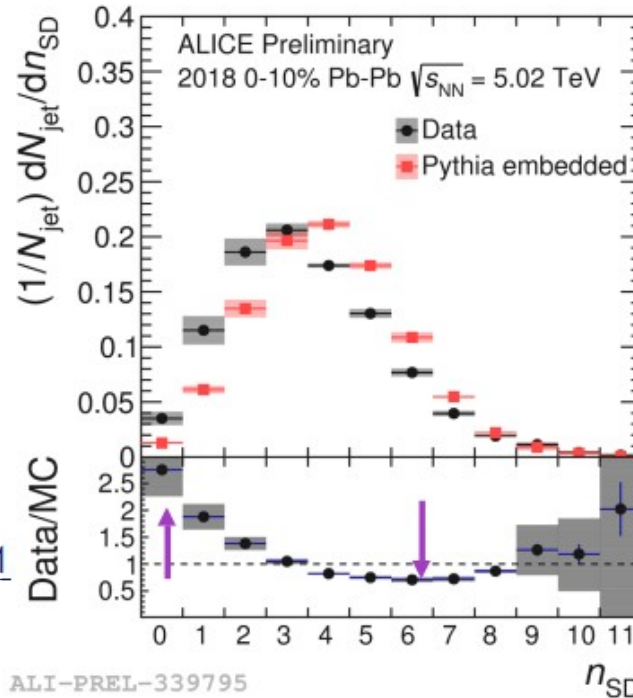
New ALICE measurement at 5.02 TeV

Modification: enhancement at small n_{SD} and suppression at intermediate n_{SD}

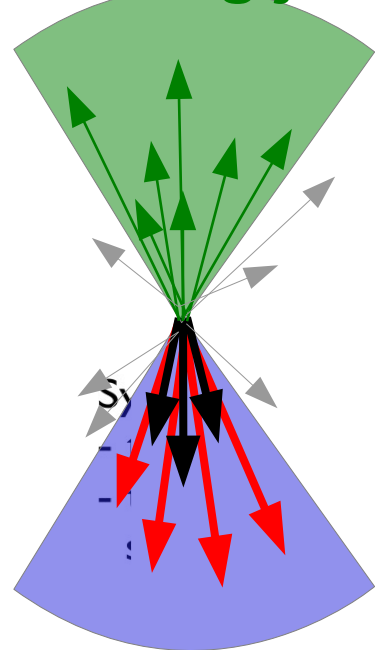


Consistent with wider/earlier being suppressed in the medium, leading to more jets with lower n_{SD}^*

[*arXiv:1907.11248v1](https://arxiv.org/abs/1907.11248v1)



Leading jet

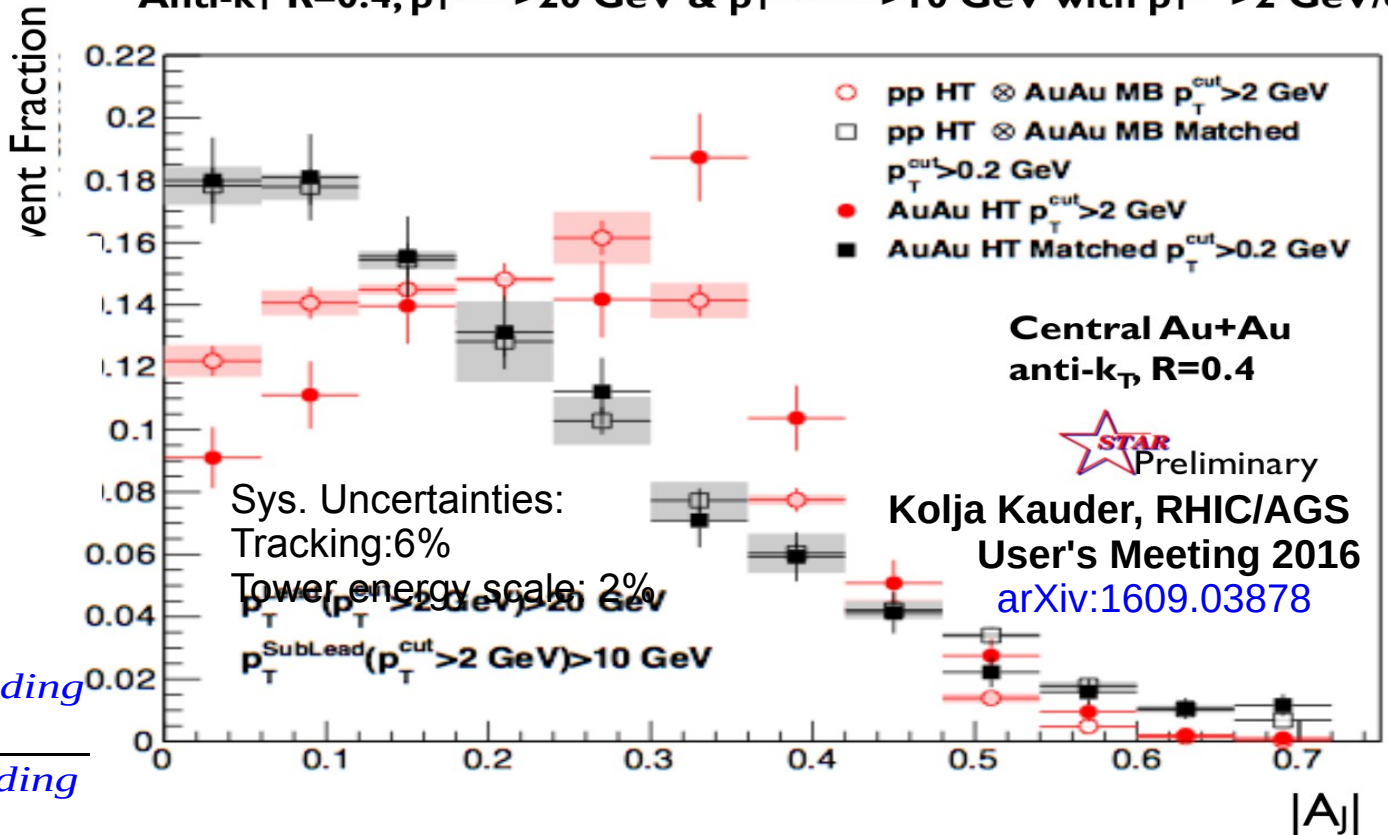


Subleading jet

$$A_j = \frac{p_T^{\text{leading}} - p_T^{\text{subleading}}}{p_T^{\text{leading}} + p_T^{\text{subleading}}}$$

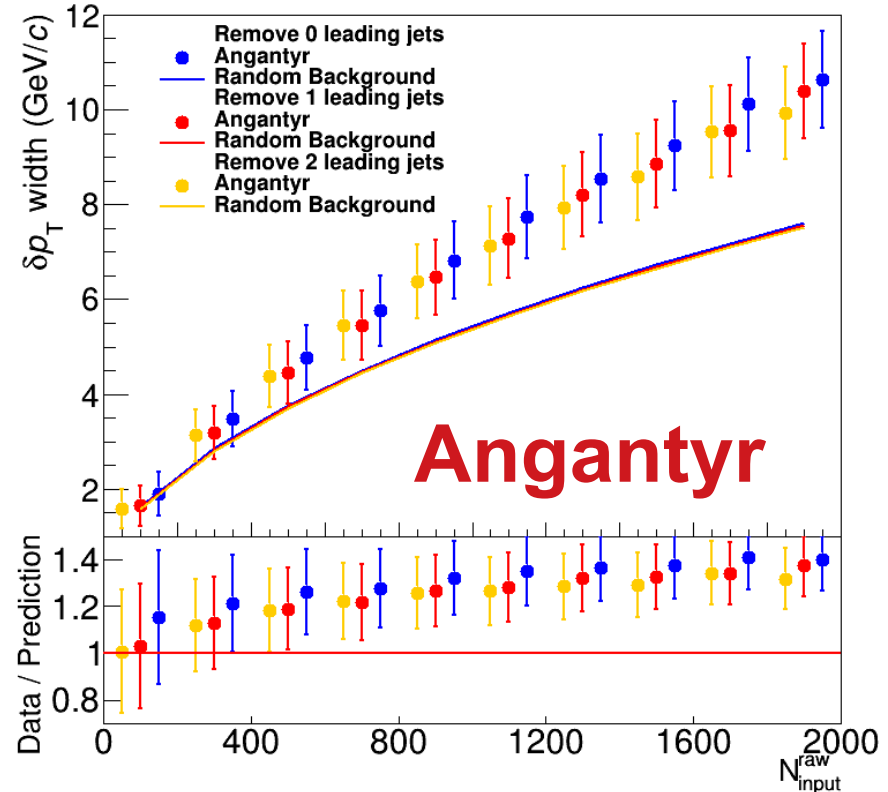
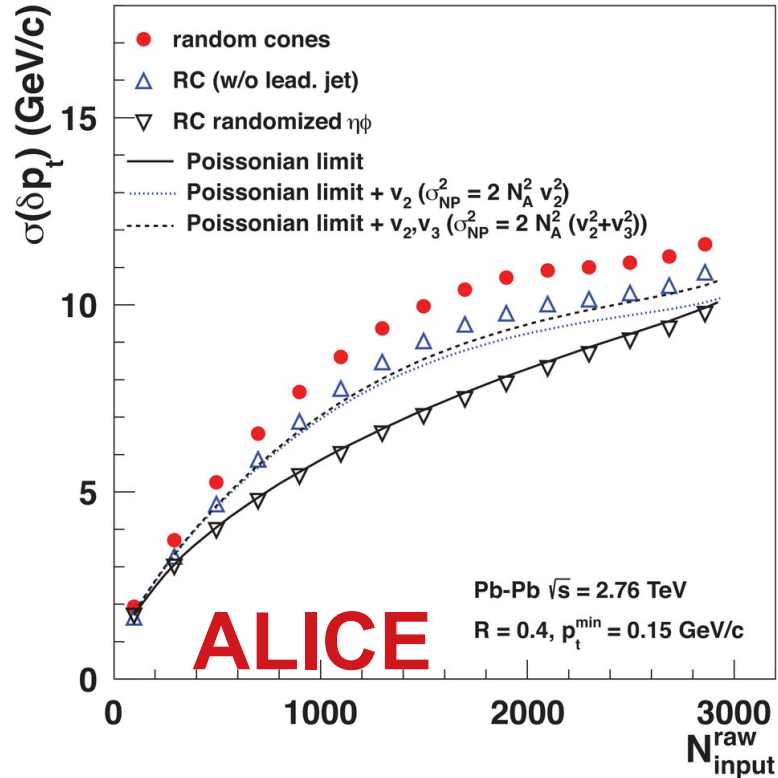
Di-jet asymmetry

Anti-k_T R=0.4, p_T^{Lead}>20 GeV & p_T^{SubLead}>10 GeV with p_T^{cut}>2 GeV/c



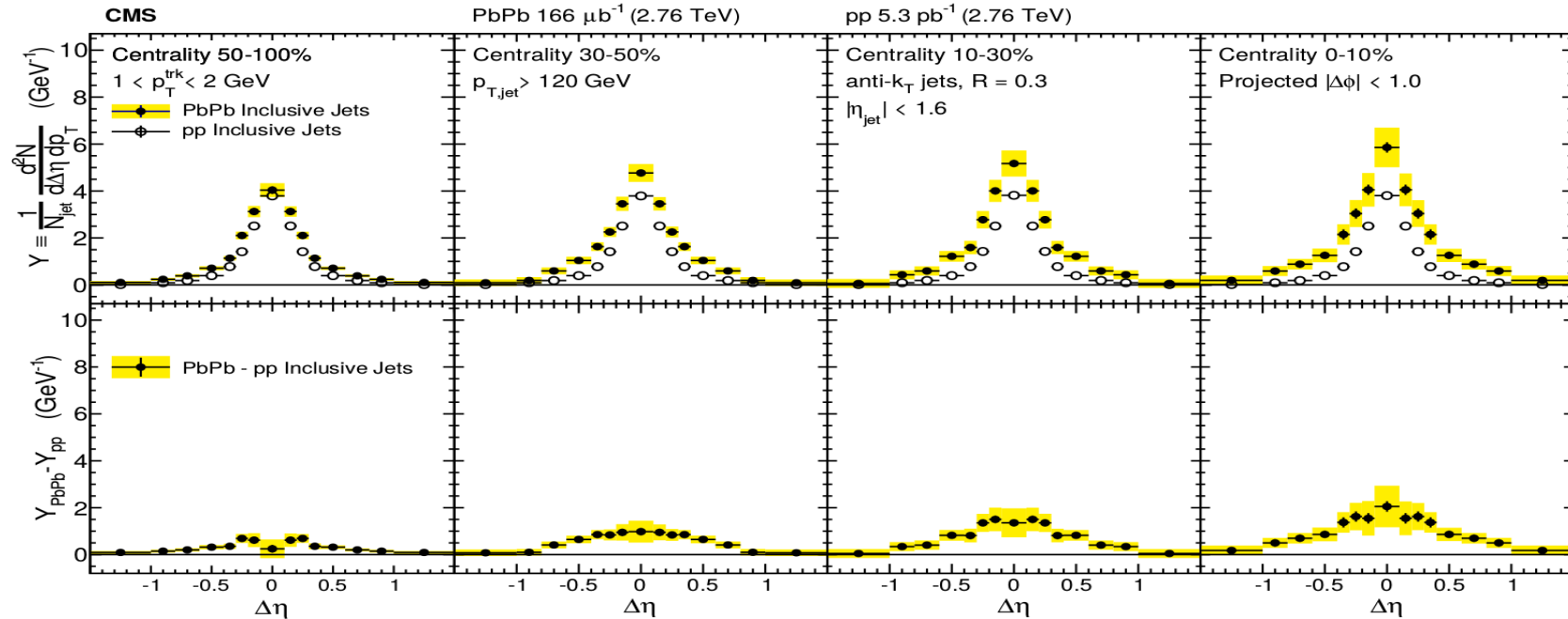
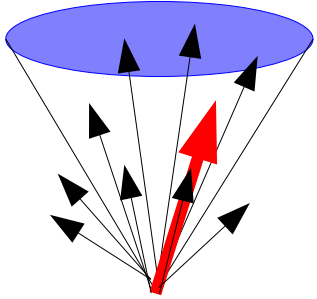
Au+Au di-jets more imbalanced than p+p for p_T^{cut}>2 GeV/c

Width vs multiplicity



Discrepancy not from an excess of jets!

Jet-hadron correlations



- Jets are broader, constituents are softer
- Also seen in:
 - Di-hadron correlations [Lots of papers]
 - Jet shapes [arXiv:1708.09429, arXiv:1512.07882, arXiv:1704.03046]
 - Dijet asymmetry with soft constituents [PRL119 (2017) 62301]