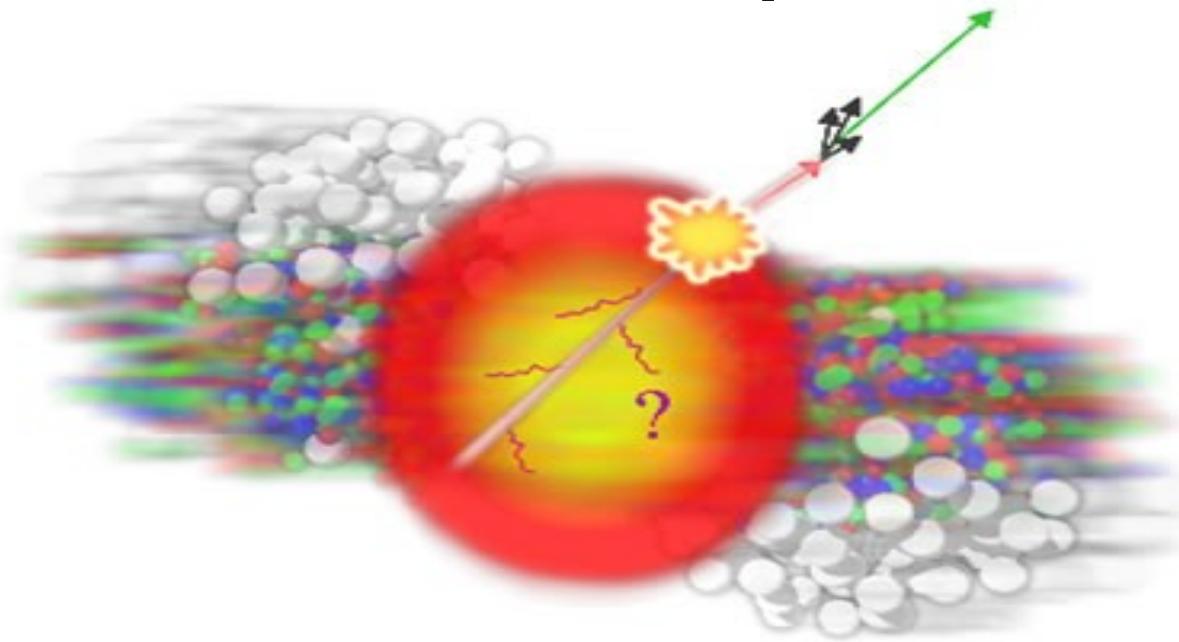


# A skeptic's guide to jets

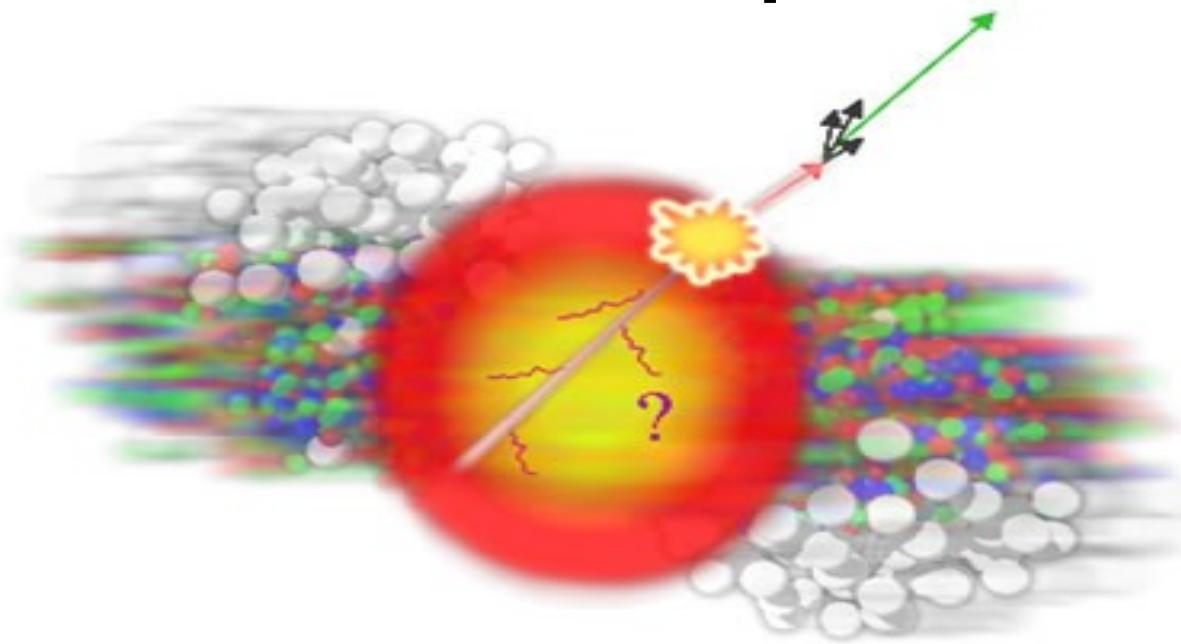
## Part 1: Jet spectra



Christine Nattrass  
University of Tennessee, Knoxville

# A skeptic's guide to jets

## Part 1: Jet spectra



Christine Nattrass  
University of Tennessee, Knoxville

# Acknowledgements

The following people contributed ideas and/or slides, but of course I take full responsibility for anything you don't like:

Rosi Reed, Megan Connors, Sevil Salur

Abhijit Majumder, Raghav Kunawalkam Elayavalli

Marta Verweij, Laura Havener

Austin Schmier, Charles Hughes, Will Witt

# Questions an experimentalist should ask

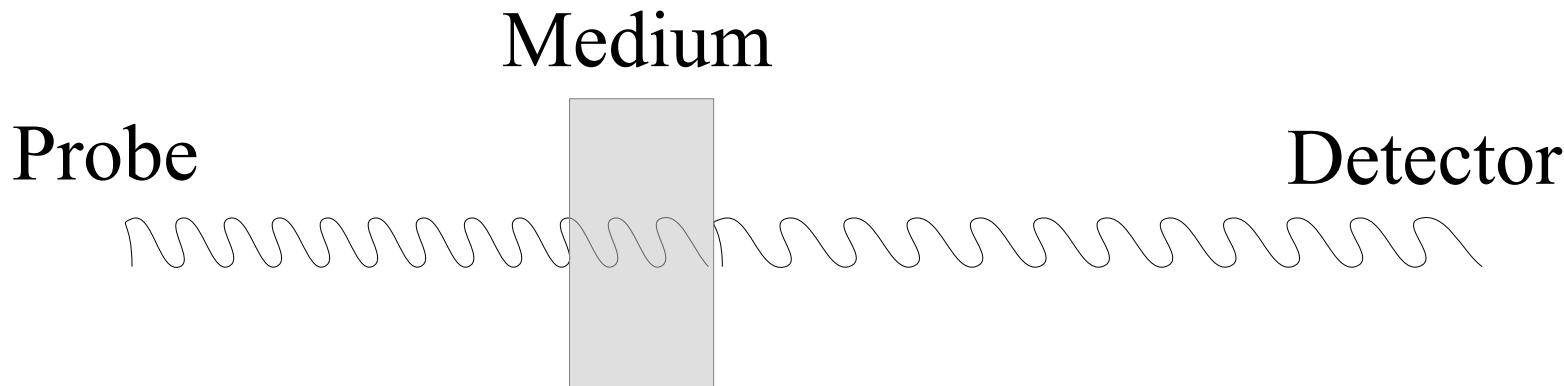
- What do I want to learn?
- What am I measuring?
- What assumptions am I making?
- What are the dominant uncertainties?
- How do I compare to models?

**The answers for jets are highly non-trivial!**

# What do I want to learn? The cartoon picture



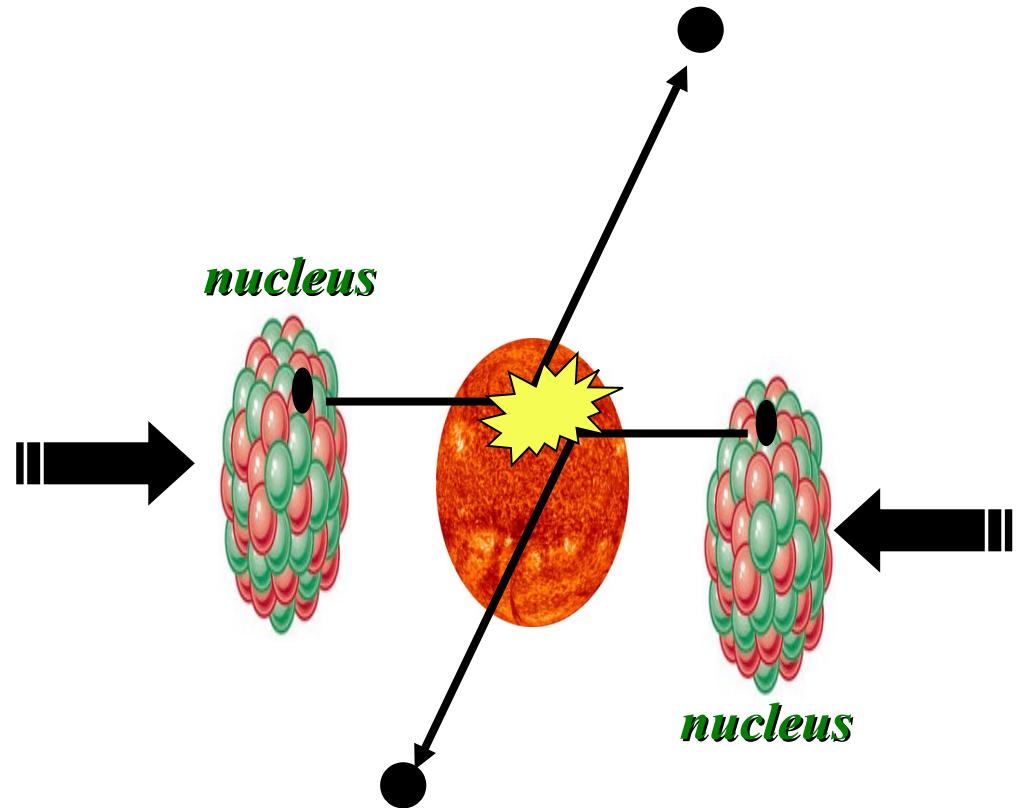
# Probing the Quark Gluon Plasma



Want a probe which traveled through the collision  
QGP is very short-lived ( $\sim 1\text{-}10 \text{ fm/c}$ ) →  
cannot use an external probe

# Probes of the Quark Gluon Plasma

Want a probe which traveled through the medium  
QGP is short lived → need a probe created in the collision

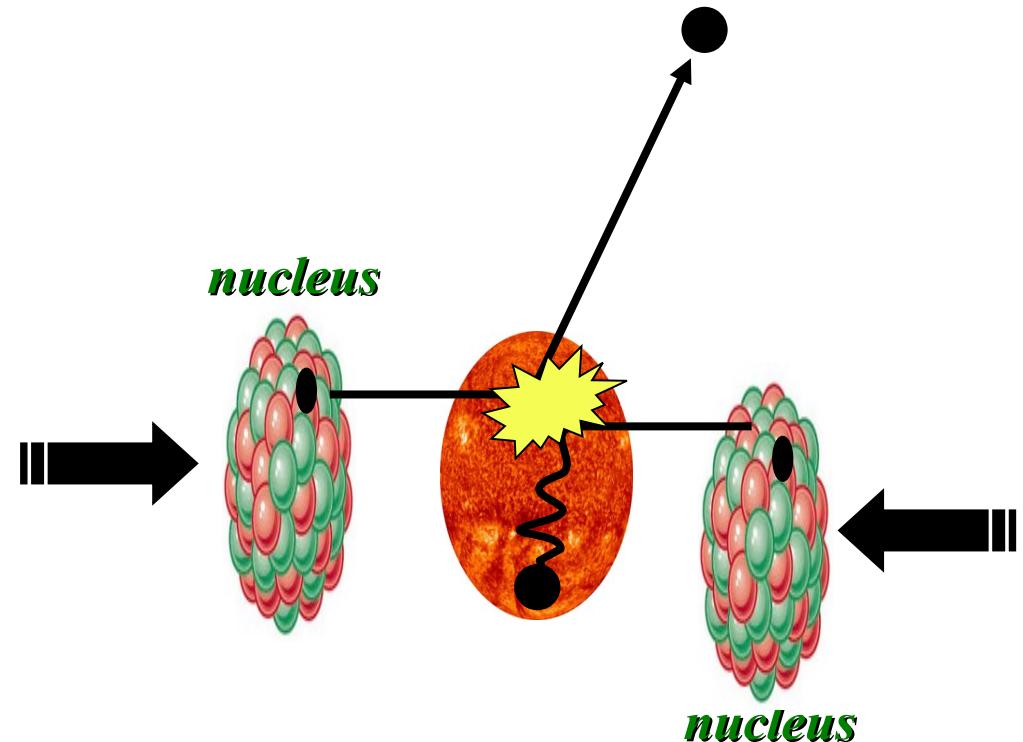


# Probes of the Quark Gluon Plasma

Want a probe which traveled through the medium

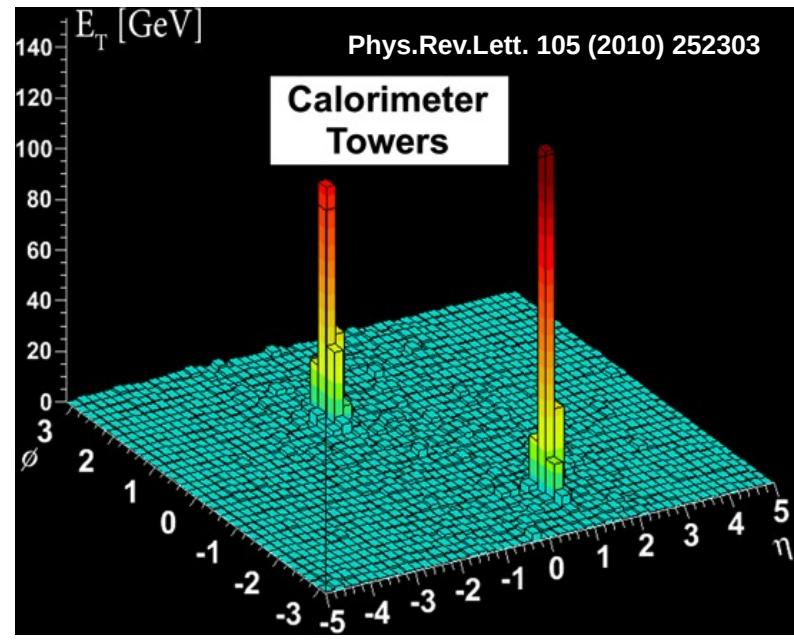
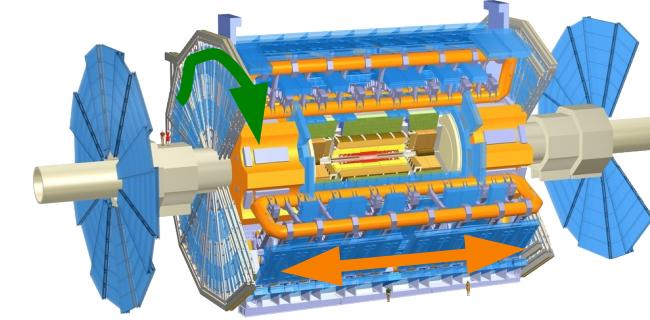
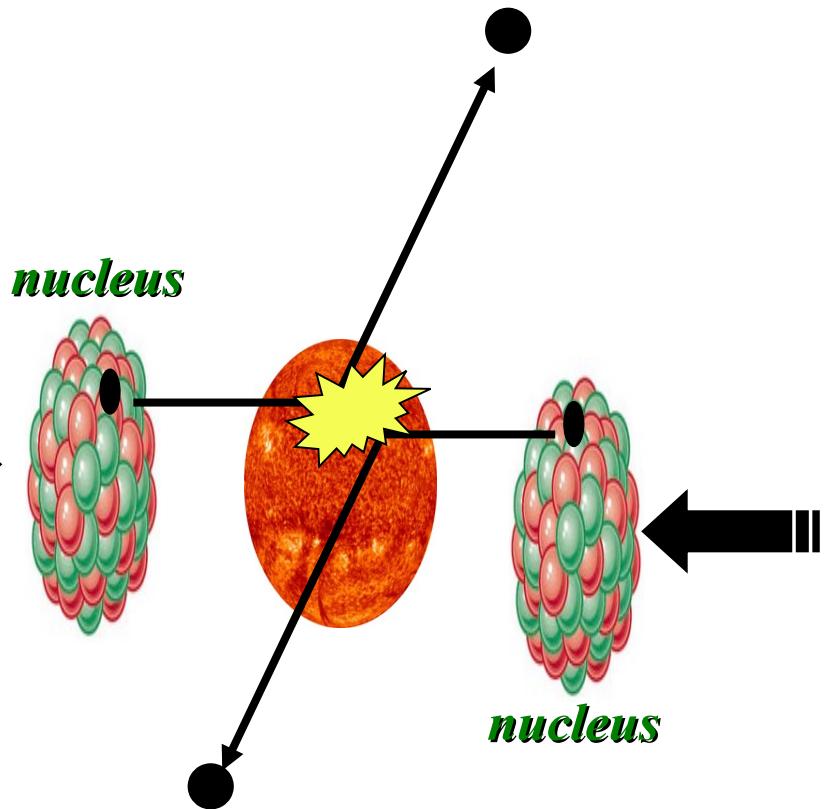
QGP is short lived → need a probe created in the collision

We expect the medium to be dense → absorb/modify probe



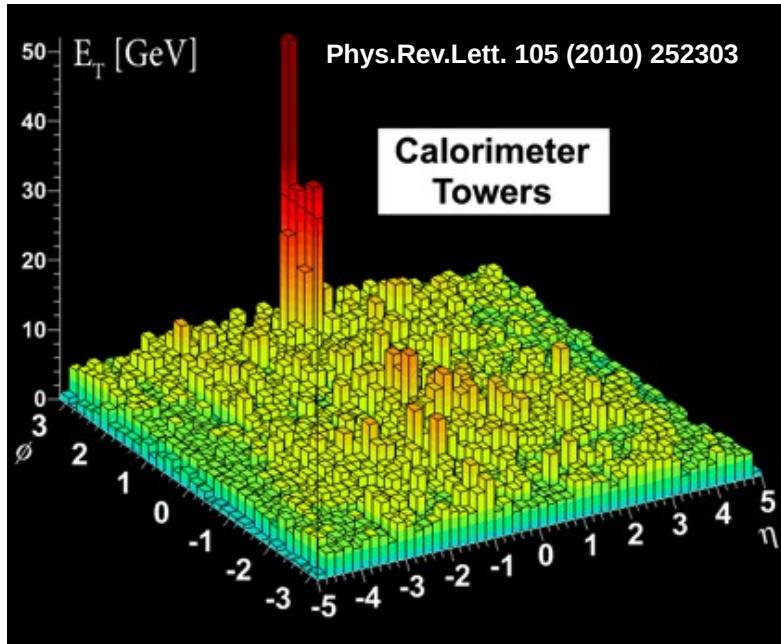
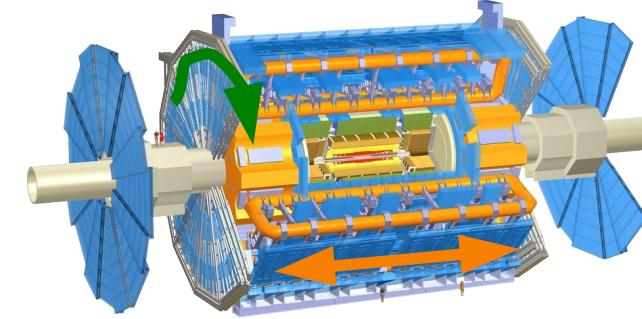
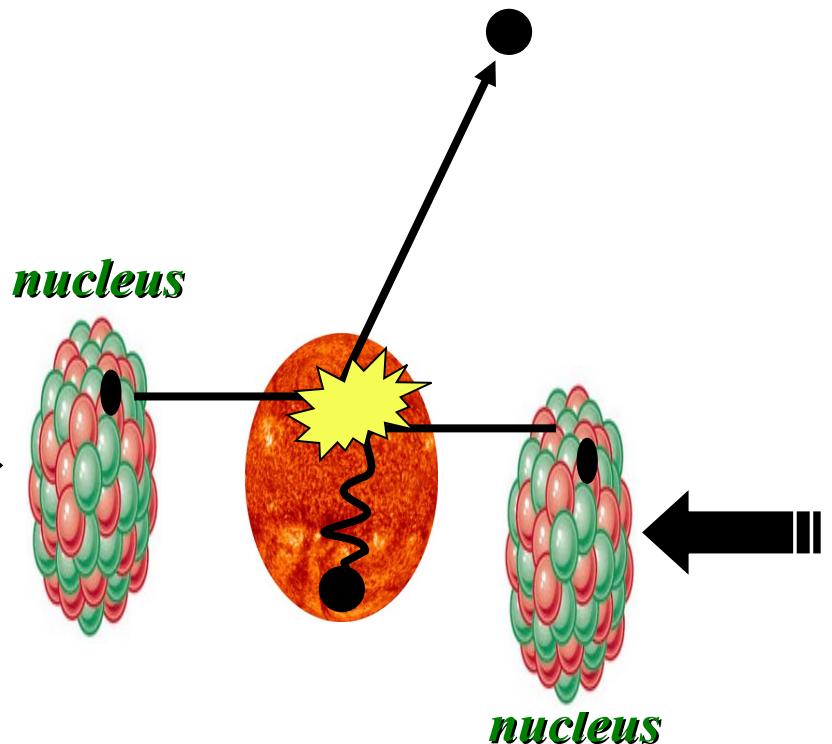
# Probes of the Quark Gluon Plasma

ATLAS



# Probes of the Quark Gluon Plasma

ATLAS

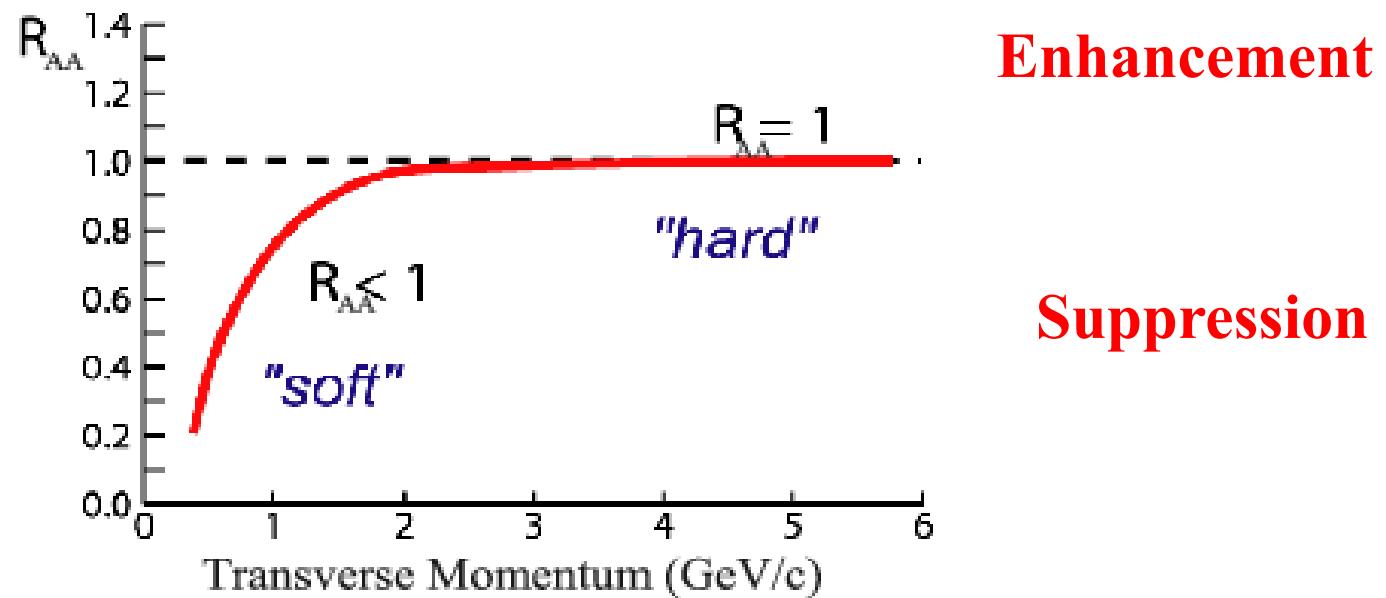


“Simple” example: Single hadrons

# Nuclear modification factor

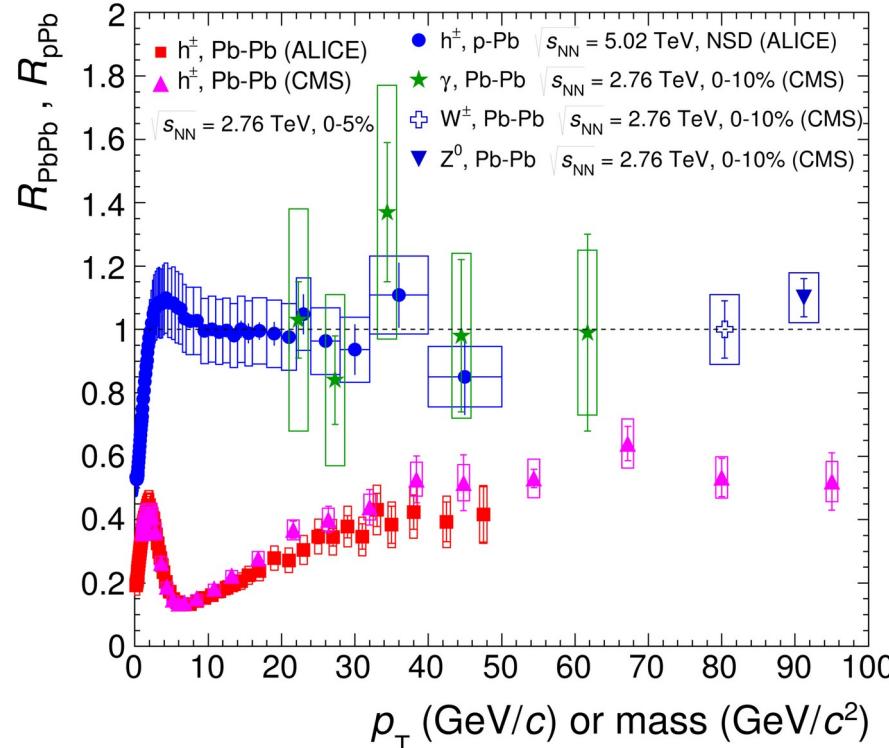
- Measure spectra of probe (jets) and compare to those in p+p collisions or peripheral A+A collisions
- If high- $p_T$  probes (jets) are suppressed, this is evidence of jet quenching

$$R_{AA} = \frac{d^2N_{AA}/dp_T d\eta}{T_{AA} d^2\sigma^{pp}/dp_T d\eta}$$



# Nuclear modification factor

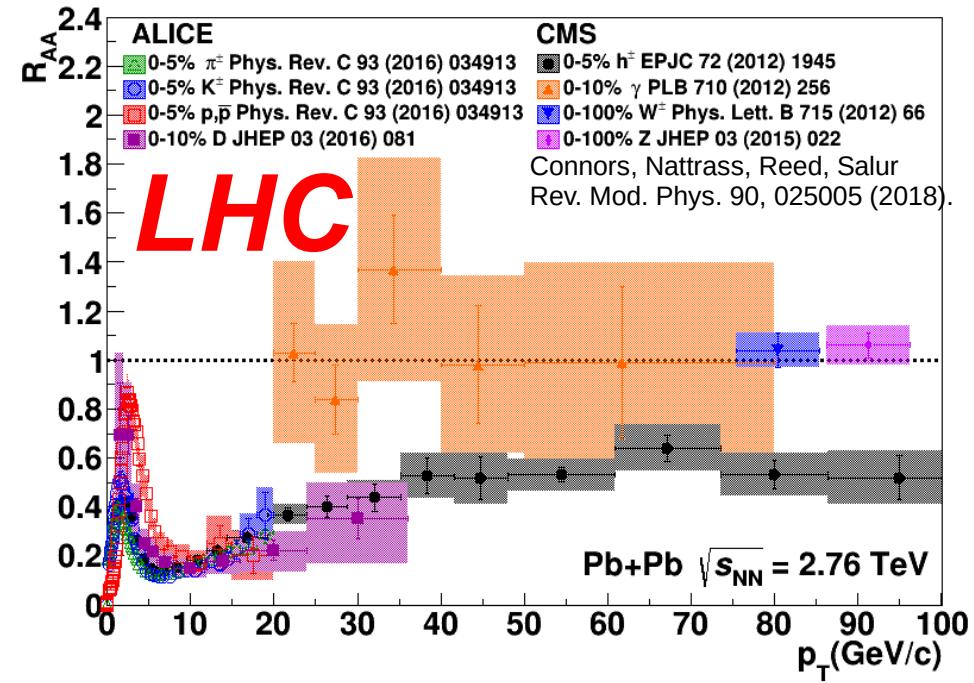
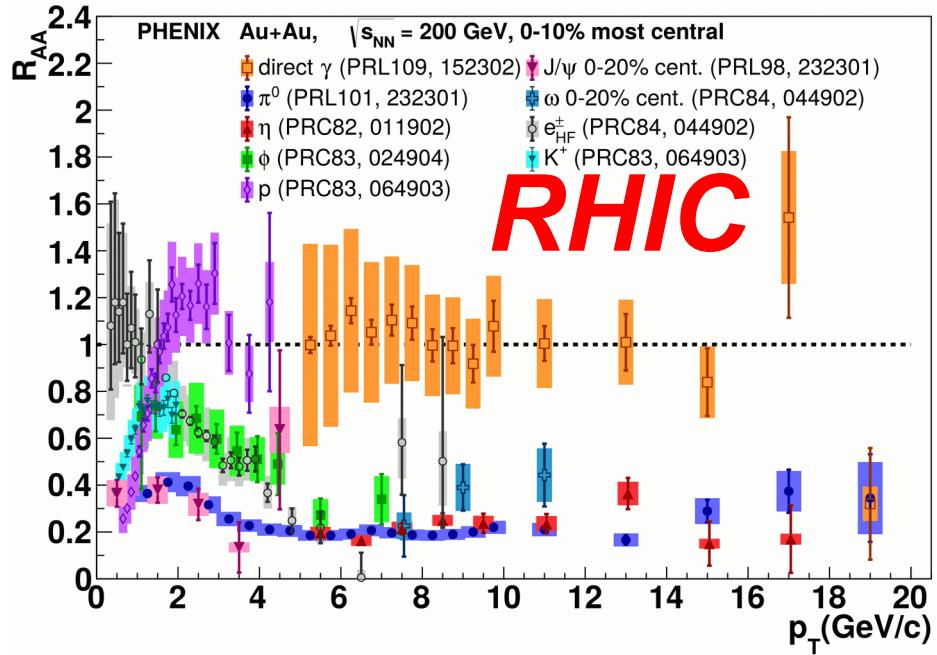
Control →  
Probe →



ALICE-DER-95222

- Charged hadrons (colored probes) suppressed in Pb—Pb
- Charged hadrons not suppressed in p—Pb at midrapidity
- Electroweak probes not suppressed in Pb—Pb

# Nuclear modification factor $R_{AA}$



*Electromagnetic probes – consistent with no modification – medium is transparent to them*

*Strong probes – significant suppression – medium is opaque to them  
- even heavy quarks!*

# What am I measuring? Definition of a jet

# Theoretical calculations

# Factorization theorem

- Assumption: Parton distribution functions, perturbative cross section, fragmentation function factorize
- What people really mean by “perturbatively calculable”
  - $D$  and  $f$  are explicitly non-perturbative!
  - $D$  is for parton  $c \rightarrow$  hadron  $h$   
Not what is experimentally measured
- Most theories for jet quenching modify fragmentation function  $D$

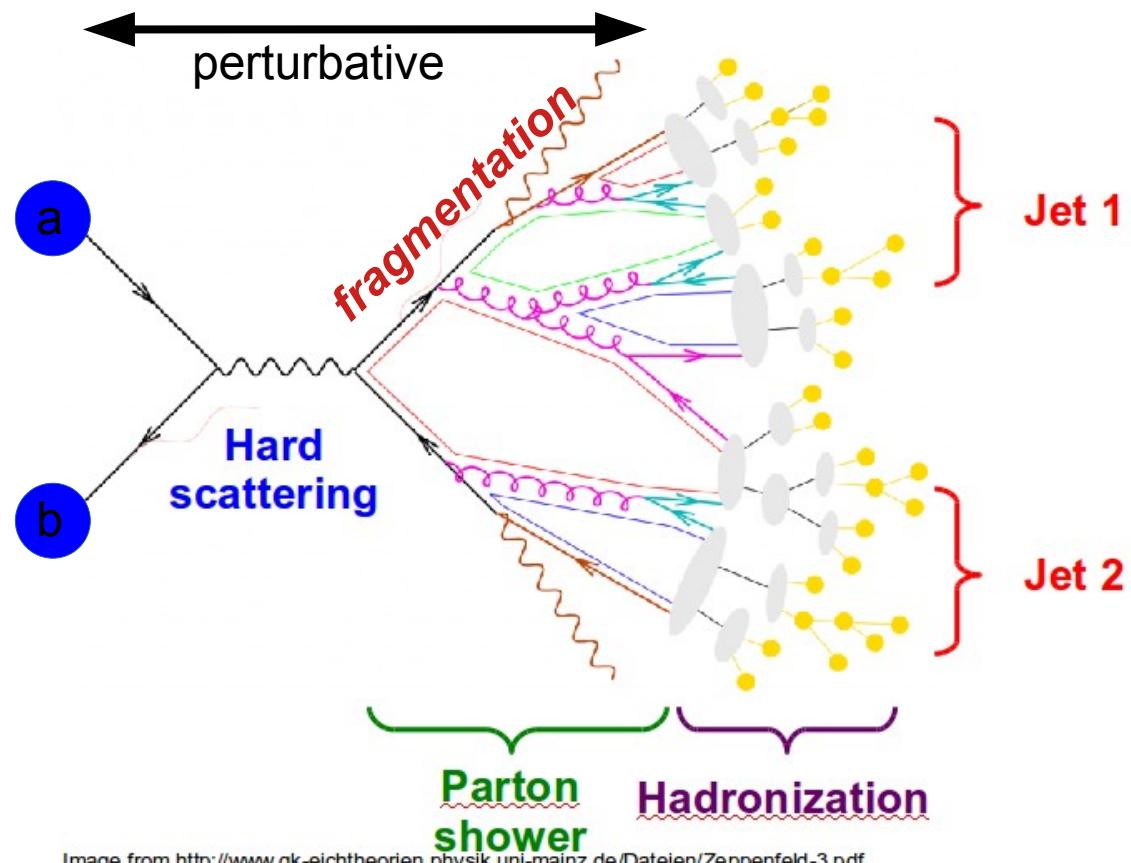


Image from <http://www.gk-eichtheorien.physik.uni-mainz.de/Dateien/Zeppenfeld-3.pdf>

$$\frac{d^3 \sigma^h}{dy d^2 p_T} = \frac{1}{\pi} \int d \mathbf{x}_a \int d x_b f_a^A(x_a) f_b^B(x_b) \frac{d \sigma_{ab \rightarrow cX}}{d \hat{t}} \frac{D_c^h(z)}{z}$$

# Jet finders

# What is a jet?

# What is a jet?

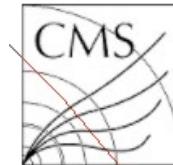
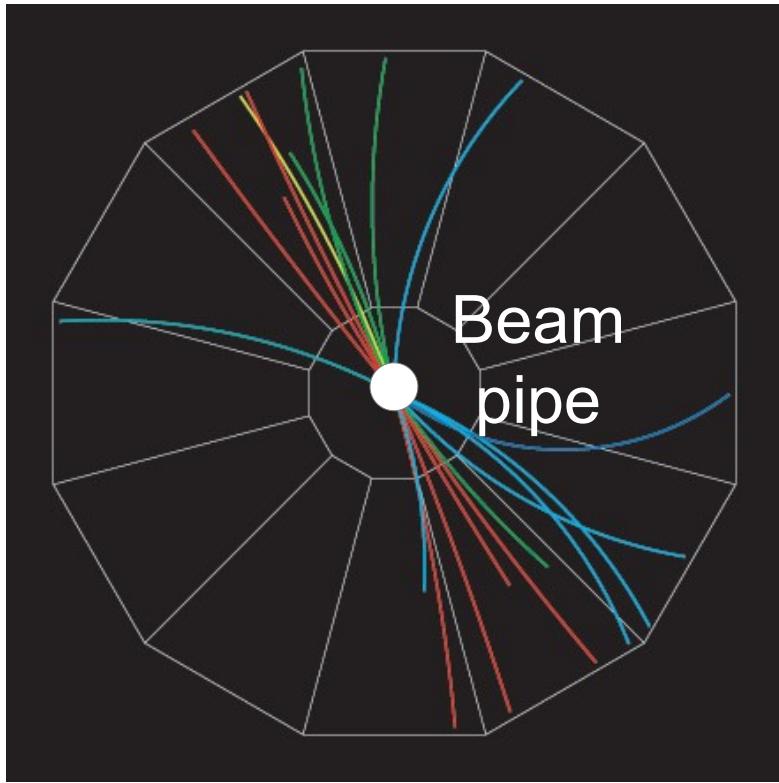
A measurement of a jet is a measurement of a parton.

# What is a jet?

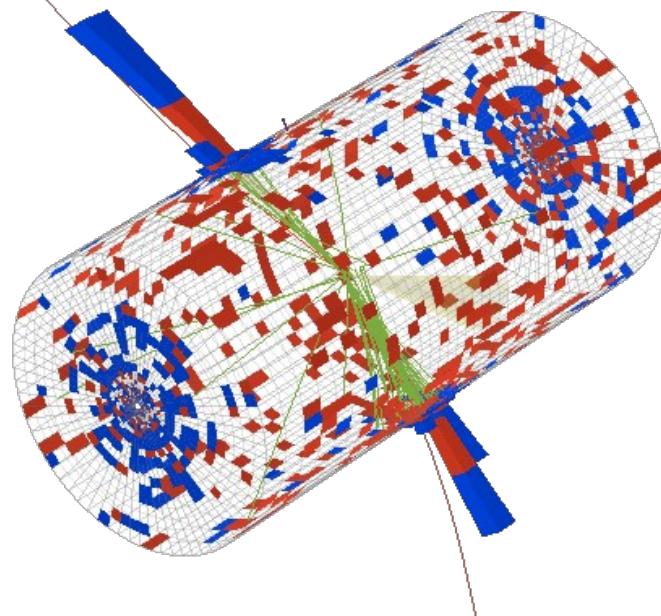
A measurement of a jet is a measurement of a parton.

# What is a jet?

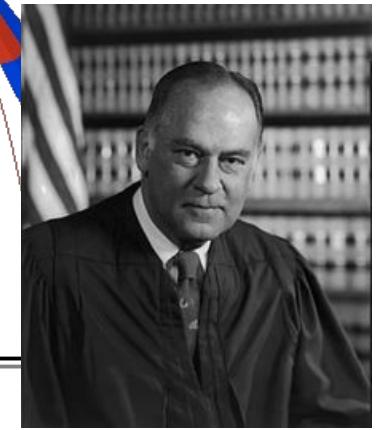
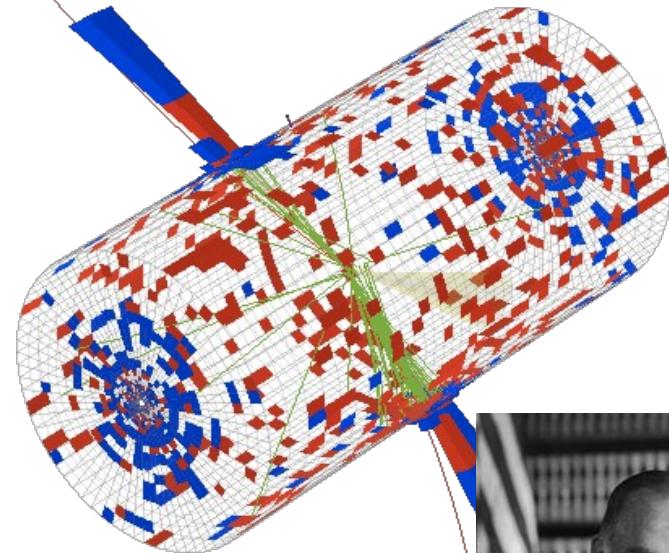
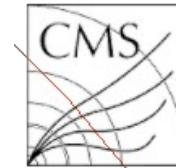
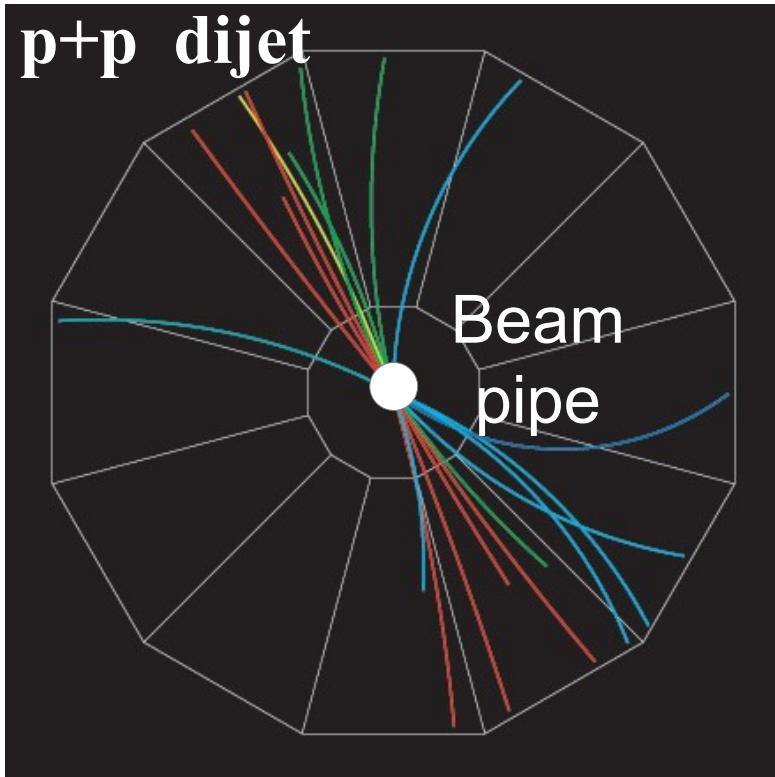
p+p dijet



CMS Experiment at LHC, CERN  
Data recorded: Fri Oct 5 12:29:33 2012 CEST  
Run/Event: 204541 / 52508234  
Lumi section: 32



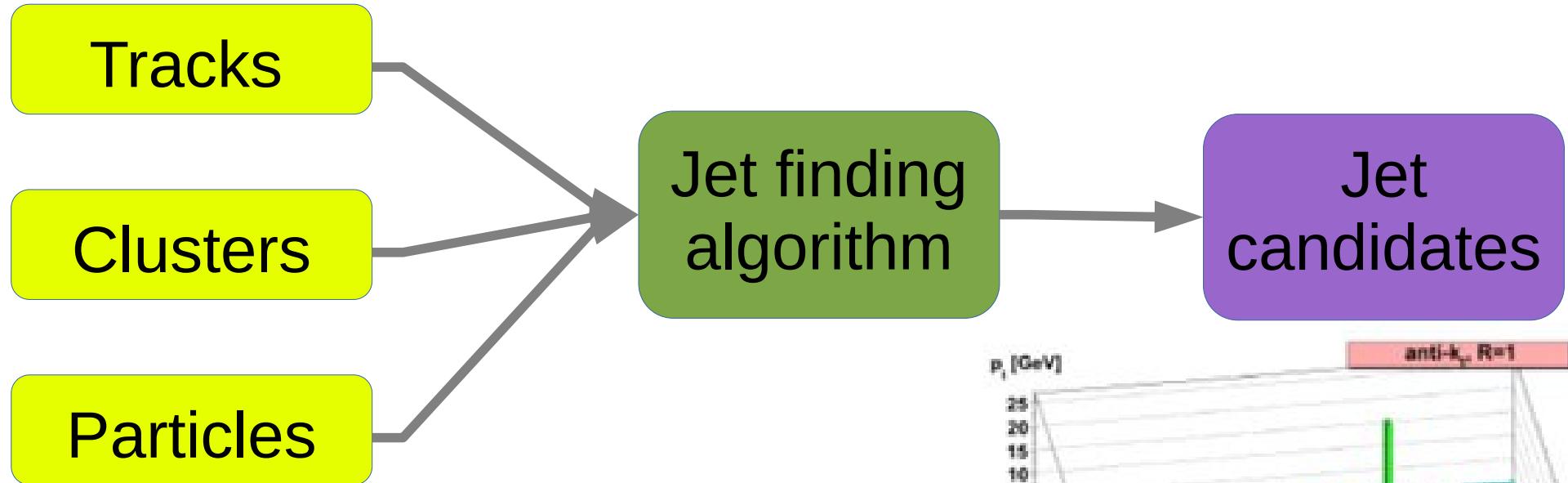
# What is a jet?



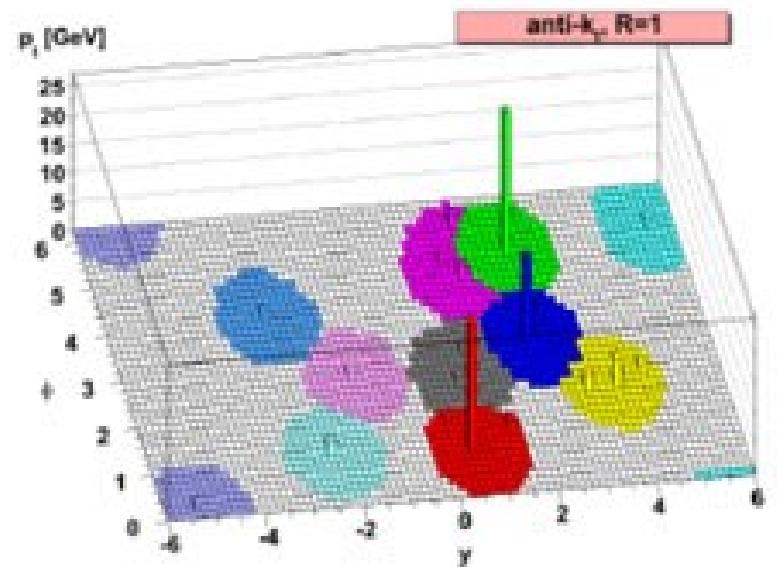
"I know it when I see it"

US Supreme Court Justice Potter Stewart, Jacobellis v. Ohio

# Jet finding algorithms



- Any list of objects works as input
- Use the same algorithm on theory & experiment
- Output only as good as input



# Jet finding *in pp collisions*

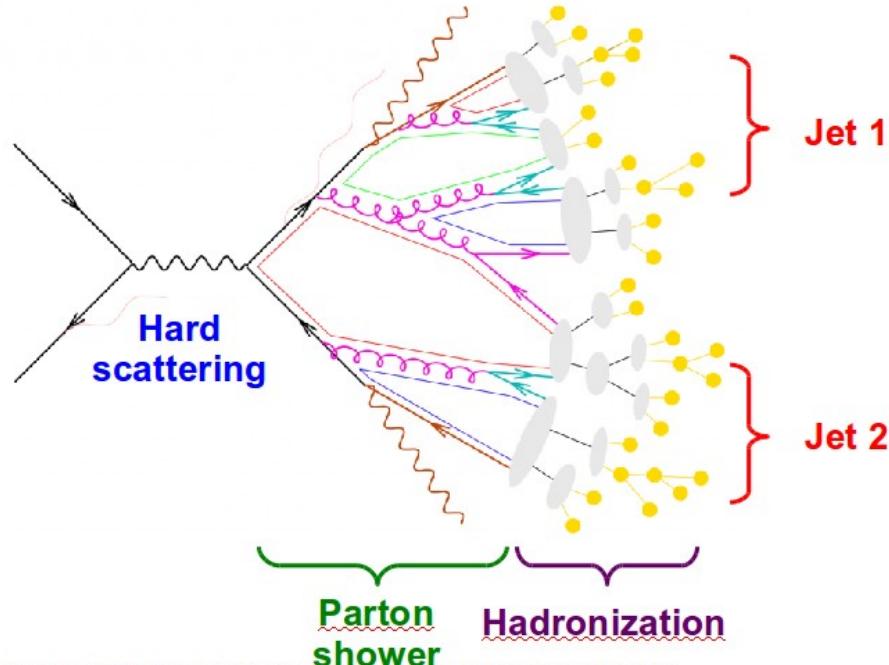


Image from <http://www.gk-eichtheorien.physik.uni-mainz.de/Dateien/Zeppenfeld-3.pdf>

- Jet finder: groups final state particles into jet candidates
  - Anti- $k_T$  algorithm  
JHEP 0804 (2008) 063 [arXiv:0802.1189]
- Depends on hadronization
- Ideally
  - Infrared safe
  - Colinear safe

**Snowmass Accord:** Theoretical calculations and experimental measurements should use the same jet finding algorithm. Otherwise they will not be comparable.

# Jets in principle

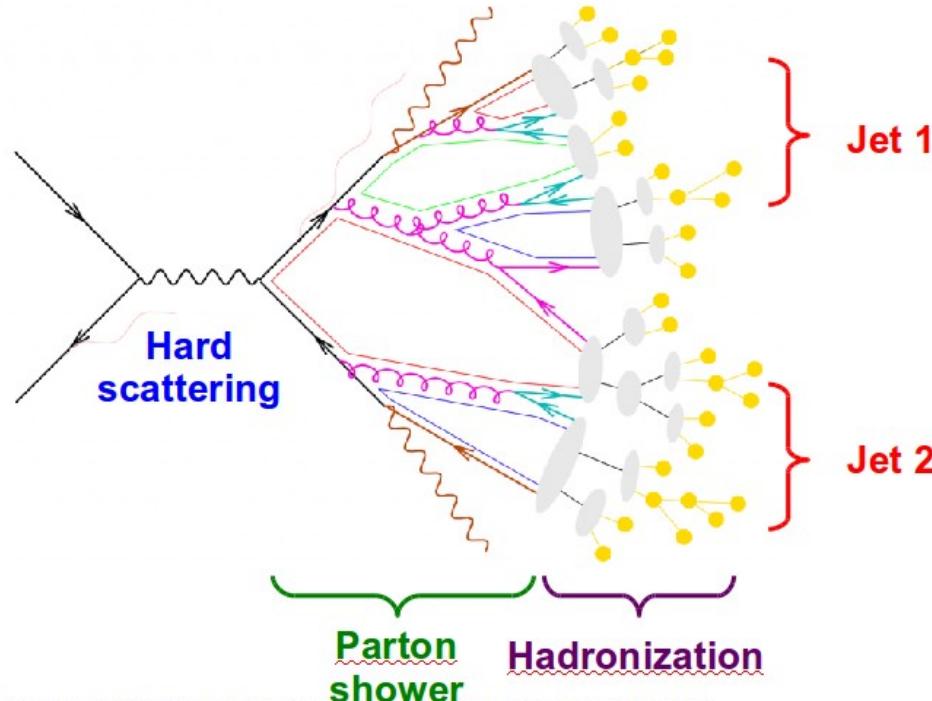
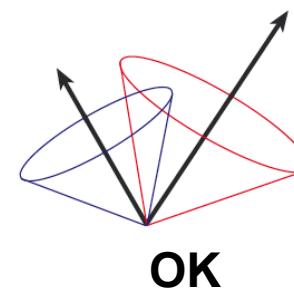
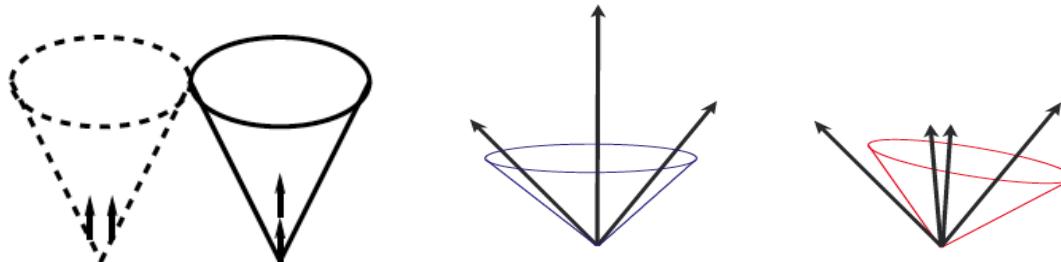
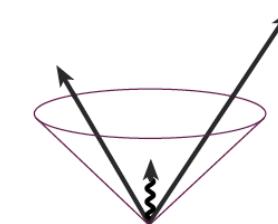


Image from <http://www.gk-eichtheorien.physik.uni-mainz.de/Dateien/Zeppenfeld-3.pdf>

- Jet measures **partons**
- Hadronic degrees of freedom are integrated out
- Algorithms are infrared and colinear safe

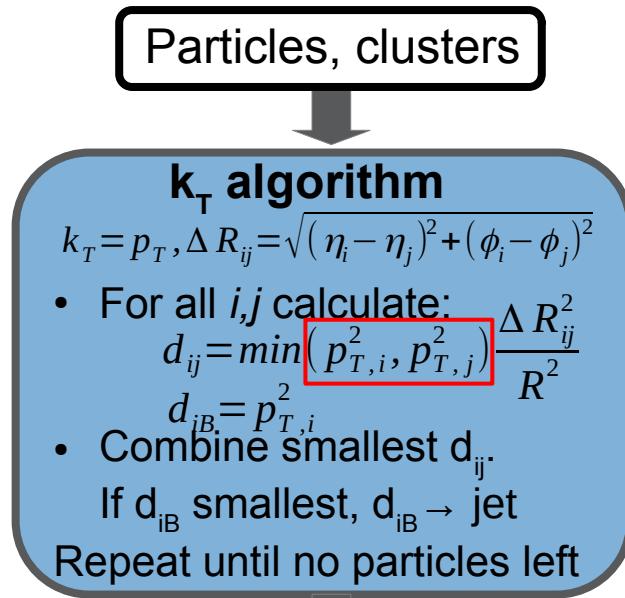


OK

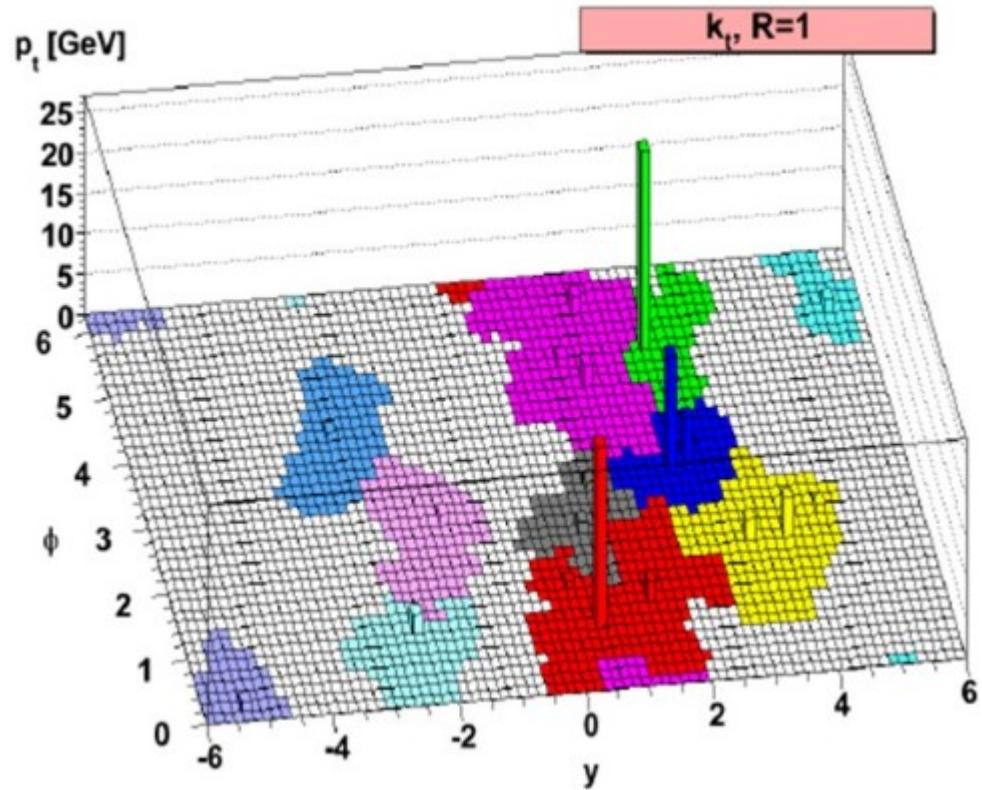


**BAD:** 2 jets  
are merged  
in one

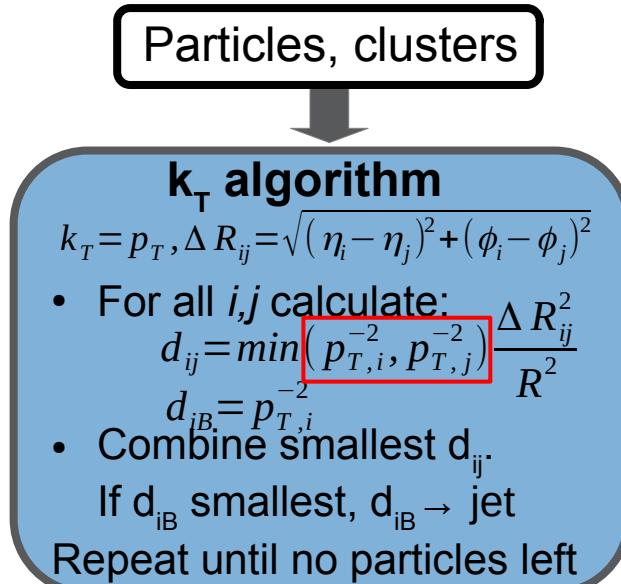
# $k_T$ jet finding algorithm



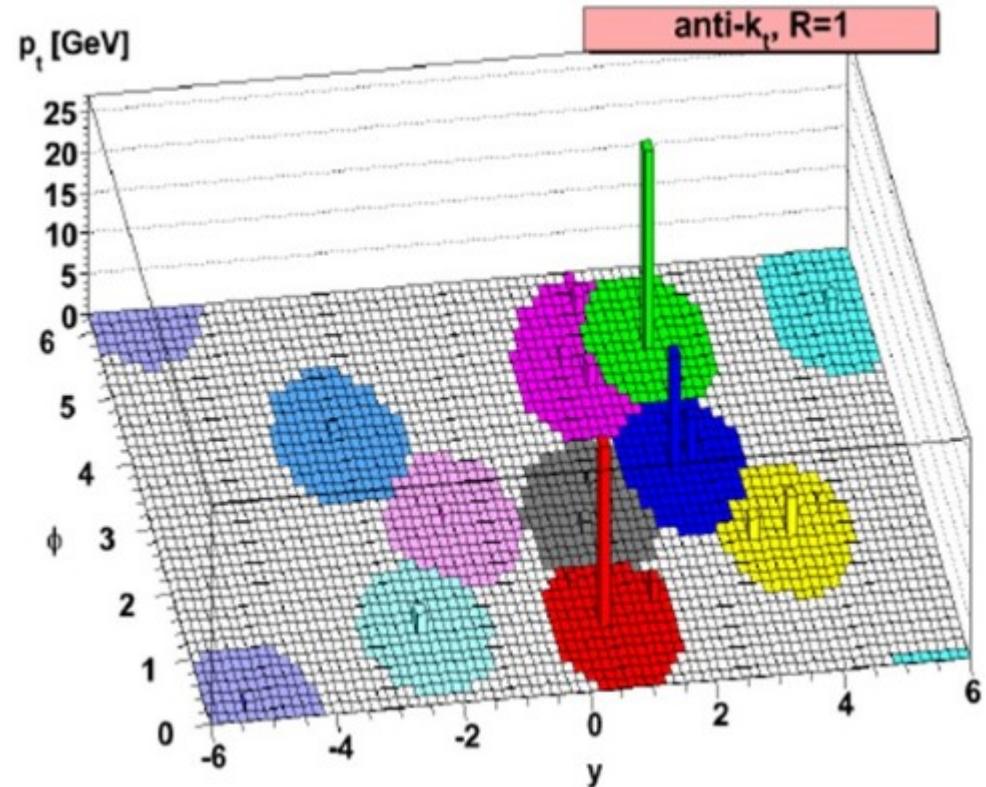
Jet candidates



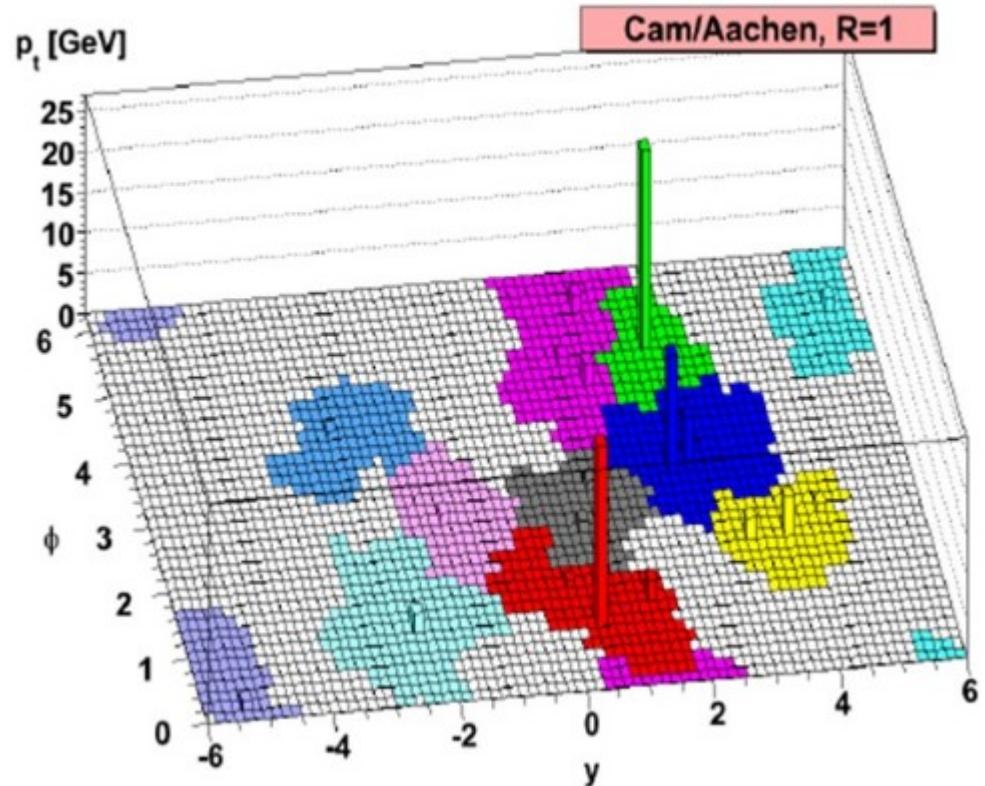
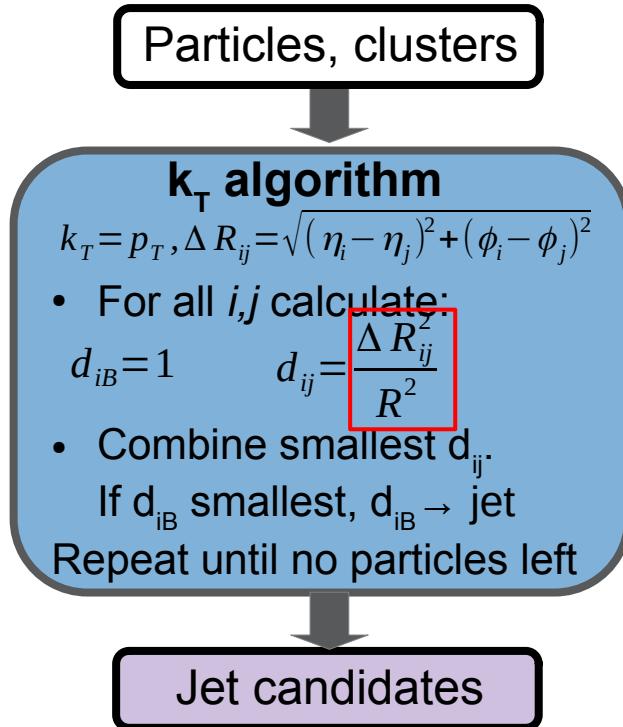
# anti- $k_T$ jet finding algorithm



Jet candidates



# Cambridge/Aachen jet finding algorithm



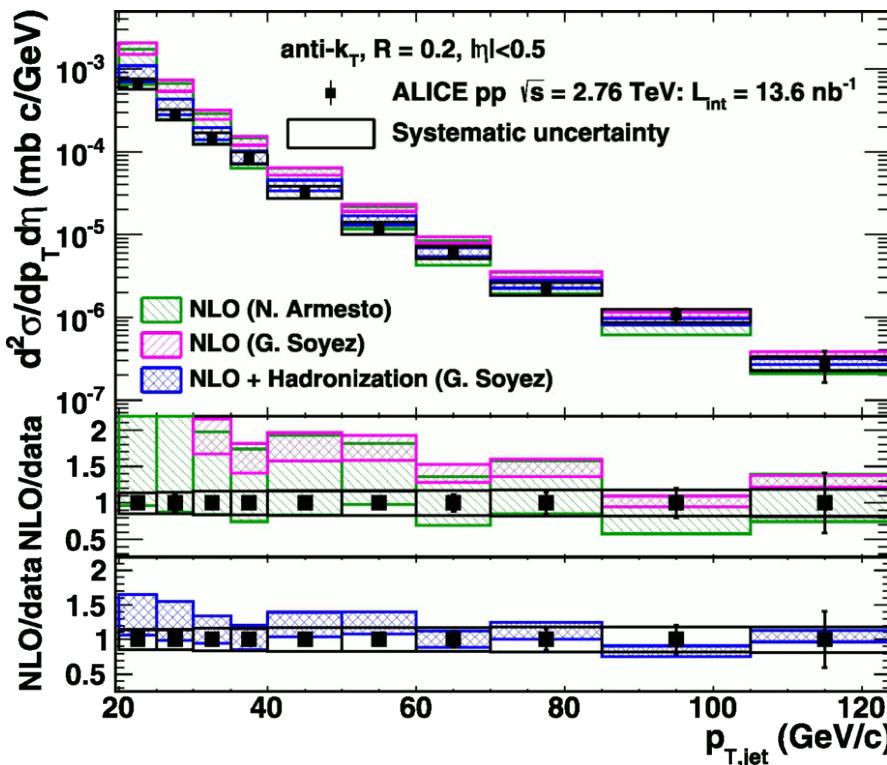
A jet is what a jet finder finds.

# Jet cross-section in pp

$\sqrt{s} = 2.76 \text{ TeV}, R = 0.2$  Inclusive

arXiv:1301.3475

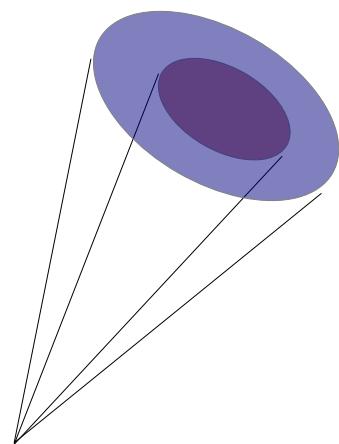
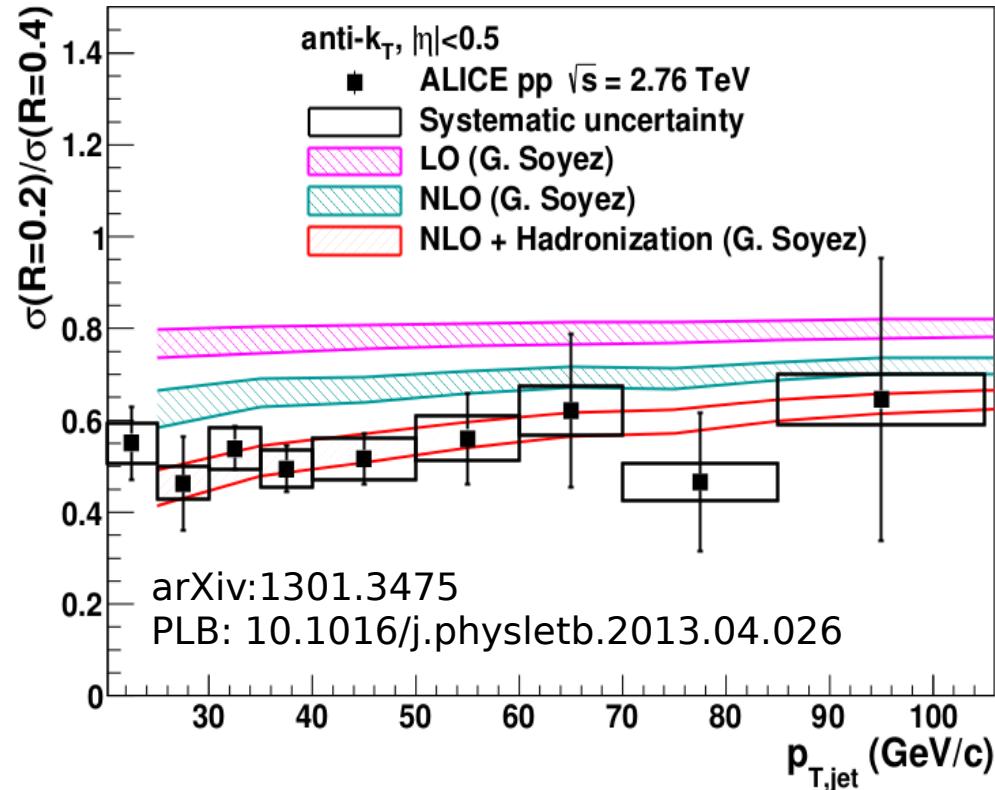
PLB: 10.1016/j.physletb.2013.04.026



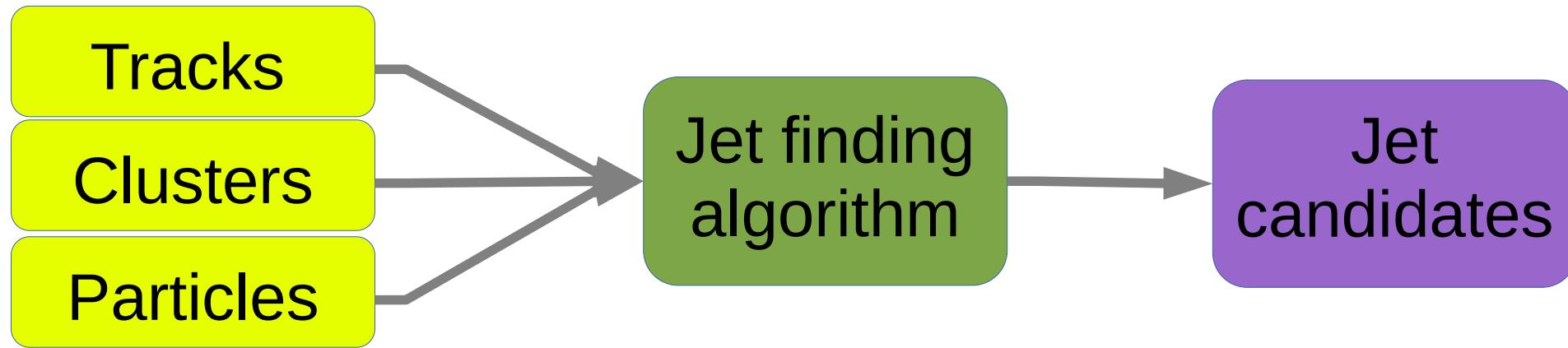
- Green and magenta bands: NLO on Parton level
- Blue band: NLO + hadronization
- Hadronization calculations necessary to describe data

# Jet ratios in pp

$\sqrt{s} = 2.76 \text{ TeV}, R = 0.2, 0.4 \text{ Inclusive}$



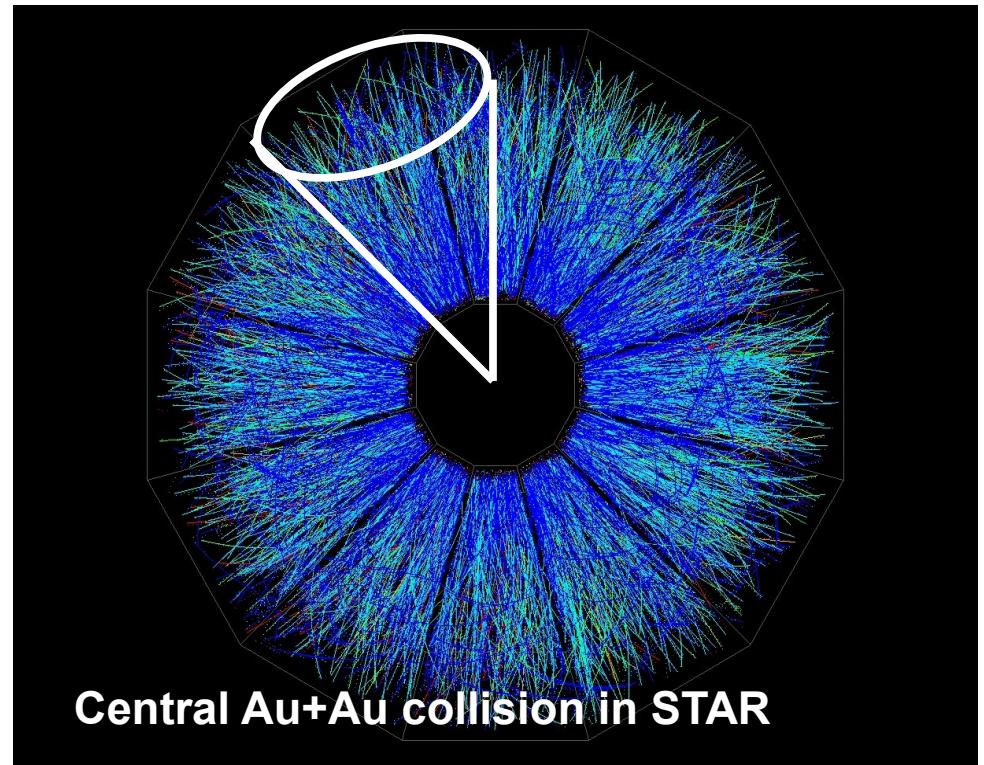
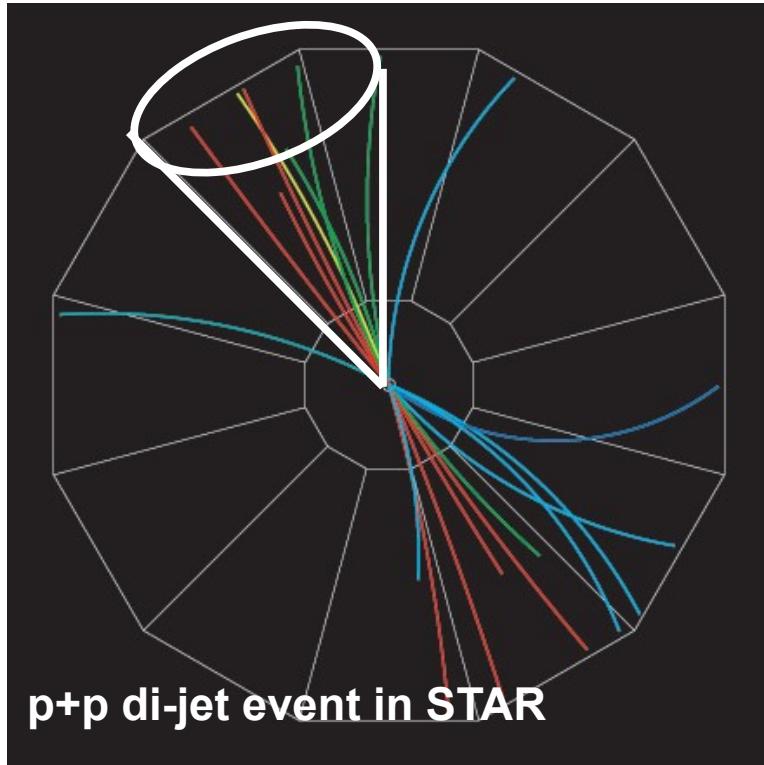
# Mini-summary



- Jets are not partons
- Good jet finders:
  - Infrared and colinear safe
  - $k_T$ , anti- $k_T$ , Cambridge/Aachen, SIScone
- Jet is defined by jet finder, its parameters
- PDFs, fragmentation functions non-perturbative  
→ all jet measurements sensitive to somewhat non-perturbative effects
- Good agreement between theory and experiment

Jets in A+A collisions  
What assumptions am I making?

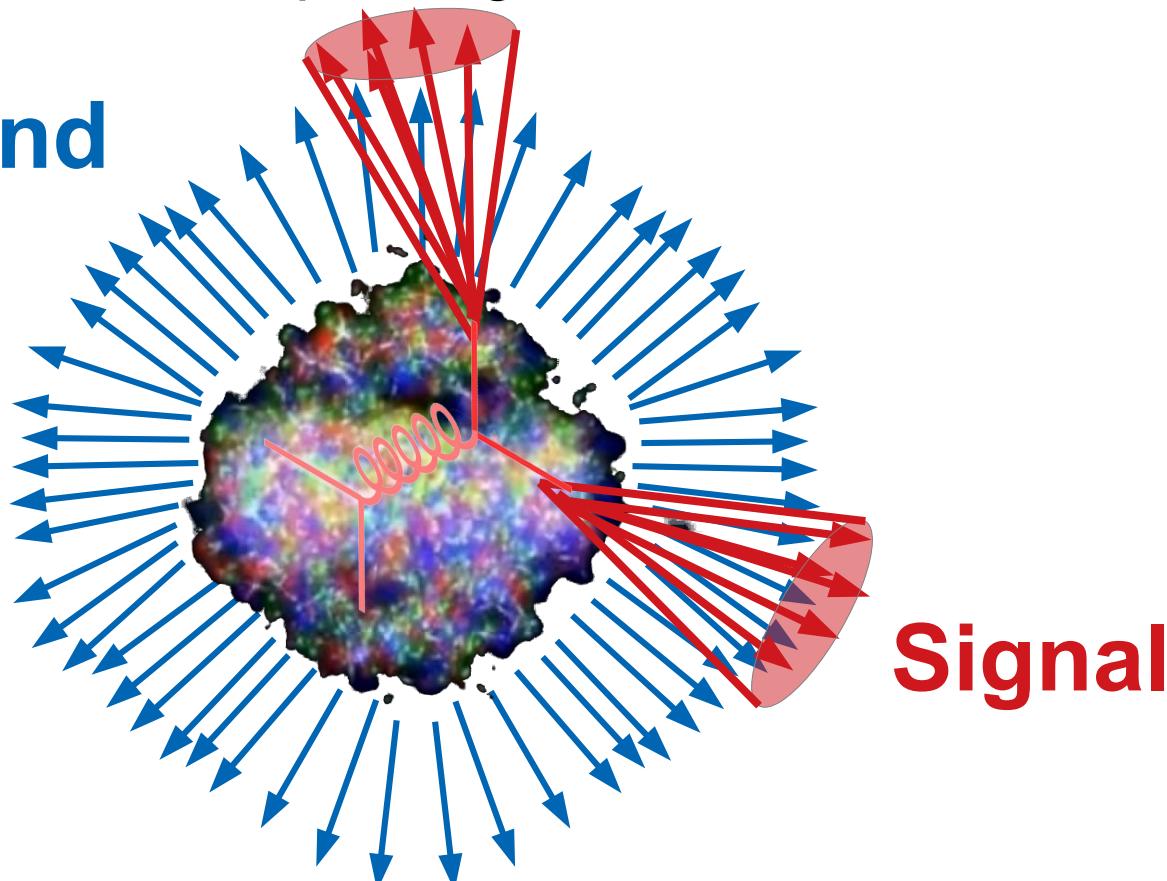
# $p+p$ vs $A+A$



# Signal vs Background:

## The standard paradigm

**Background**



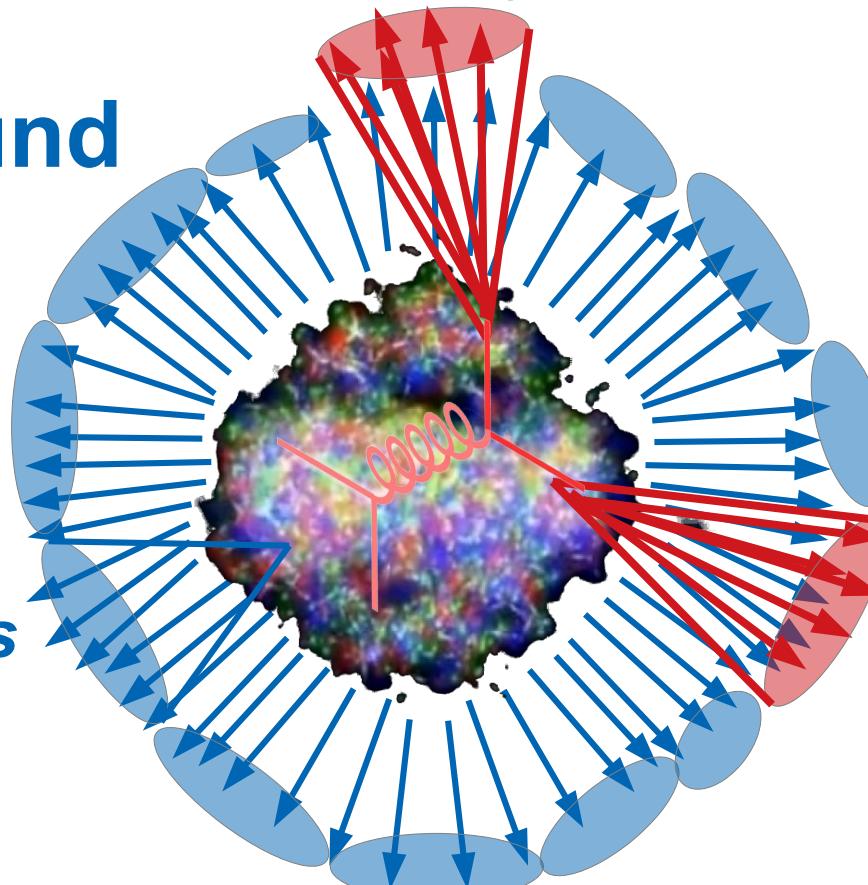
**Signal**

# Signal vs Background: The standard paradigm

Background

*Combinatorial jets*

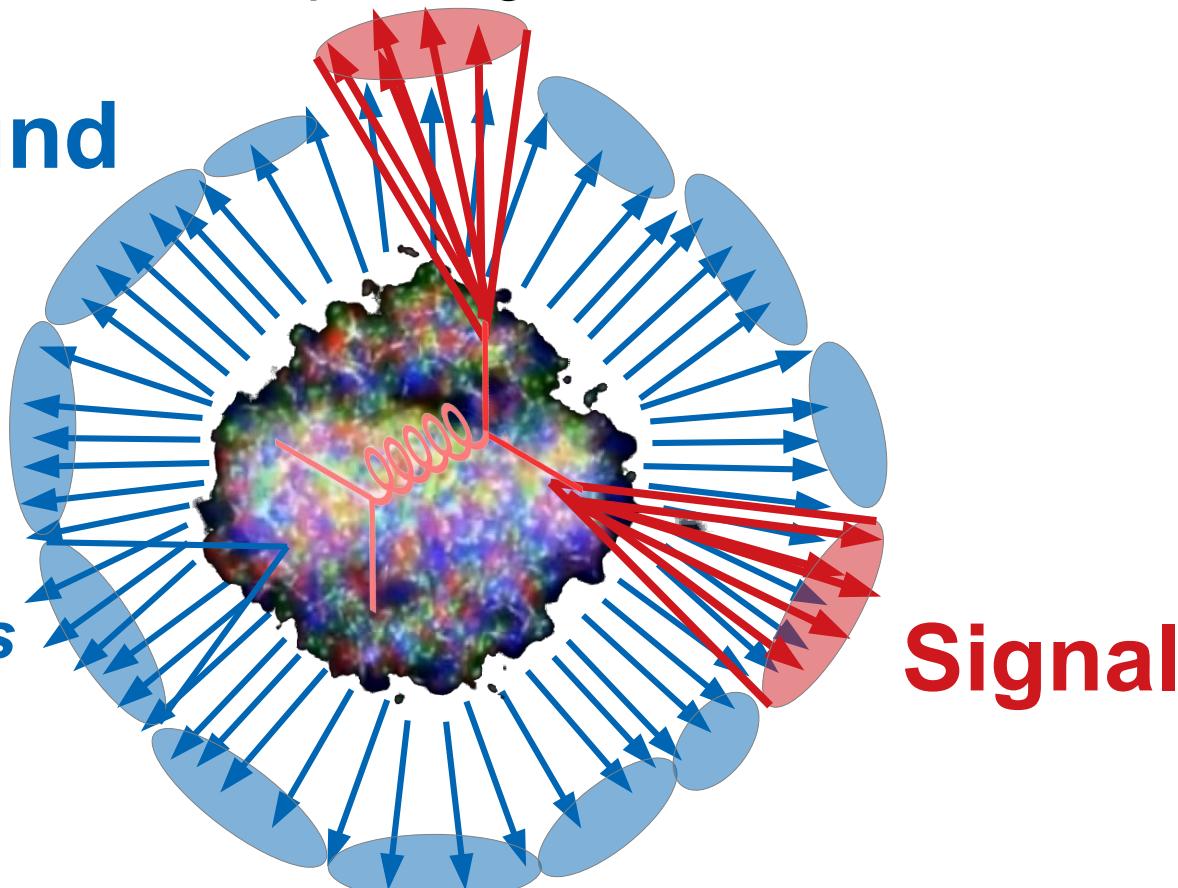
Signal



# Signal vs Background:

## The standard paradigm

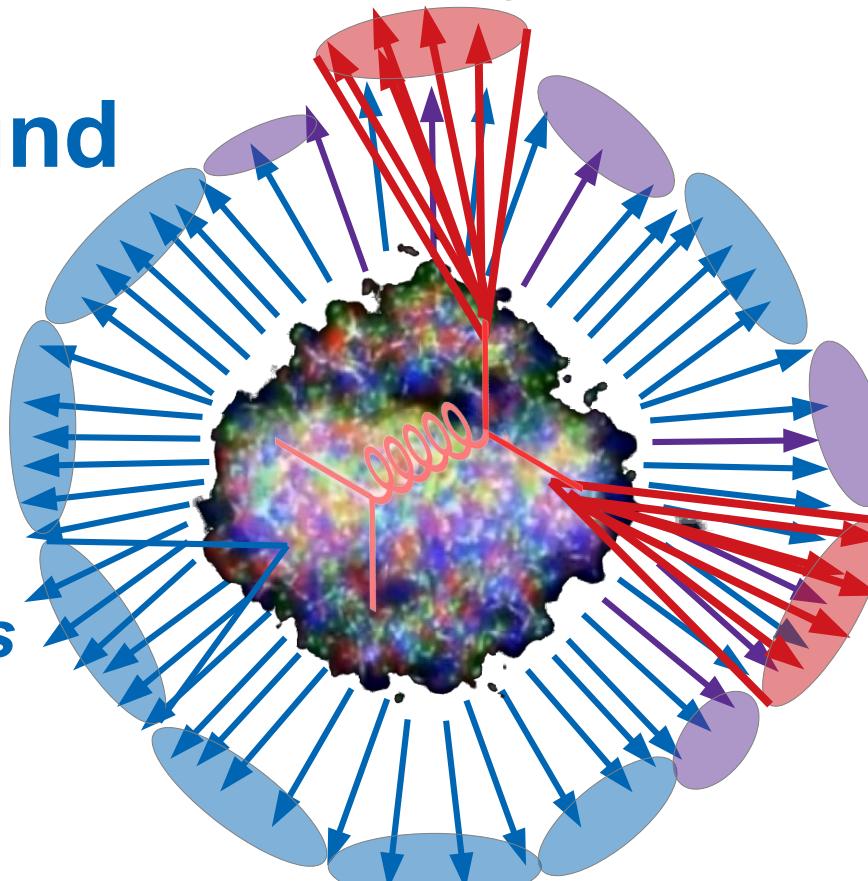
Background



Signal

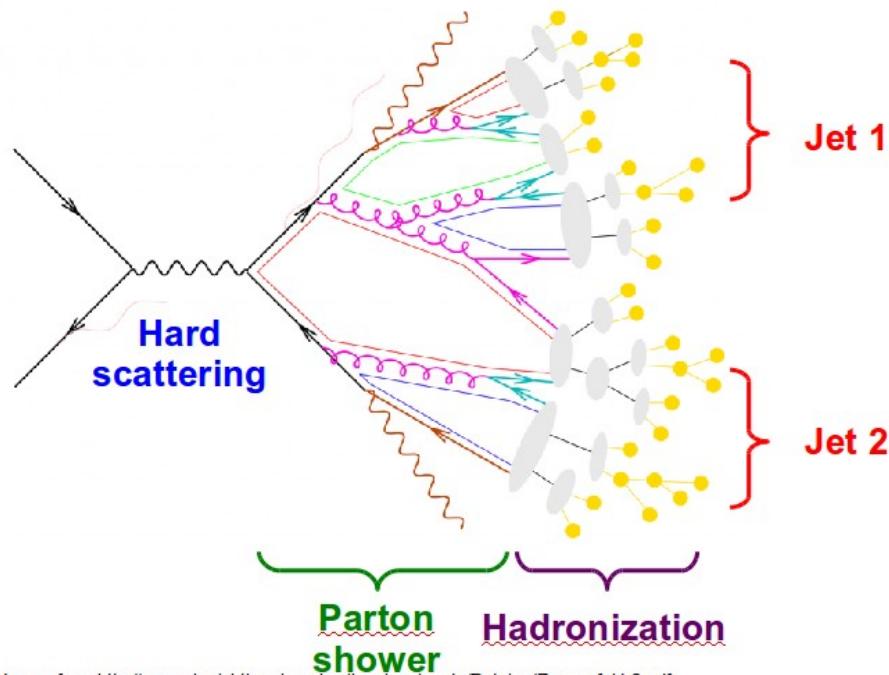
# Signal vs Background: The standard paradigm

Background



\*Some gray areas

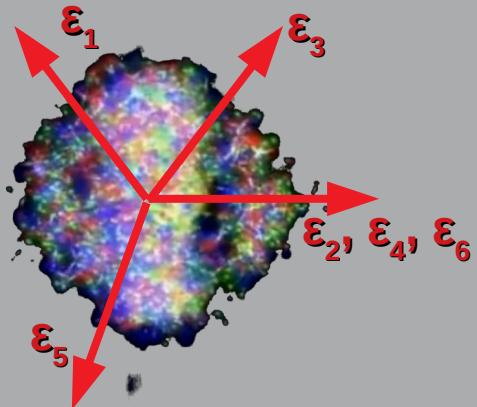
# Jet finding in AA collisions



- Jet finder: groups final state particles into jet candidates
  - Anti- $k_T$  algorithm  
JHEP 0804 (2008) 063 [arXiv:0802.1189]
- Combinatorial jet candidates
- Energy smearing from background
- Sensitive to methods to suppress combinatorial jets and correct energy
- Focus on narrow/high energy jets

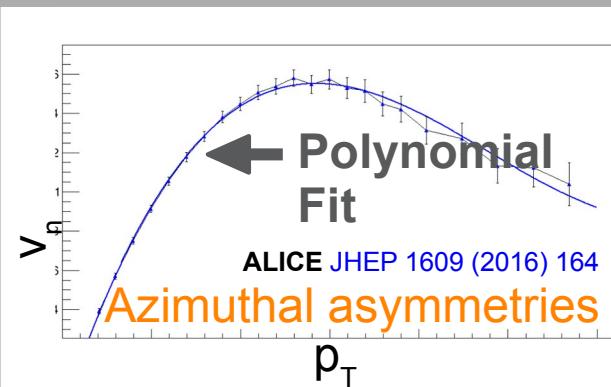
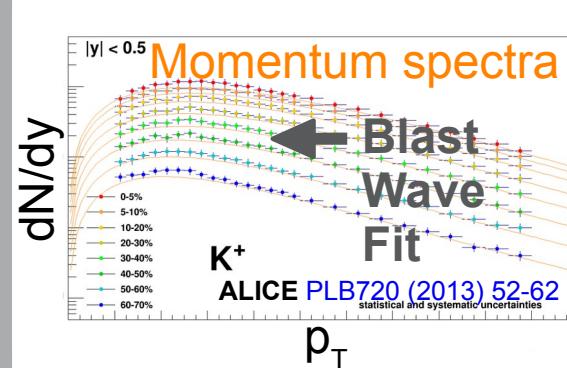
# TennGen background generator

## Event properties



- Even event planes fixed at  $\Psi=0$
- Odd planes at random  $\varphi$
- Multiplies from ALICE PRC88 (2013) 044910

## Track properties



→ Random  $p_T$

→  $v_n$

→ Random  $\varphi$

No jets! No resonances  
Emulates hydro correlations

# PYTHIA Angantyr

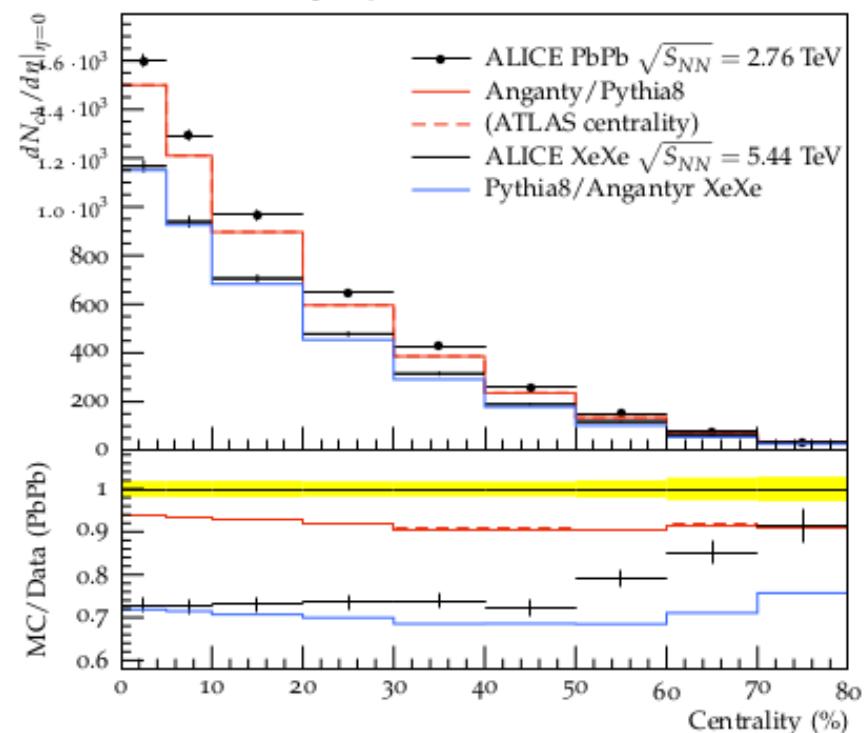
JHEP (2018) 2018: 134

- Based on PYTHIA 8

Sjöstrand, Mrenna & Skands,  
JHEP05 (2006) 026  
Comput. Phys. Comm. 178 (2008) 852.

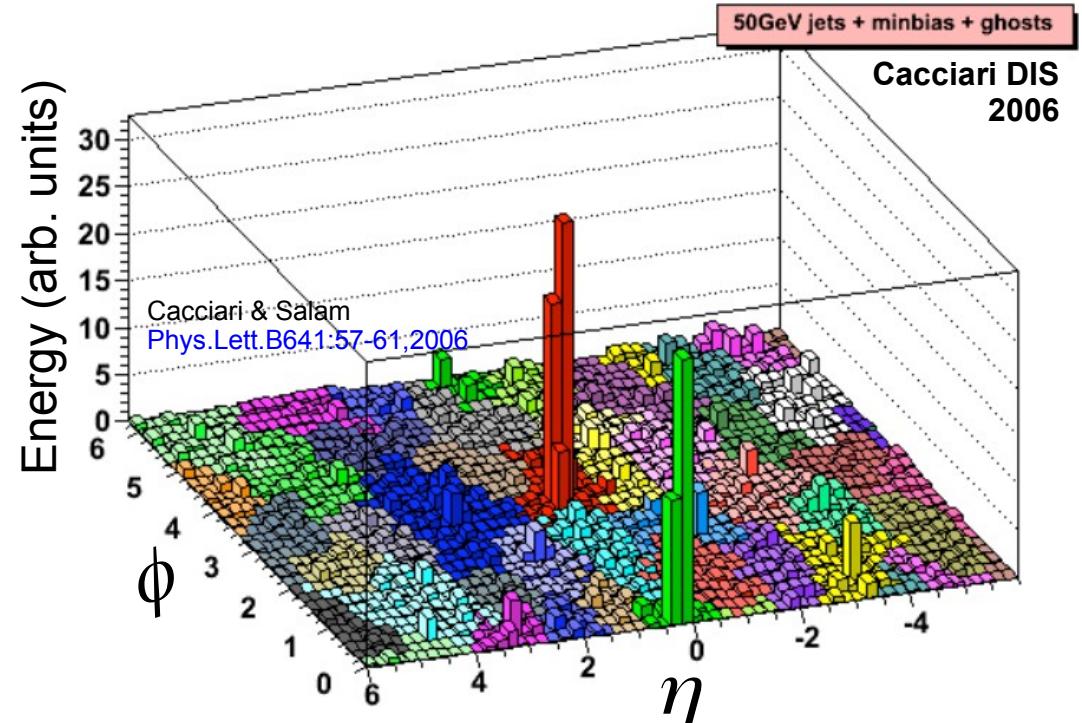
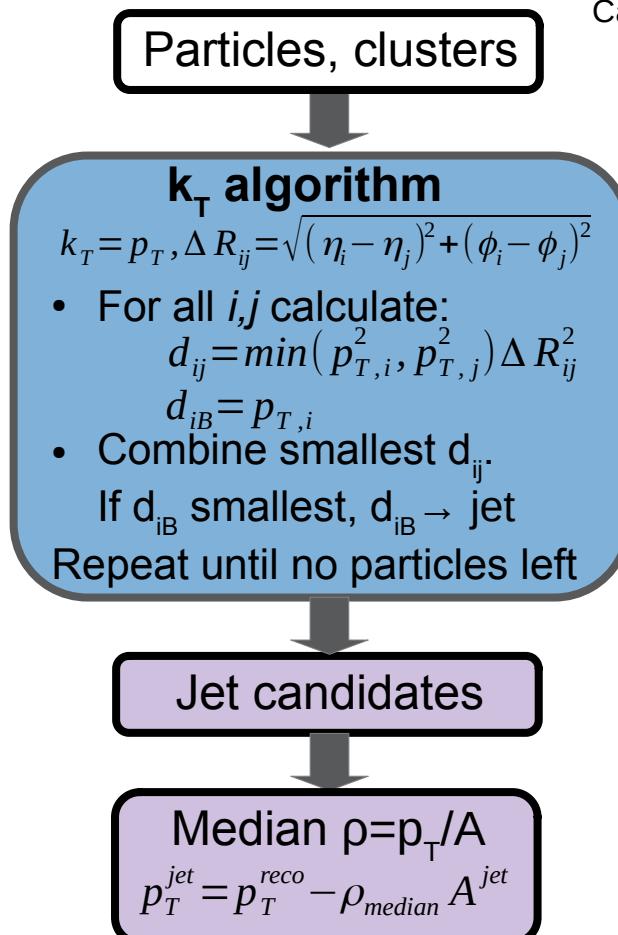
- Based on Fritiof & wounded nucleons
- N-N collisions w/fluctuating radii  
→ fluctuating  $\sigma$

Lots of jets! And resonances!  
No hydrodynamics, no jet quenching

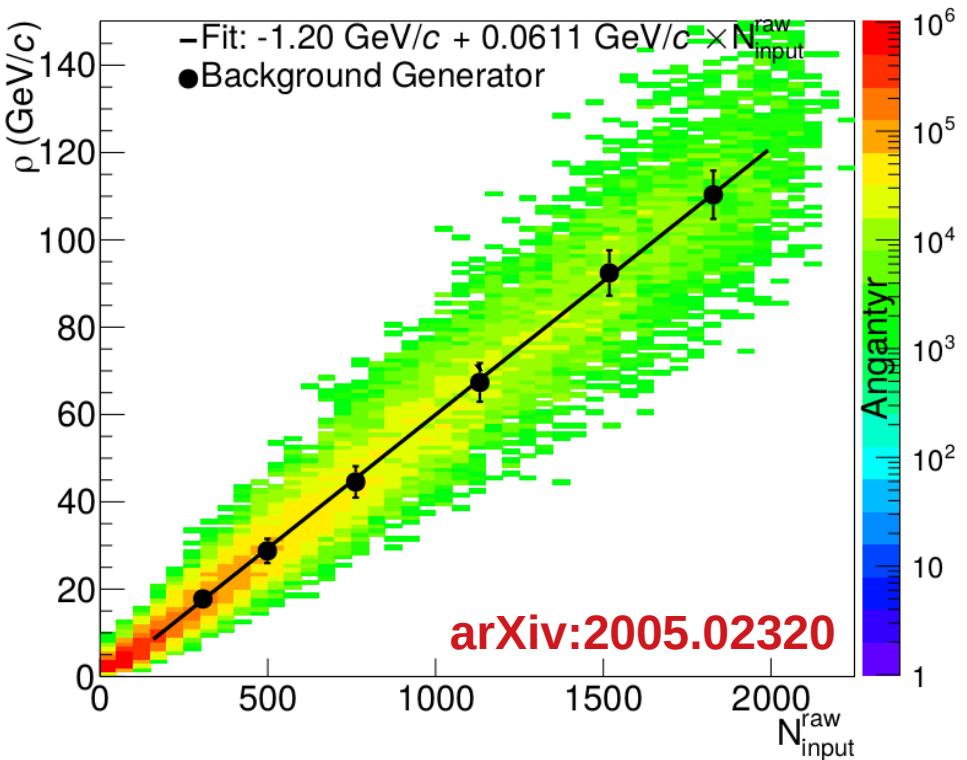
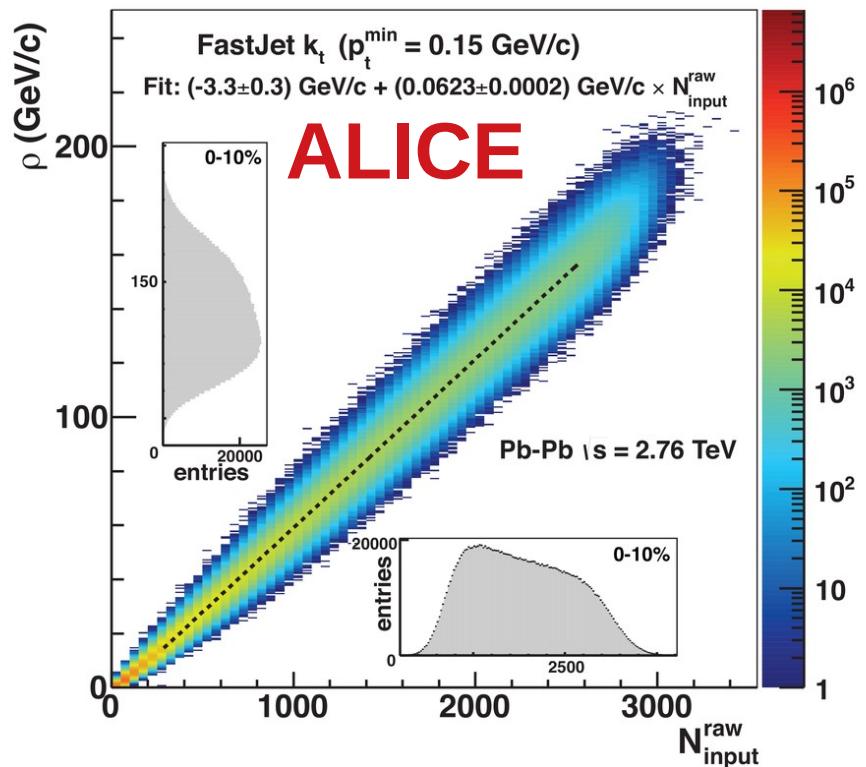


# Area-based background subtraction

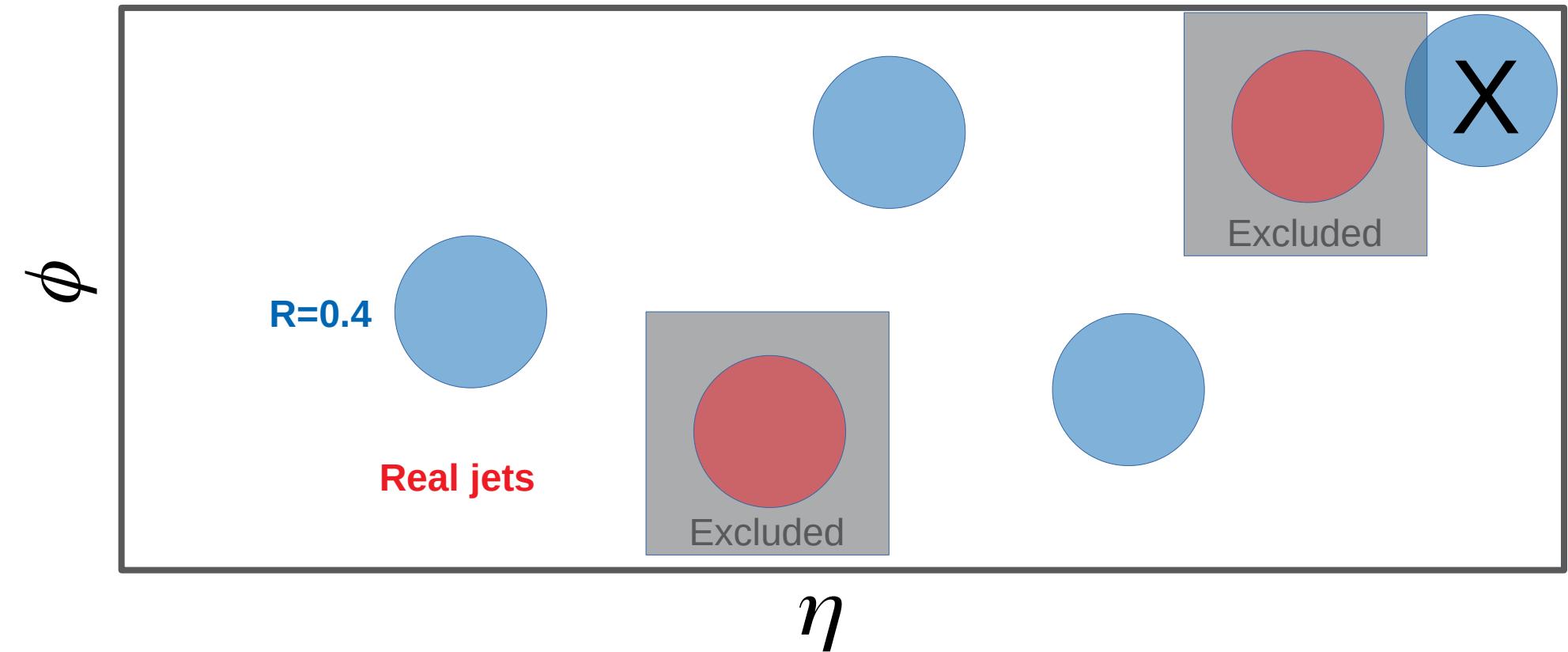
Cacciari & Salam, PLB659:119–126, 2008



# Background density $\rho$



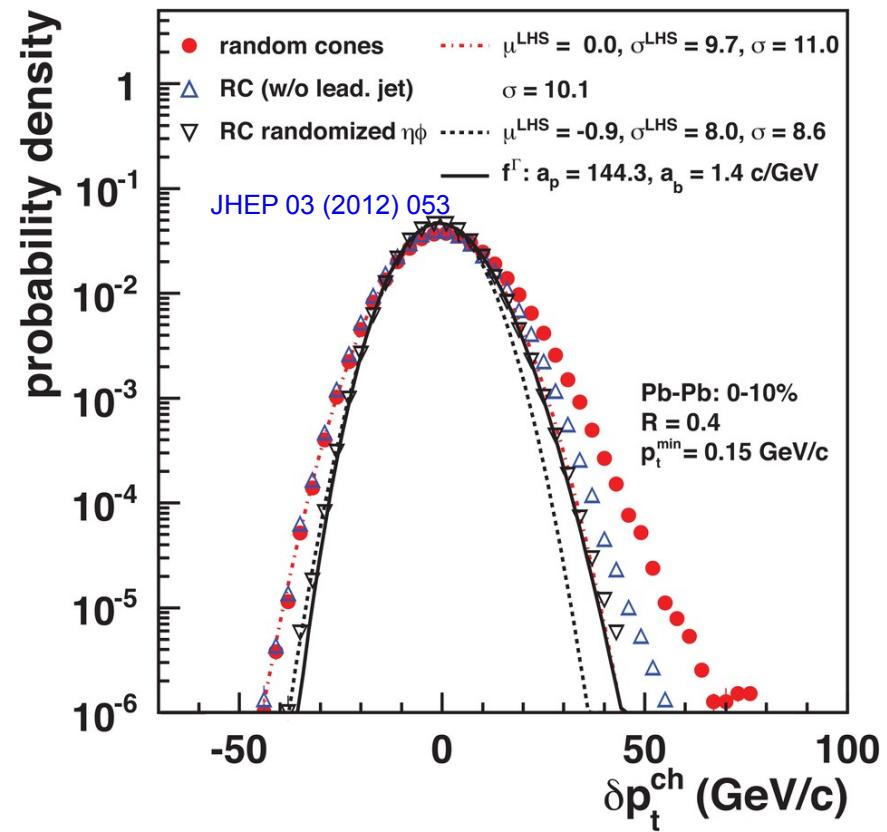
# Random cones



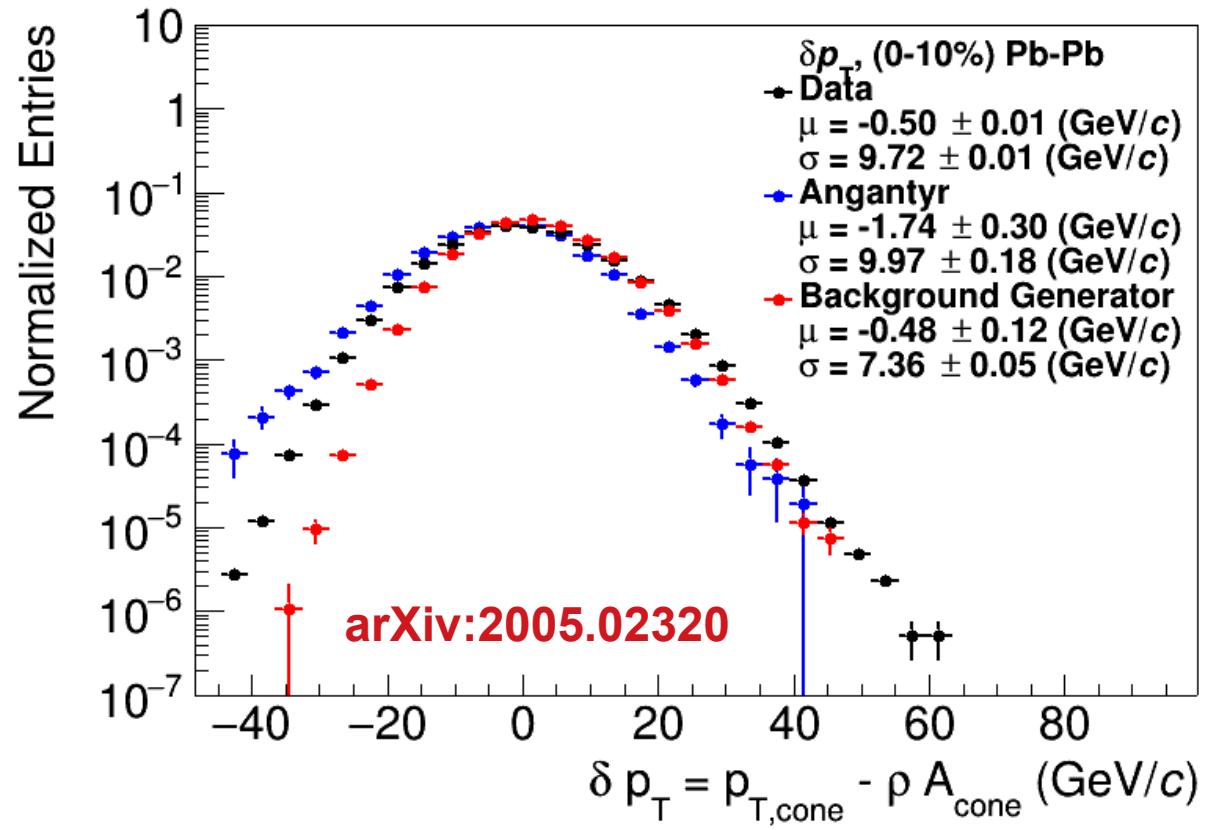
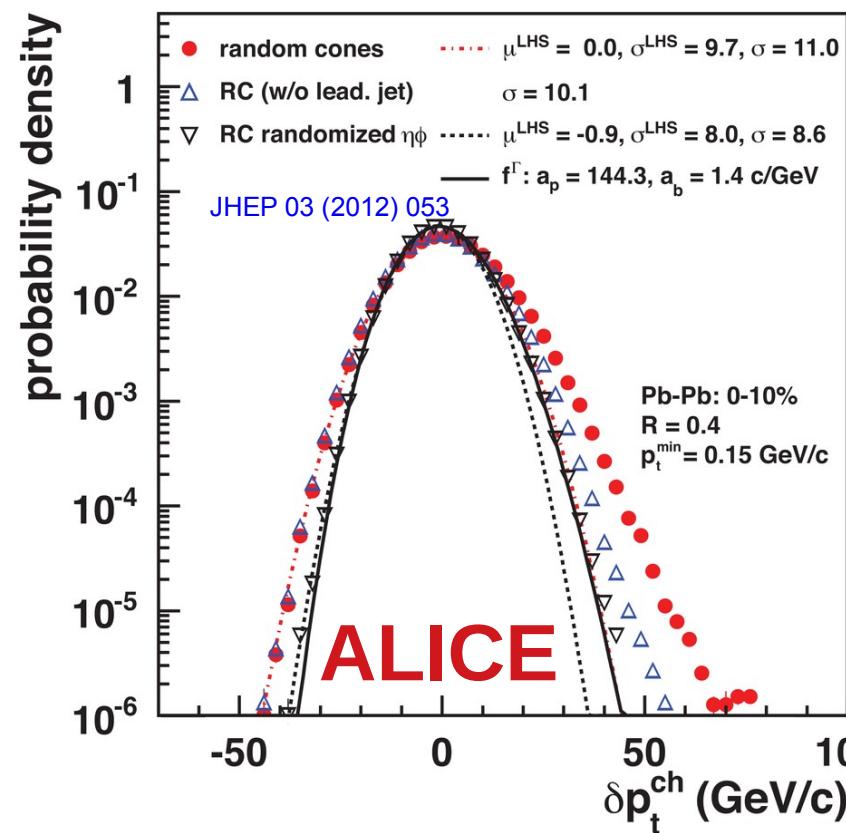
# Random cones in ALICE

- Estimate  $\rho$ 
  - $k_T$  jet finder  $\rightarrow$  jet candidates
  - $\rho = \text{Median}(p_T/A)$
- Draw Random cone

$$\delta p_T = p_T^{reco} - \rho A$$



# Random cones



# Shape of width of the distribution

## Single particle spectra

$$f_{\Gamma}(p_T, p, b) = \frac{b}{\Gamma(p)} (b p_T)^{p-1} e^{-bx}$$

$$\frac{dN}{dy} \propto f_{\Gamma}(p_T, 2, b) = b^2 p_T e^{-kp_T}$$

$$\mu_{p_T} = \frac{p}{b}, \sigma_{p_T} = \frac{\sqrt{p}}{b}$$

Tannenbaum, PLB(498), 1–2, Pg.29-34(2001)

## $\Sigma p_T$ of N particles $\rightarrow$ N-fold convolution:

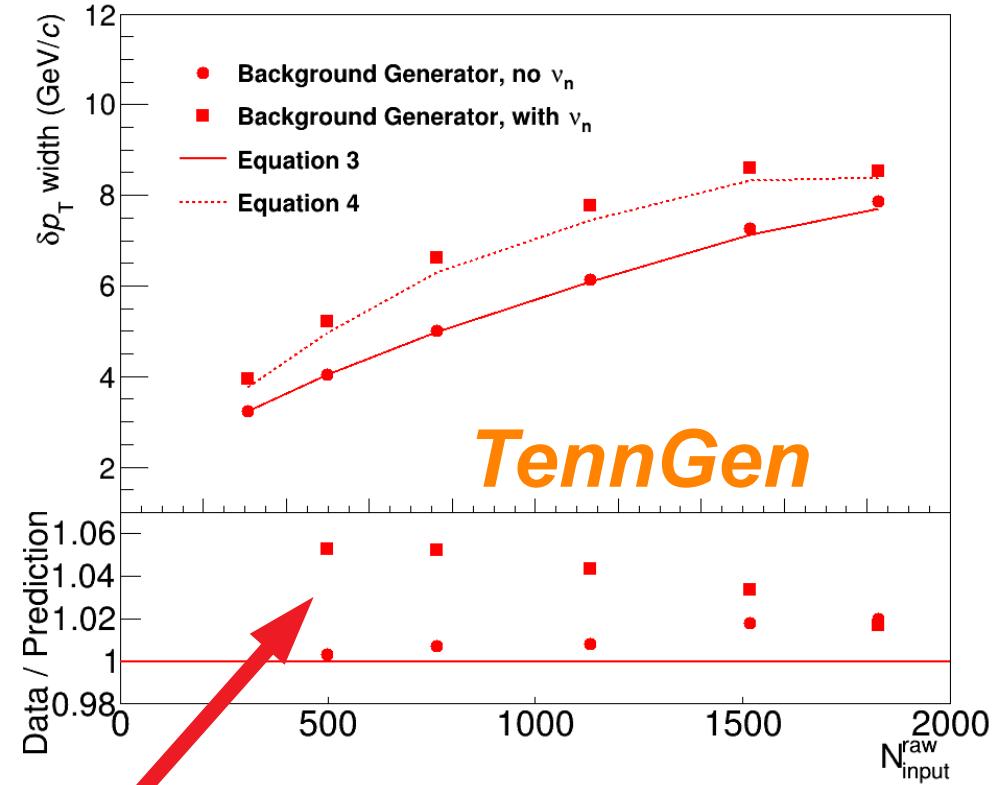
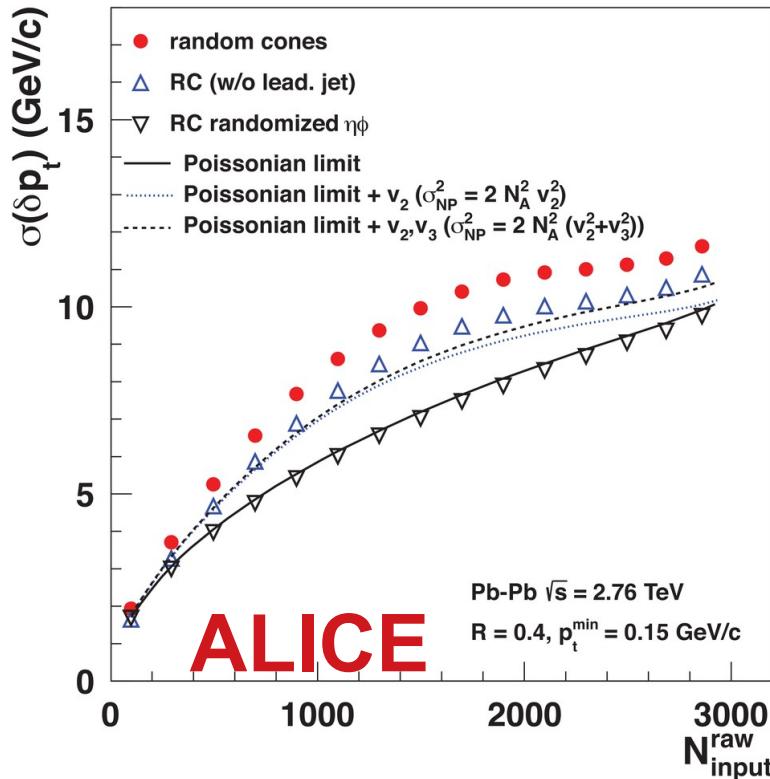
$$f_N(p_T, p, b) = f_{\Gamma}(p_T, Np, b) \quad \frac{dpT^{total}}{dy} \propto f_N(p_T, Np, b)$$
$$N = \frac{N_{total}}{A_{total}} \pi R^2 \quad \mu_{total} = \frac{Np}{b} = N \mu_{p_T}, \sigma_{total} = \frac{\sqrt{Np}}{b} = \sqrt{N} \sigma_{p_T}$$

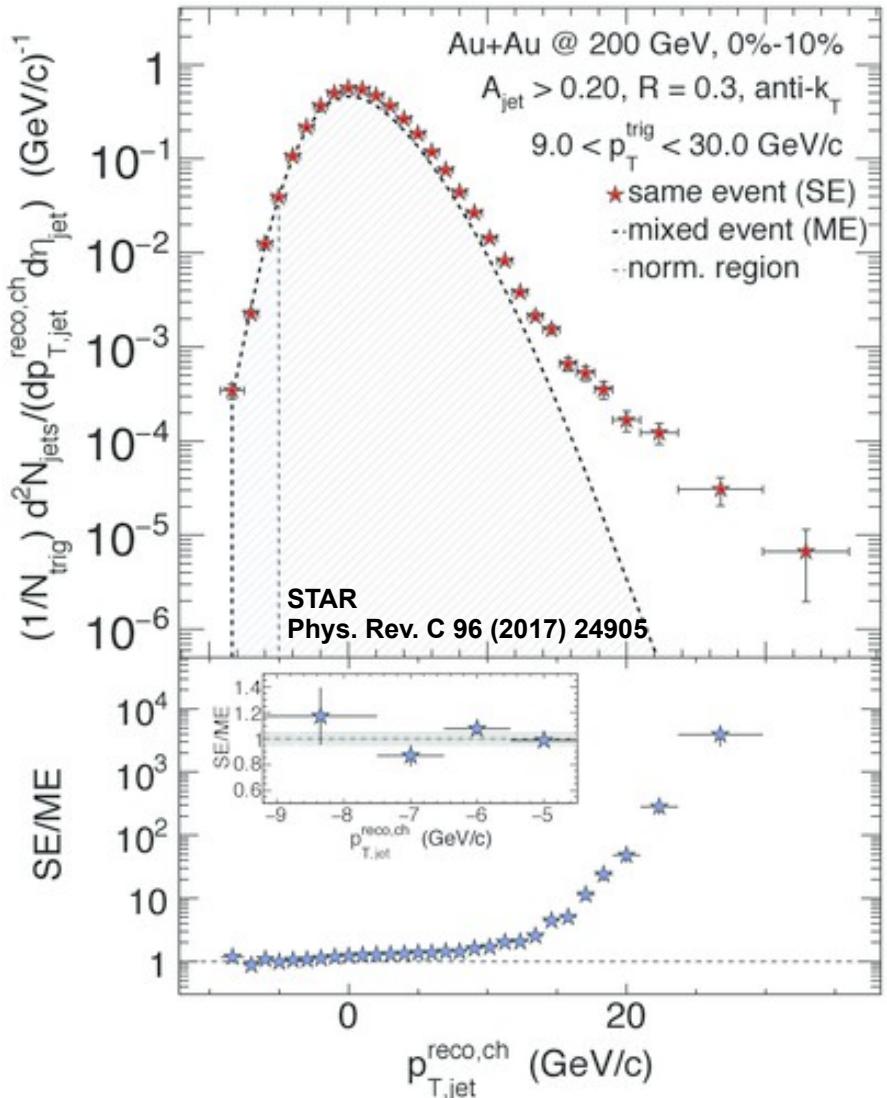
Add Poissonian fluctuations in N:  $\sigma_{total} = \sqrt{N \sigma_{p_T}^2 + N \mu_{p_T}^2}$

Add non-Poissonian fluctuations in N due to flow

$$\sigma_{total} = \sqrt{N \sigma_{p_T}^2 + (N+2 \sum_n v_n^2) \mu_{p_T}^2}$$

# Width vs multiplicity

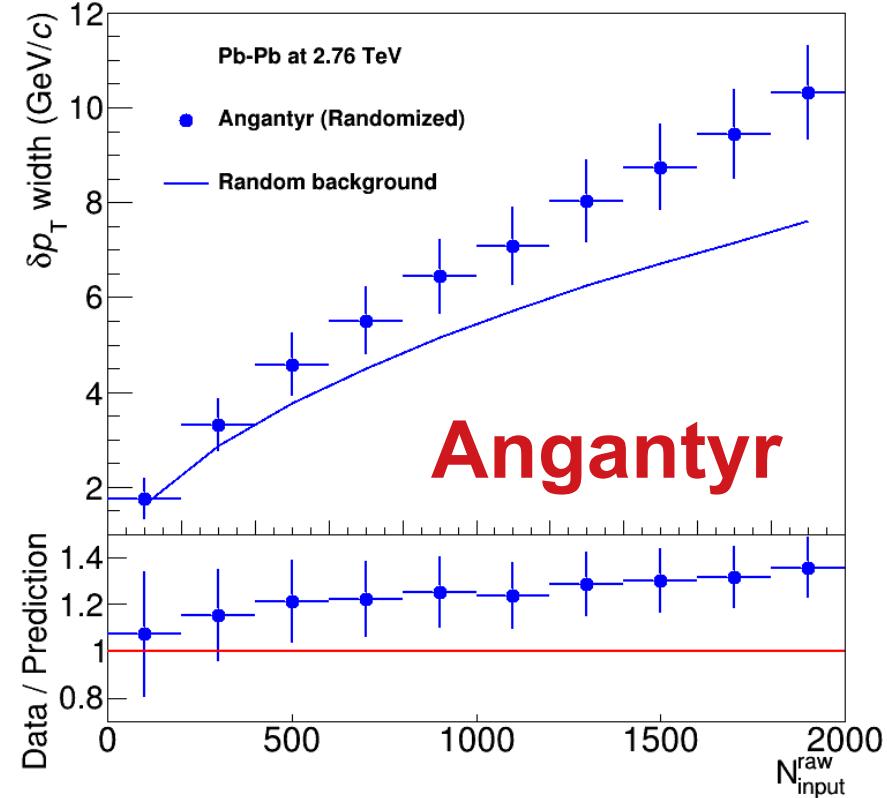
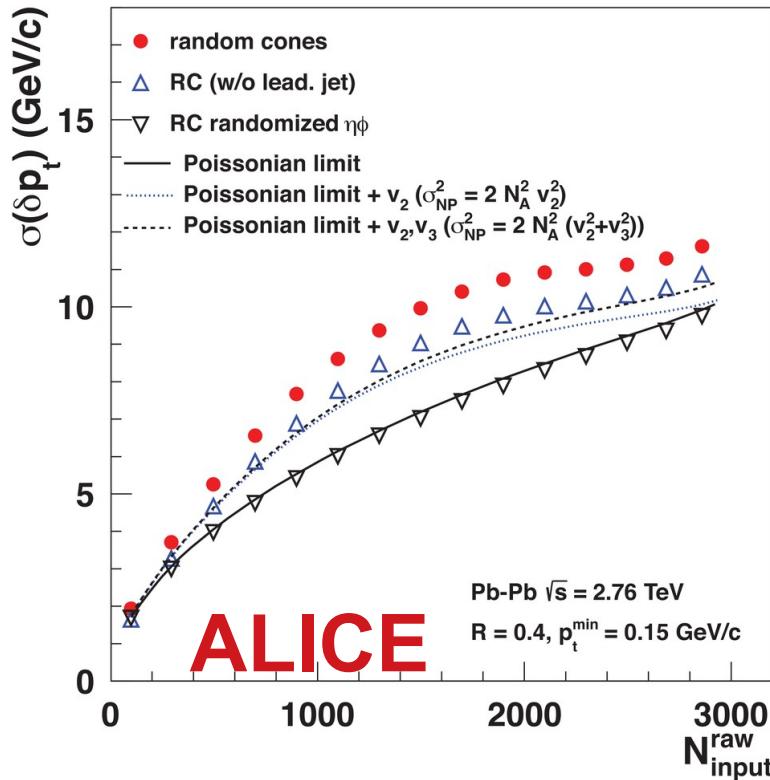




## Mixed events

- Gets background up to a normalization factor
- Good agreement with the data... but 20% discrepancies still within uncertainties
- In measurement with background suppressed (h-jet correlations)
- Did not see such agreement at the LHC

# Width vs multiplicity



Doesn't go away with random track orientation!

# Shape of width of the distribution

## Single particle spectra

$$f_{\Gamma}(p_T, p, b) = \frac{b}{\Gamma(p)} (b p_T)^{p-1} e^{-bx}$$

$$\frac{dN}{dy} \propto f_{\Gamma}(p_T, 2, b) = b^2 p_T e^{-kp_T}$$

$$\mu_{p_T} = \frac{p}{b}, \sigma_{p_T} = \frac{\sqrt{p}}{b}$$

Tannenbaum, PLB(498), 1–2, Pg.29-34(2001)

Assumes shape

**$\Sigma p_T$  of N particles  $\rightarrow$  N-fold convolution:**

$$f_N(p_T, p, b) = f_{\Gamma}(p_T, Np, b) \quad \frac{dpT^{total}}{dy} \propto f_N(p_T, Np, b)$$
$$N = \frac{N_{total}}{A_{total}} \pi R^2 \quad \mu_{total} = \frac{Np}{b} = N \mu_{p_T}, \sigma_{total} = \frac{\sqrt{Np}}{b} = \sqrt{N} \sigma_{p_T}$$

Add Poissonian fluctuations in N:  $\sigma_{total} = \sqrt{N \sigma_{p_T}^2 + N \mu_{p_T}^2}$

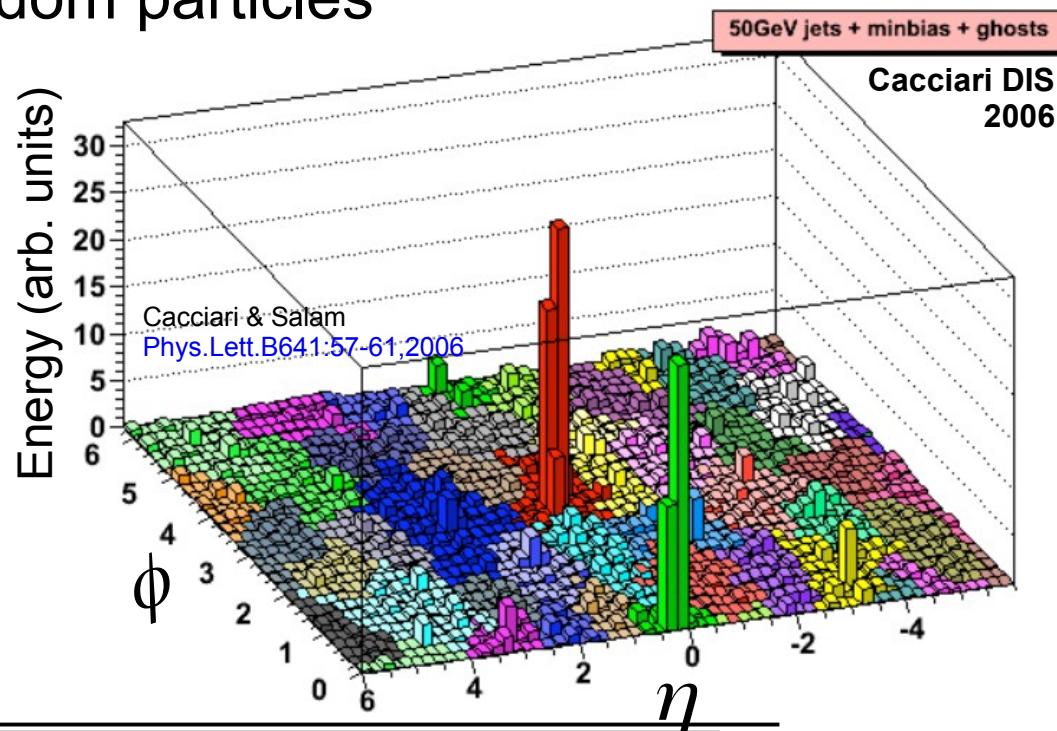
Add non-Poissonian fluctuations in N due to flow

$$\sigma_{total} = \sqrt{N \sigma_{p_T}^2 + (N + 2 \sum_n v_n^2) \mu_{p_T}^2}$$

Assumes uncorrelated number fluctuations

# Mini-summary

- Jet finders put all input clusters, tracks in a jet candidate
- Background is *dominated* by random particles
  - But 5% effects from flow
- Models have background too!
  - And it doesn't agree with data!
  - Sensitive to multiplicity, shape of spectrum

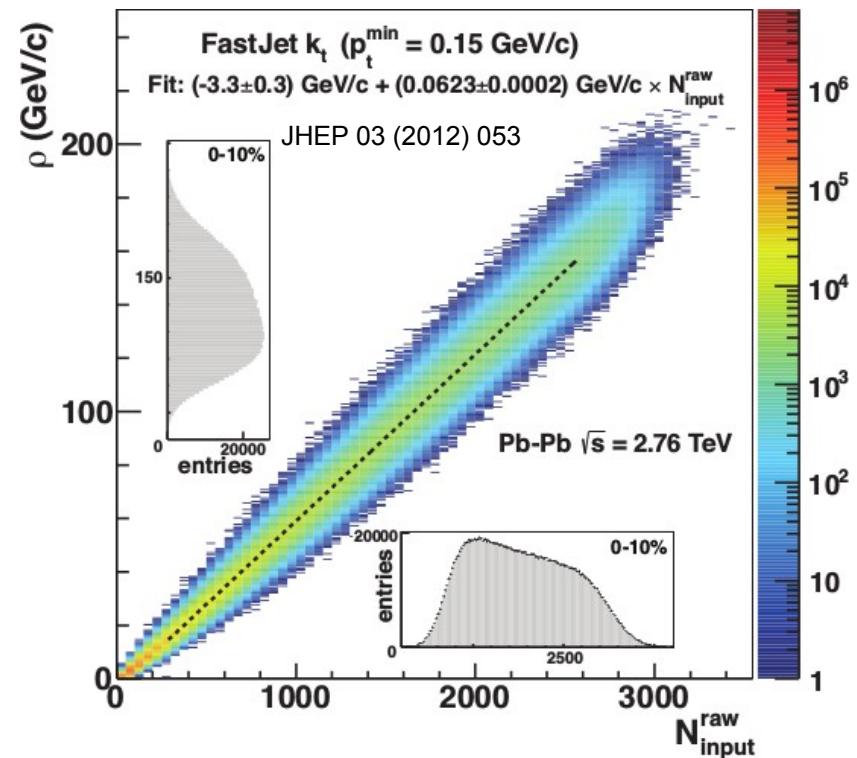


# Jets in A+A collisions: Dealing with background

# Focus on smaller angles

- Pros
  - Background is smaller
  - Background fluctuations smaller
- Cons:
  - Modifications expected at higher R
  - Biases sample towards quarks

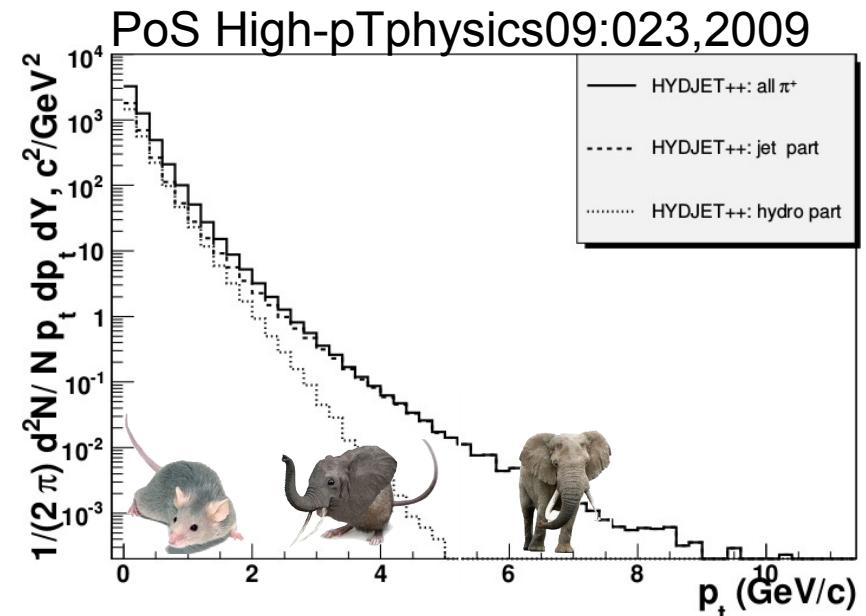
Aside: “quark” and “gluon” jet  
only defined at leading order.



# Focus on high $p_T$

- Pros:
  - Reduces combinatorial background
- Cons:
  - Cuts signal where we expect modifications
  - Could bias towards partons which have not interacted
  - Biases sample towards quark jets

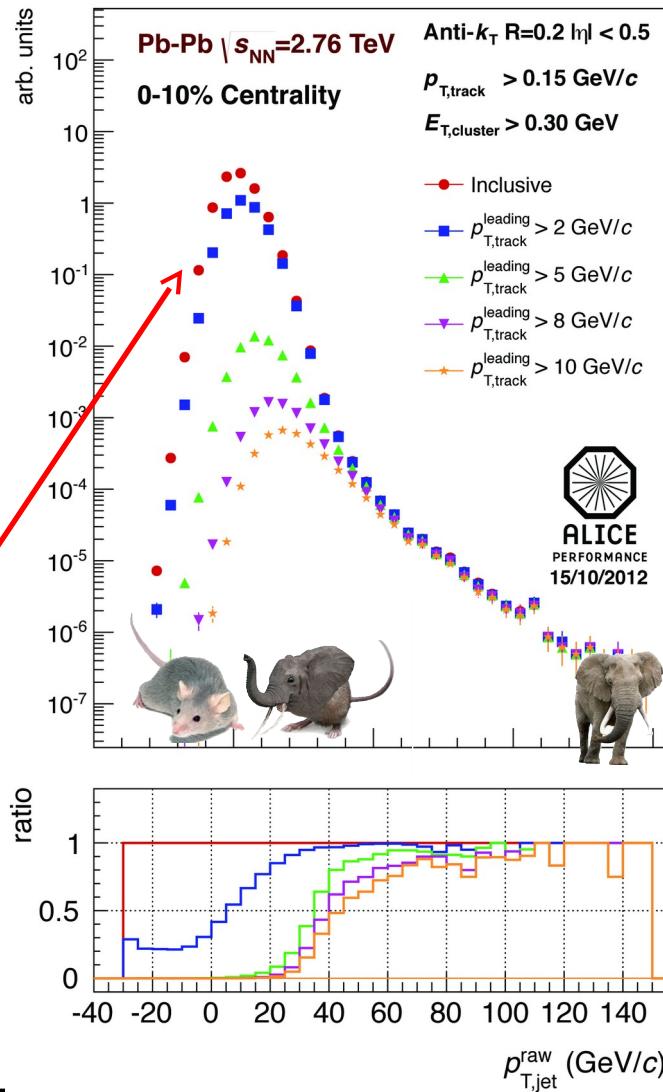
“Quark” and “gluon” jets only defined at leading order!



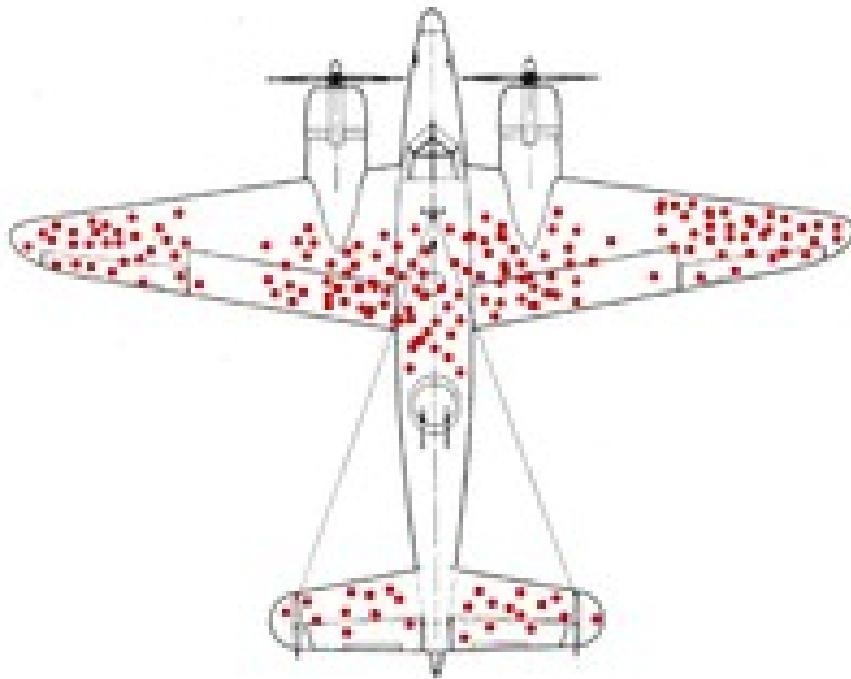
# Area-based subtraction

- ALICE/STAR
- Require leading track  $p_T > 5 \text{ GeV}/c$ 
  - Suppresses combinatorial “jets”
  - Biases fragmentation
- No threshold on constituents
- Limited to small R

Combinatorial “jets”



# Survivor bias



- **WWII Example:** holes planes returning indicate where it's *safer* to get hit
- We're looking at the jets which *remain*





<http://walkthewilderness.net/animals-of-india-72-asiatic-elephant/>

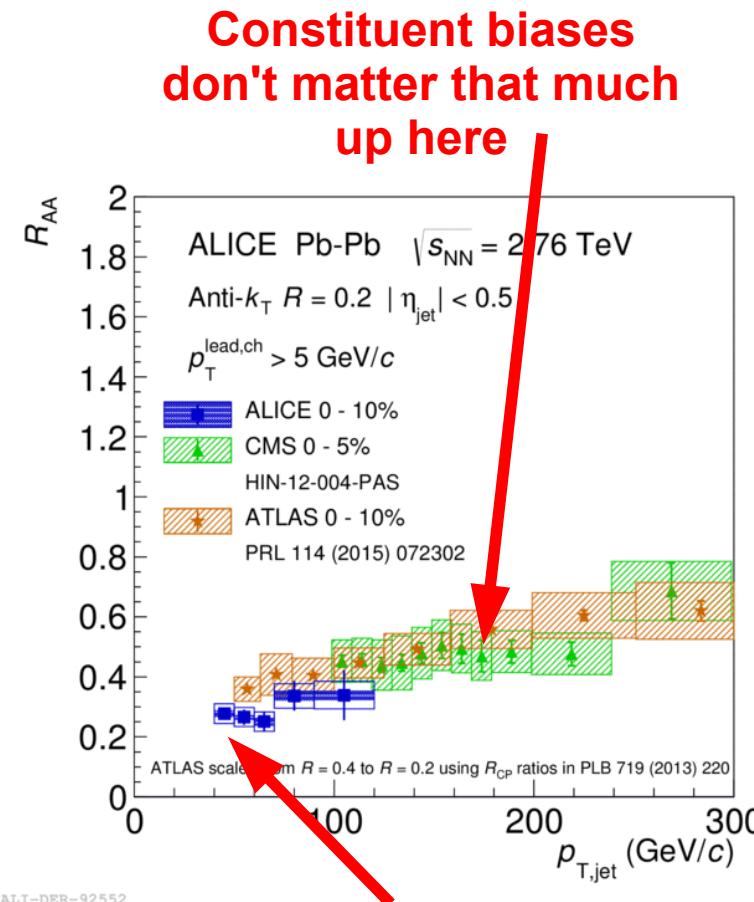
What you see depends on what you're  
looking for

# Bias & background

- **Experimental background subtraction methods:** complex, make assumptions, apply biases
- **Survivor bias:** Modified jets probably look more like the medium
- **Quark/Gluon bias:**
  - Quark jets are narrower, have fewer tracks, fragment harder [Z Phys C 68, 179-201 (1995), Z Phys C 70, 179-196 (1996), ]
  - Gluon jets reconstructed with  $k_T$  algorithm have more particles than jets reconstructed with anti- $k_T$  algorithm [Phys. Rev. D 45, 1448 (1992)]
  - Gluon jets fragment into more baryons [EPJC 8, 241-254, 1998]
- **Fragmentation bias:** Experimental measurements explicitly select jets with hard fragments

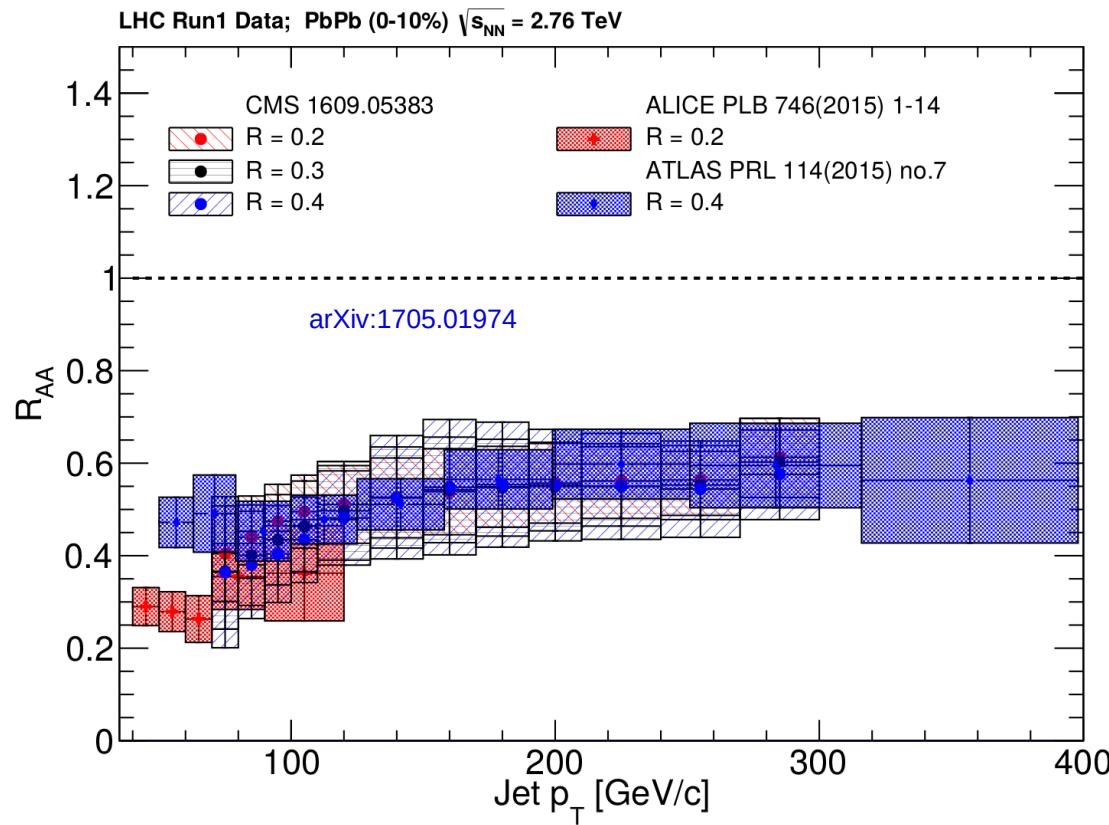
# Iterative procedure

- Used by ATLAS & CMS
- ATLAS
  - **Calorimeter jets:** Reconstruct jets with  $R=0.2$ .  $v_2$  modulated  $\langle Bkgd \rangle$  estimated by energy in calorimeters excluding jets with at least one tower with  $E_{\text{tower}} > \langle E_{\text{tower}} \rangle$
  - **Track jets:** Use tracks with  $p_T > 4 \text{ GeV}/c$
  - Calorimeter jets from above with  $E > 25 \text{ GeV}$  and track jets with  $p_T > 10 \text{ GeV}/c$  used to estimate background again.
  - Calorimeter tracks matching one track with  $p_T > 7 \text{ GeV}/c$  or containing a high energy cluster  $E > 7 \text{ GeV}$  are used for analysis down to  $E_{\text{jet}} = 20 \text{ GeV}$

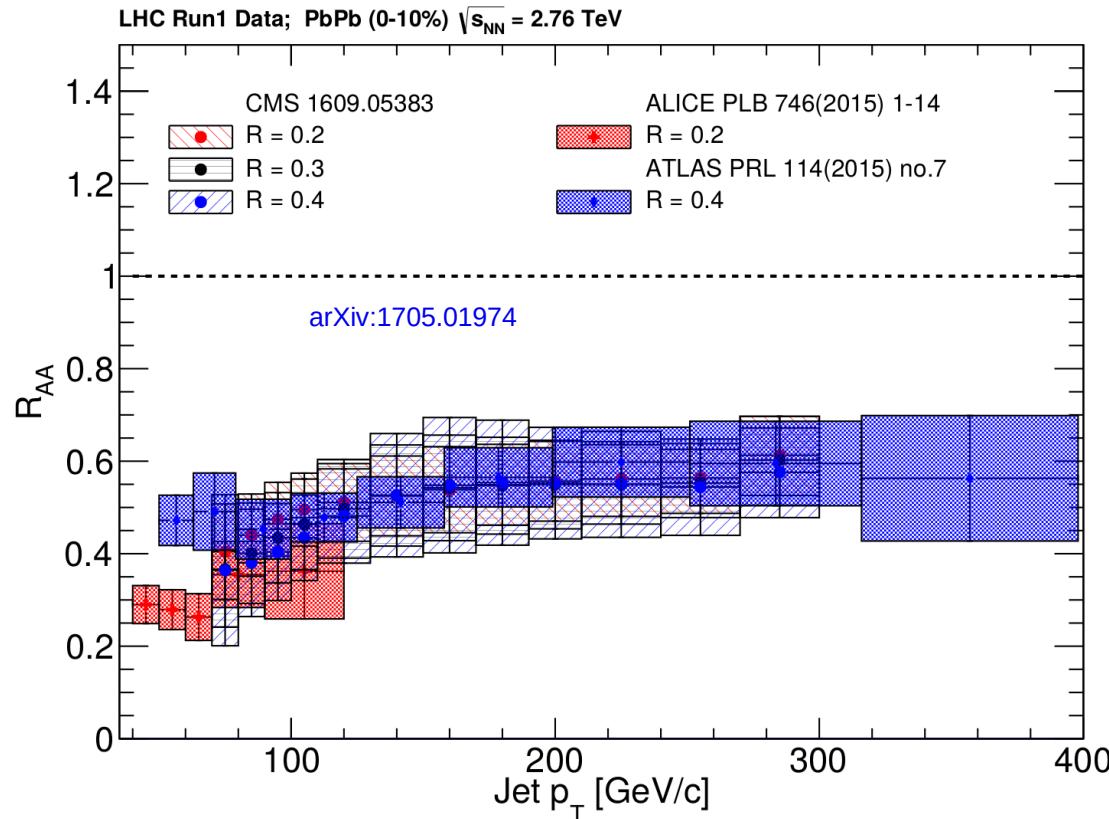


But they do matter  
down here!

# Jet R<sub>AA</sub>



# Jet R<sub>AA</sub>



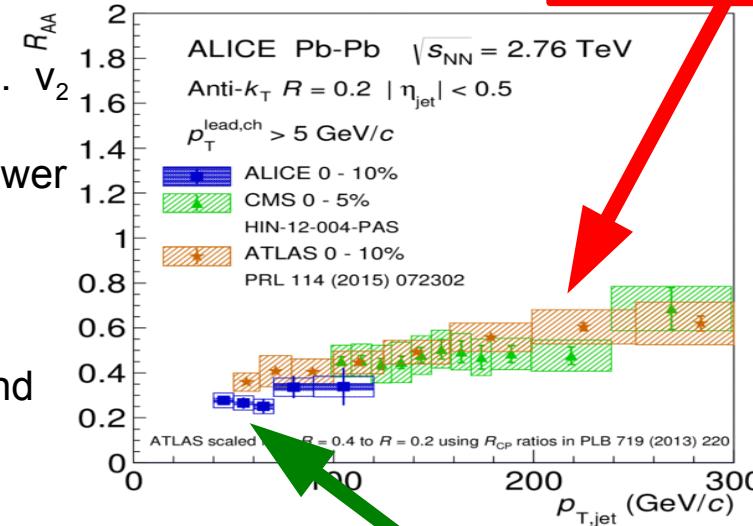
**Tension between ATLAS & ALICE/CMS**



## Background subtraction method:

- Iterative procedure
  - Calorimeter jets:** Reconstruct jets with  $R=0.2$ .  $v_2^{\text{AA}}$  modulated  $\langle \text{Bkgd} \rangle$  estimated by energy in calorimeters excluding jets with at least one tower with  $E_{\text{tower}} > \langle E_{\text{tower}} \rangle$
  - Track jets:** Use tracks with  $p_T > 4 \text{ GeV}/c$
  - Calorimeter jets from above with  $E > 25 \text{ GeV}$  and track jets with  $p_T > 10 \text{ GeV}/c$  used to estimate background again.
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Phys. Lett. B 719 (2013) 220-241

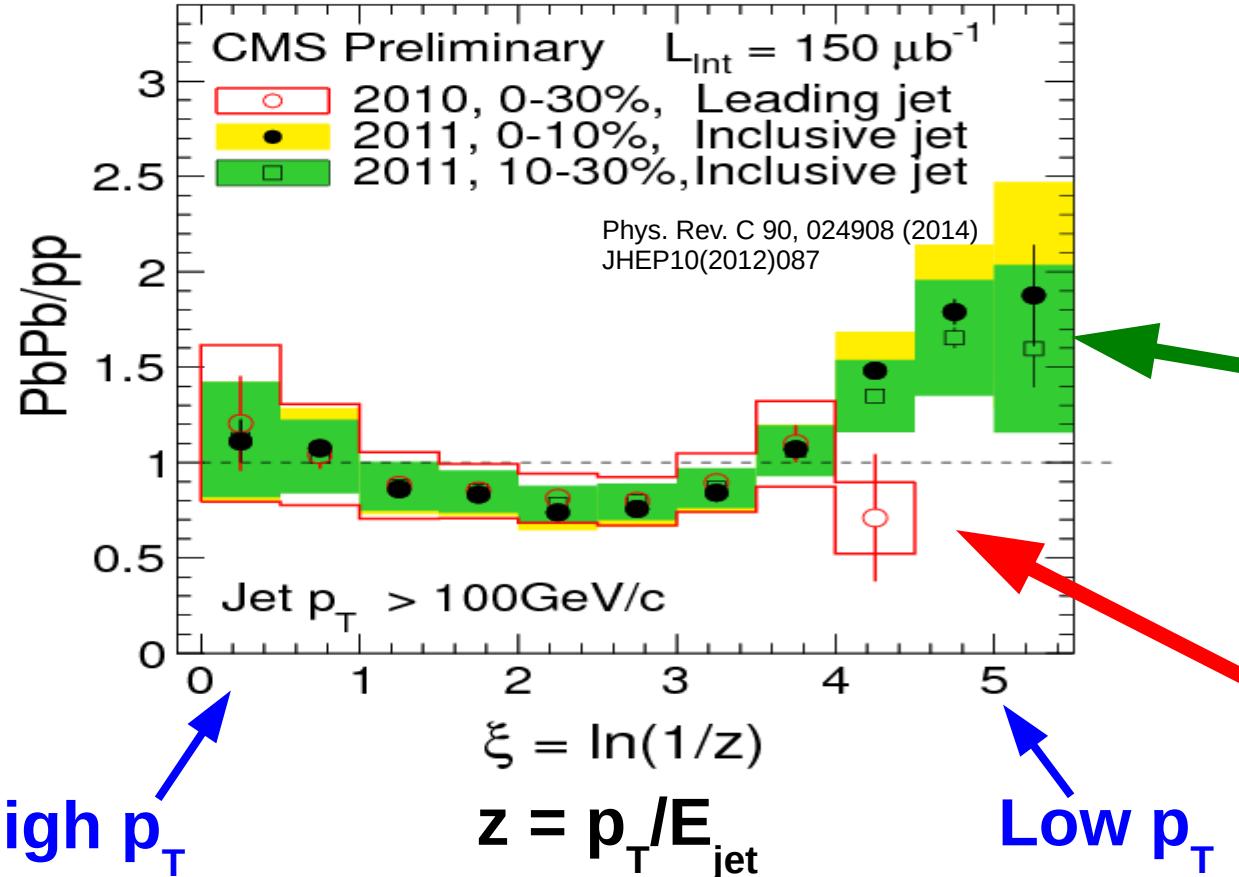


Constituent biases don't matter that much up here

But they do matter down here!



# What you see depends on where you look

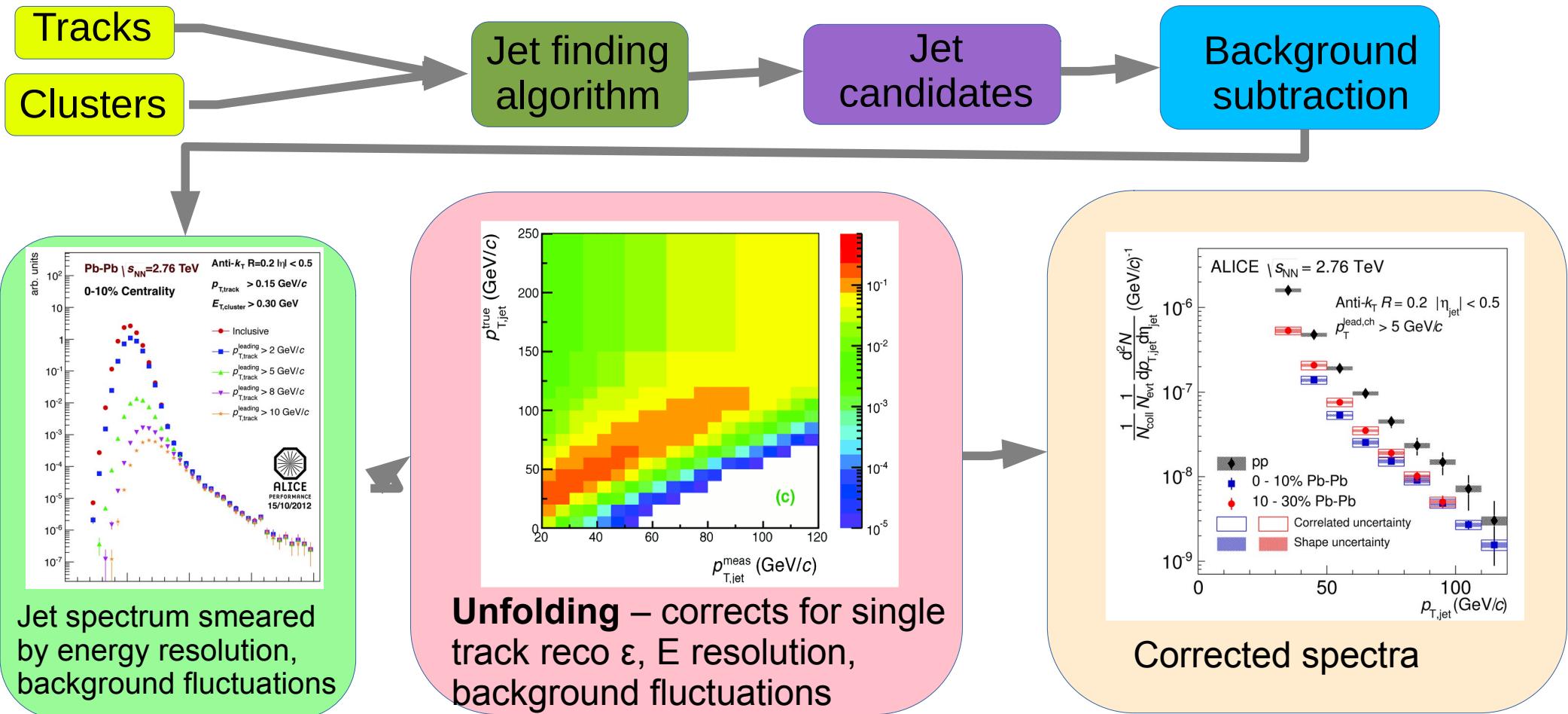


# Mini-summary

- Most studies do one or more of the following:
  - Explicitly apply a (non-purturbative) bias
  - *Implicitly* apply a (non-purturbative) bias
  - Focus on small R
  - Focus on high pT
- May also → survivor bias
- Background subtraction should be part of definition of algorithm

What are the dominant uncertainties?

# Analysis steps



# Unfolding

$$\vec{v} = R\vec{\mu} + \vec{\beta}$$

- $\vec{\mu}$  : the “true” histogram
- $\vec{v}$  : the actual data we measure
- $\vec{\beta}$  : background
- R : the response matrix

$$v_i = \sum_{j=1}^M (R_{ij}\mu_j) + \beta_i$$

# Simple Solution (Inversion)

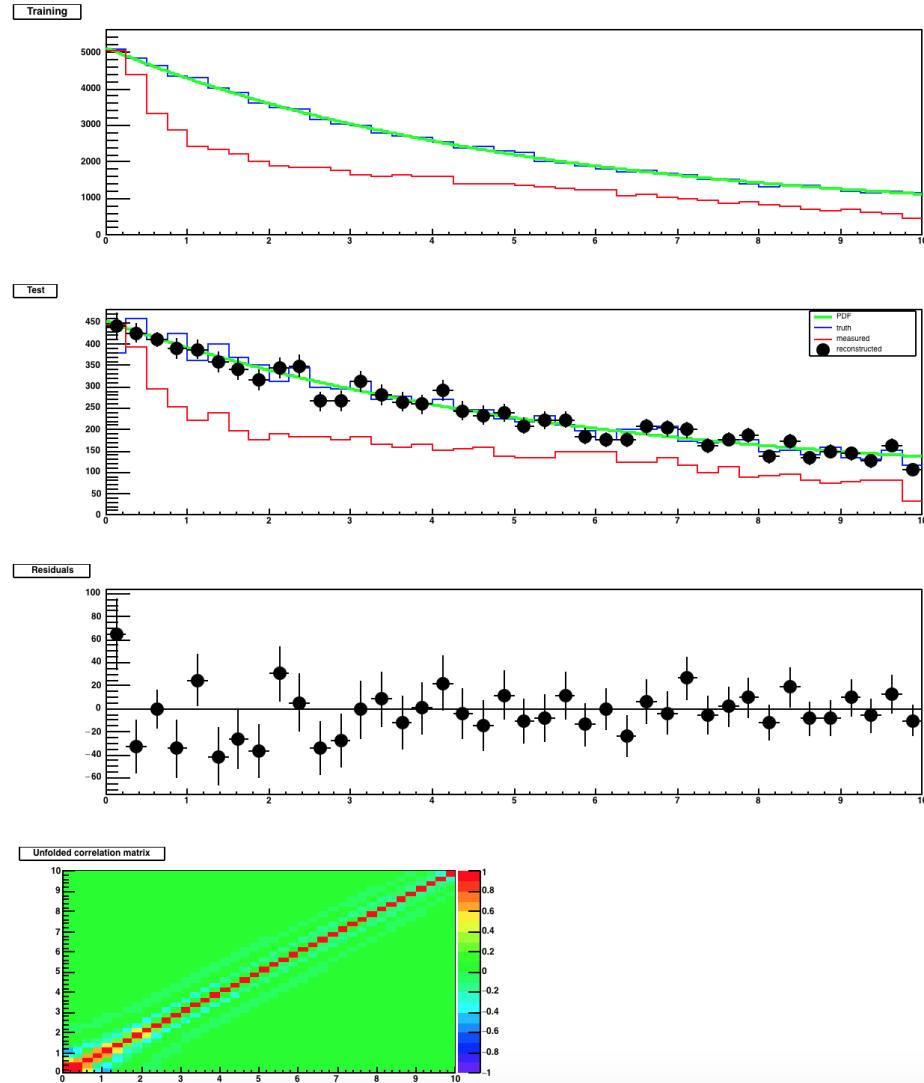
- Rearrange  $\vec{v} = R\vec{\mu} + \vec{\beta}$  to get  $\vec{\mu} = R^{-1}(\vec{v} - \vec{\beta})$
- Problem: we don't have  $\vec{v}$ , we have  $\vec{n}$ , the measured data, which is subject to statistical fluctuations.
- We assume  $n_i$  is the maximum likelihood estimator for  $v_i$ , then solve for the estimator  $\hat{\mu} = R^{-1}(\vec{n} - \vec{\beta})$ .
- $R^{-1}$  is obtained from  $R$  through simple matrix inversion

# Iterative Bayesian Method

- Using prior knowledge, start with an initial guess for the distribution of true histograms  $P^0(\hat{\mu})$
- Use Bayes' Theorem to invert the response matrix  $P(\hat{\mu}_i | v_j^{sig}) = \frac{P(v_j^{sig} | \hat{\mu}_i) P^0(\hat{\mu}_i)}{\sum_{l=1}^M P(v_j^{sig} | \hat{\mu}_l) P^0(\hat{\mu}_l)}$
- $\hat{\mu}_i = \frac{1}{\epsilon_i} \sum_{j=1}^N v_j^{sig} P(\hat{\mu}_i | v_j^{sig})$  where  $\epsilon_i$  is the detector efficiency
- Plug in the newly obtained  $P(\hat{\mu}_i | v_j^{sig})$  and  $\hat{\mu}_i$  as new priors, then repeat
- Terminate before the wildly oscillating true inverse is reached (usually  $\sim 4$  iterations) to preserve some smoothness

# RooUnfold-Bayes

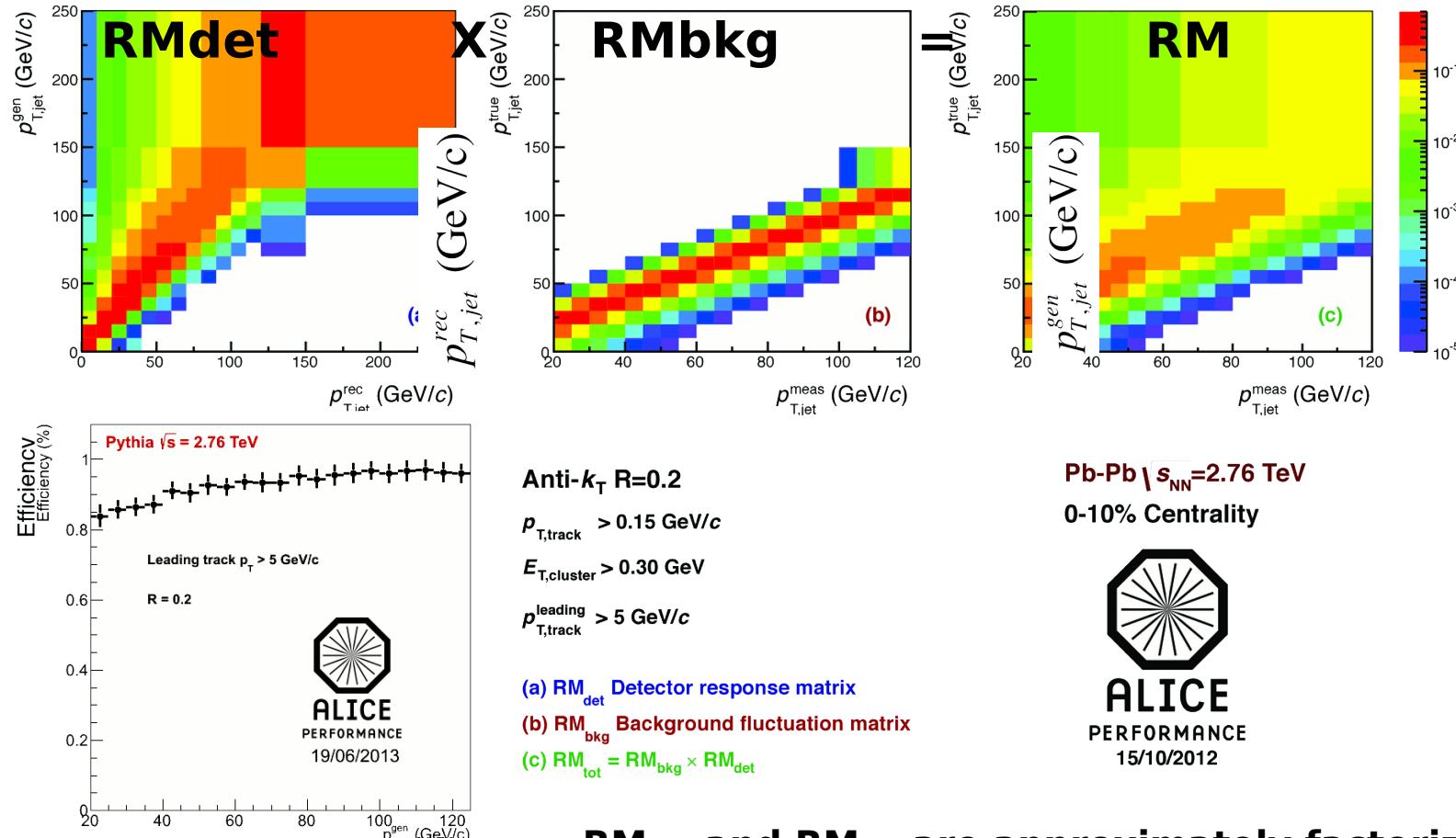
- RooUnfoldTest.cxx
- method = Bayes
- Exponential training and testing



# About unfolding...

- d'Agostini (author of Bayesian unfolding algorithm) says you should avoid it if you can
- Necessary when experimental resolution is poor
  - Ex: Single particle spectra  $\frac{\sigma_p}{p} \ll w_{bin}$  → unfolding unnecessary
  - Ex: Jet spectra  $\frac{\sigma_p}{p} \approx w_{bin}$  → unfolding necessary
- Algorithm assumes response matrix is correct
  - Matching reconstructed and simulated jets is non-trivial!
- Corrects for multiple experimental effects simultaneously
  - Difficult to disentangle different effects
  - Leads to non-trivial uncertainty correlations between data points due to algorithm
  - May not handle systematic correlations between effects correctly

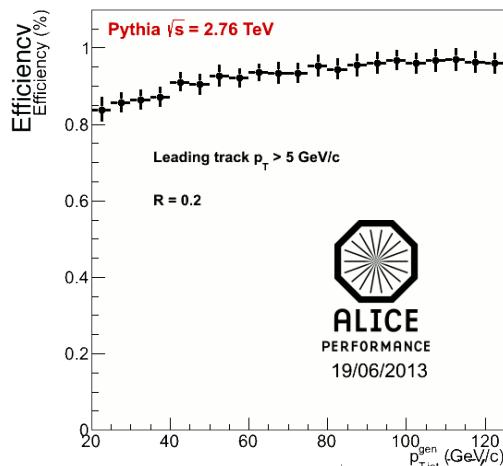
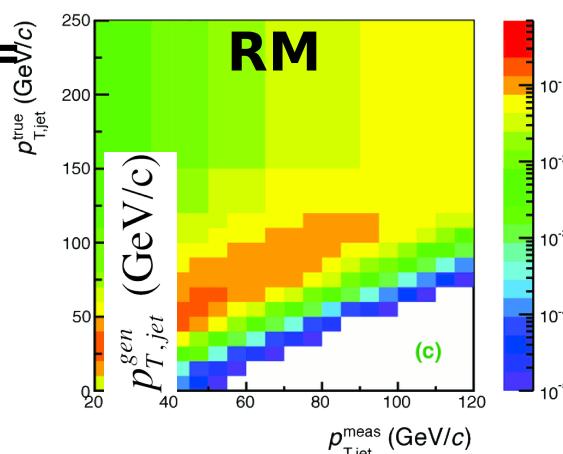
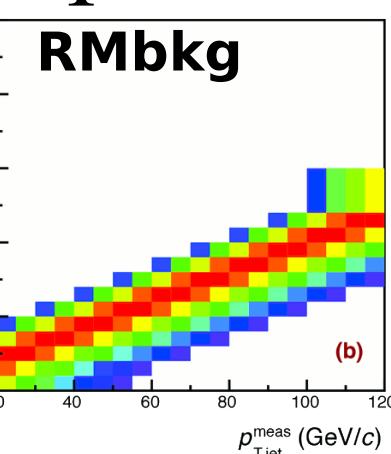
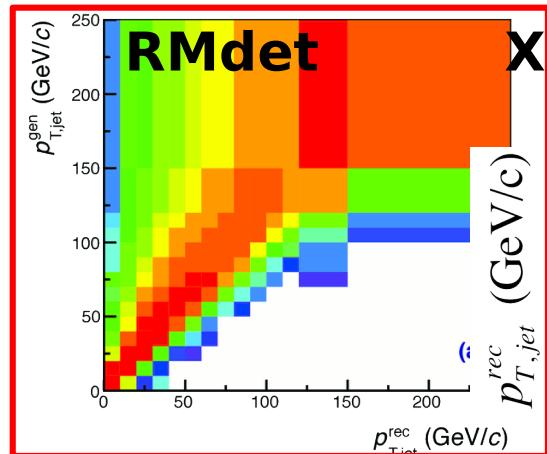
# Jets in ALICE: Response Matrix Construction



**RM<sub>bkg</sub> and RM<sub>det</sub> are approximately factorizable**

# Jets in ALICE: Response Matrix Construction

**DETECTOR EFFECT**



Anti- $k_T$   $R=0.2$

$p_{T,\text{track}} > 0.15 \text{ GeV}/c$

$E_{T,\text{cluster}} > 0.30 \text{ GeV}$

$p_{T,\text{track}}^{\text{leading}} > 5 \text{ GeV}/c$

(a)  $\text{RM}_{\text{det}}$  Detector response matrix

(b)  $\text{RM}_{\text{bkg}}$  Background fluctuation matrix

(c)  $\text{RM}_{\text{tot}} = \text{RM}_{\text{bkg}} \times \text{RM}_{\text{det}}$

Pb-Pb  $\sqrt{s_{NN}}=2.76 \text{ TeV}$

0-10% Centrality

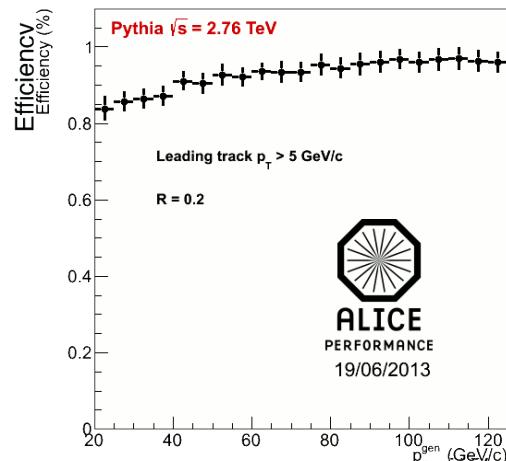
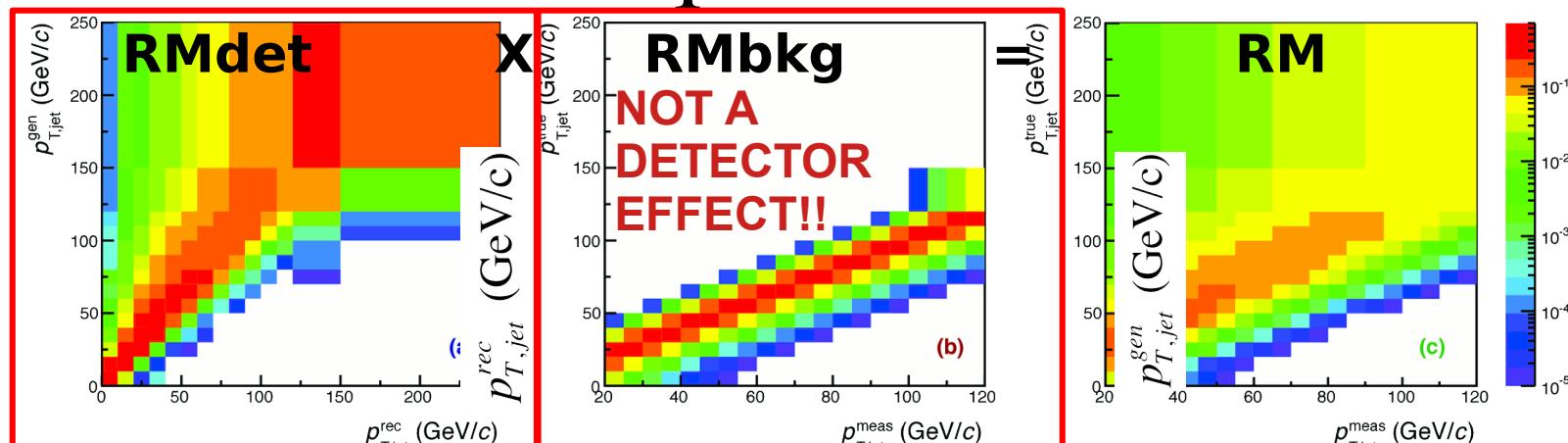


**ALICE**  
PERFORMANCE  
15/10/2012

**$\text{RM}_{\text{bkg}}$  and  $\text{RM}_{\text{det}}$  are approximately factorizable**

# Jets in ALICE: Response Matrix Construction

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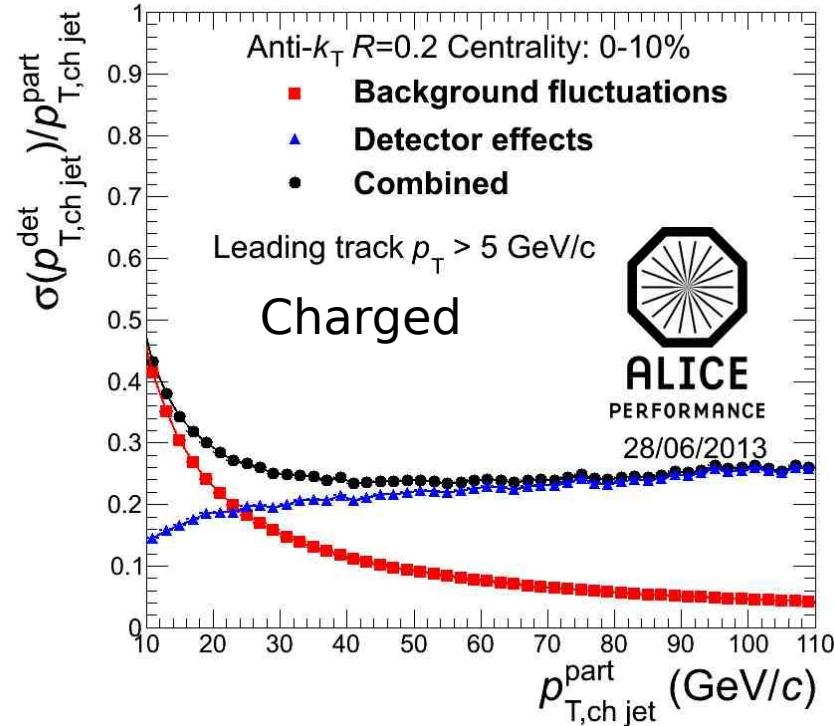
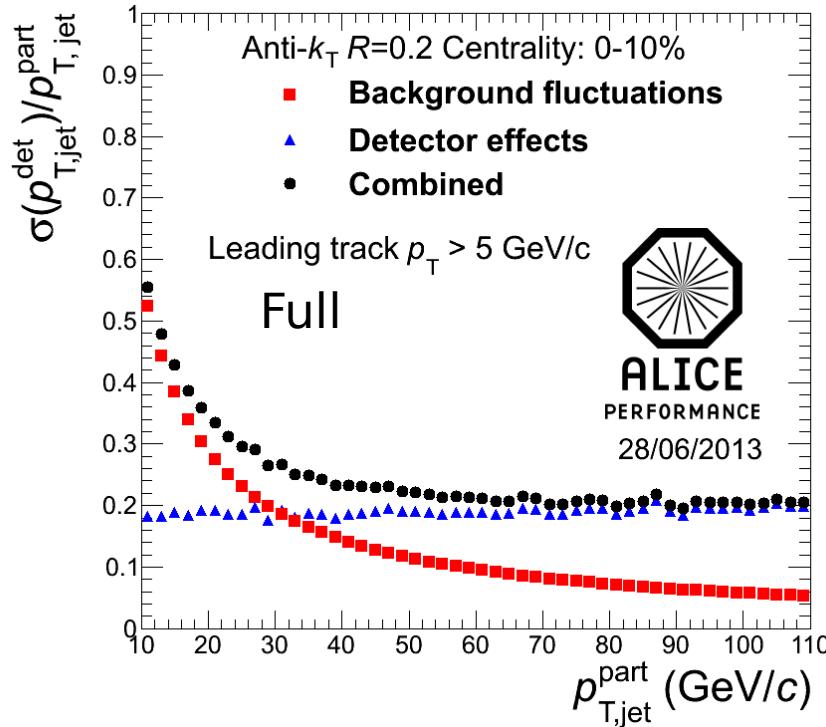
ALICE  
PERFORMANCE  
15/10/2012

**RM<sub>bkg</sub> and RM<sub>det</sub> are approximately factorizable**

# Response matrix includes assumptions about

- Detector response
  - Including particle composition of jets!
- Fragmentation and hadronization
  - How does hadronization influence the width of your jet?
- Background and/or background fluctuations
- How you match reconstructed (“detector level”) and true (“particle level”) jets

# Jet Momentum Resolution



- Jet resolution

- Dominated by background fluctuations at low momentum
- Dominated by detector effects at high momentum

# Mini-summary

- Jet energy resolution is fundamentally large
  - Measuring multiple correlated particles!
  - Be skeptical of jet measurements with <10% uncertainties
- Unfolding is complicated, often unstable, and hard
- Construction of response matrix includes several assumptions

# Jets in A+A collisions: How to compare to models

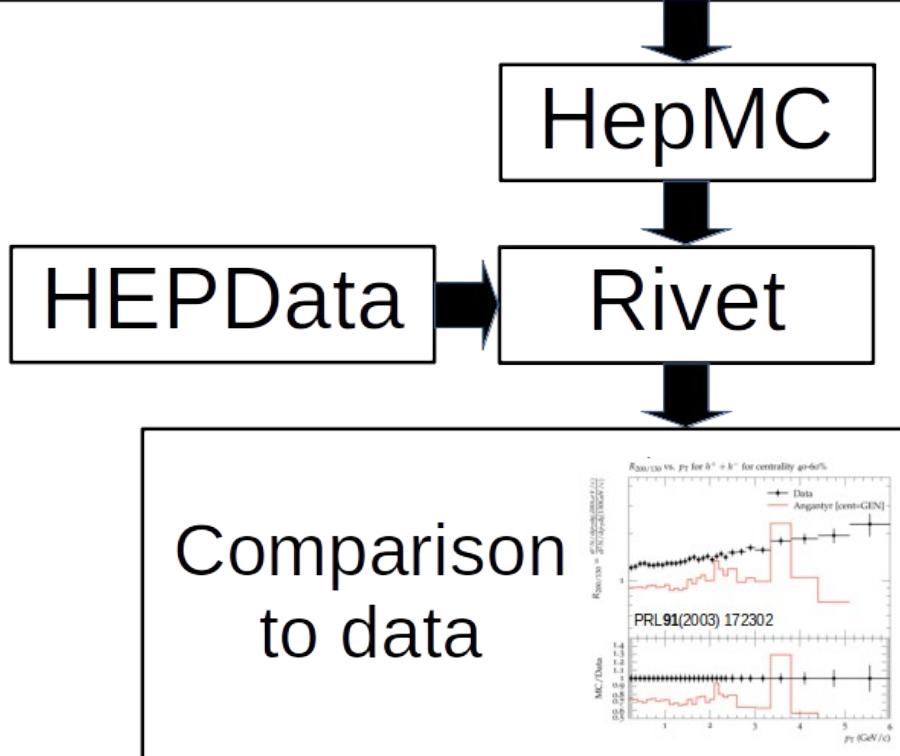
**Snowmass Accord:** Apply the same algorithm to data and your model. Then the measurement and the calculation are the same.

**Rivet:** Apply the same algorithm to data and your model. Then the measurement and the calculation are the same.

# What is Rivet?



# Monte Carlo Model



# Why use Rivet?

- Facilitates comparisons between Monte Carlos and data
- It's not that hard
- It preserves analysis details

# Rivetizing Heavy Ion Collisions at RHIC 2020

November 30, 2020 to December 4, 2020

Online

US/Eastern timezone

- Overview
- Remote connection
- Announcement
- Registration
- Participant List
- Organizing Committee
- Code of Conduct
- HEPData@RHIC

Support

 [christine.nattrass@utk.edu](mailto:christine.nattrass@utk.edu)

 [antonio.silva@cern.ch](mailto:antonio.silva@cern.ch)

Workshop to implement RHIC analyses in Rivet



**Starts** Nov 30, 2020, 9:00 AM

**Ends** Dec 4, 2020, 12:00 PM

US/Eastern



Online



[Antonio Carlos Oliveira da Silva](#)  
Christine Nattrass



There are no materials yet.



**Registration**

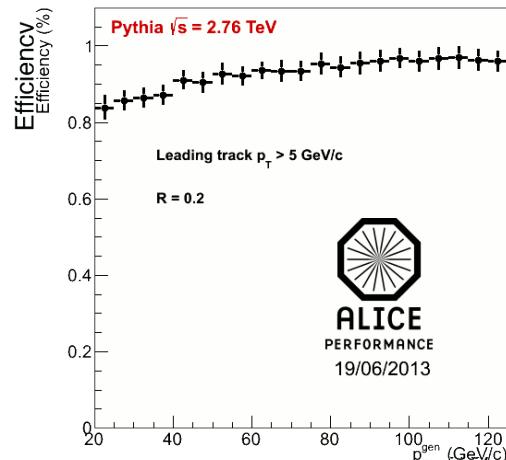
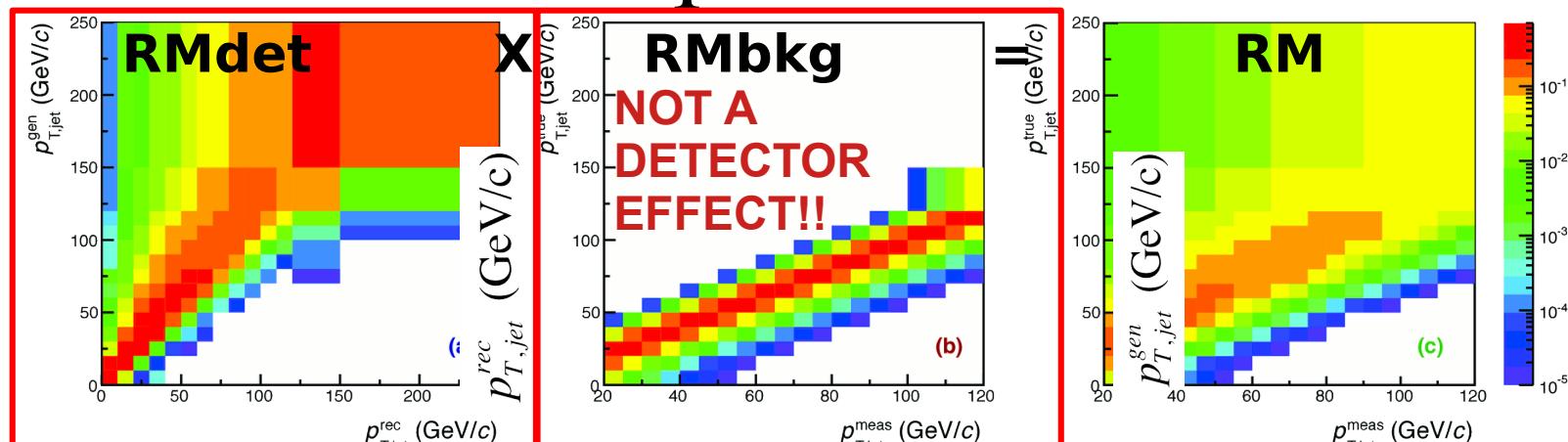
Registration for this event is currently open.

[Register now ➔](#)



# Jets in ALICE: Response Matrix Construction

**DETECTOR EFFECT**



Anti- $k_T$   $R=0.2$

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(a) RM<sub>det</sub> Detector response matrix

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(c) RM<sub>tot</sub> = RM<sub>bkg</sub> × RM<sub>det</sub>

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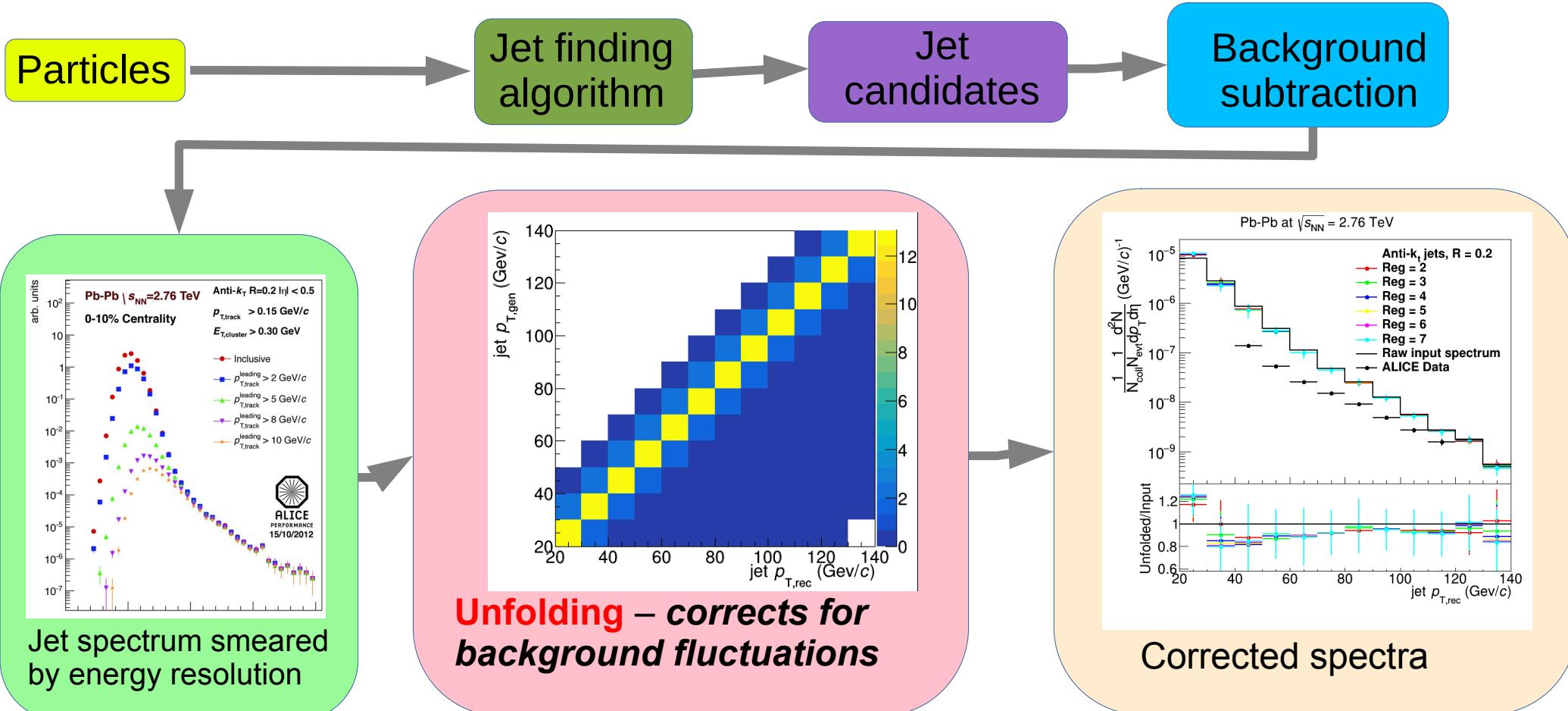
0-10% Centrality

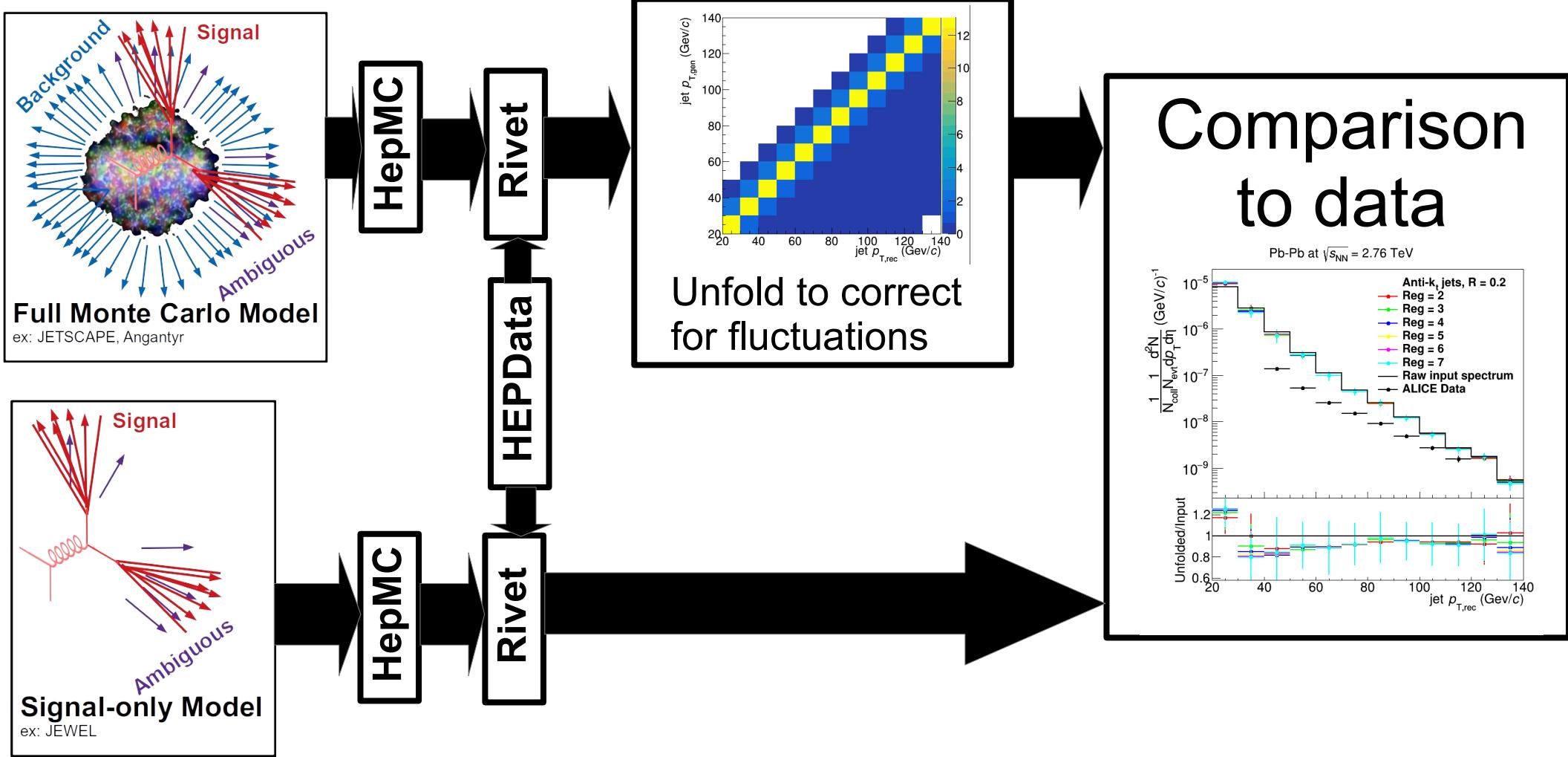


ALICE  
PERFORMANCE  
15/10/2012

**RM<sub>bkg</sub> and RM<sub>det</sub> are approximately factorizable**

# Analysis steps: Full Monte Carlo



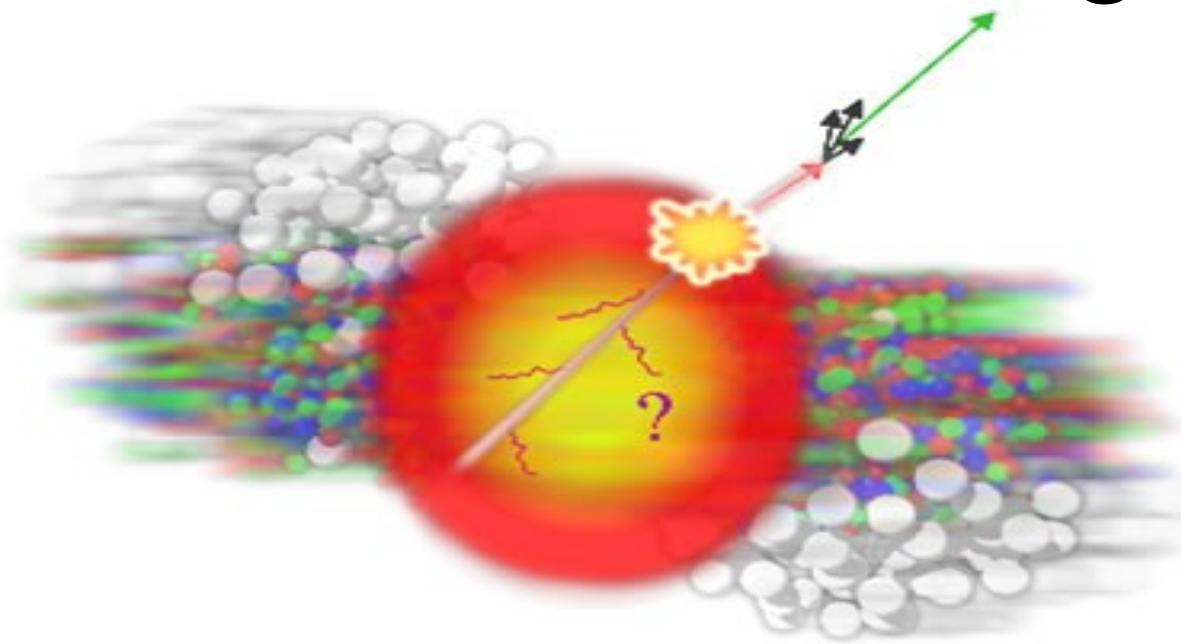


# Mini-summary

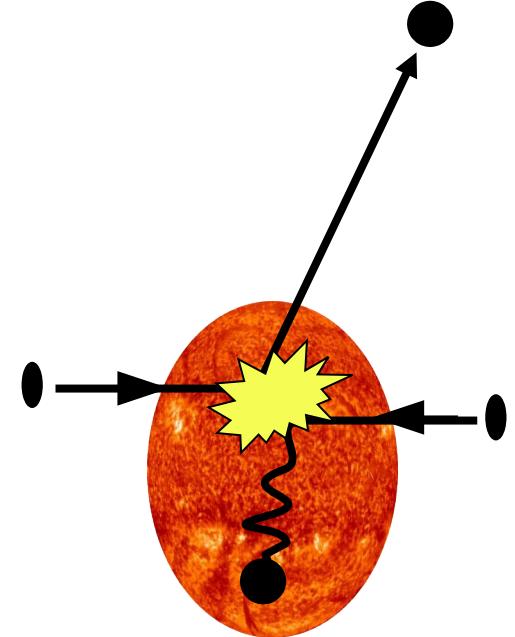
- Experimental techniques can bias measurement in subtle ways
  - Background subtraction
  - Kinematic cuts
  - Choice of jet finder, R
  - Centrality determination
  - Technique for finding reaction plane
- Unclear how these influence the measurement
- Safest to do the same analysis on data and model
  - But unfolding is necessary in a full Monte Carlo model!

# A skeptic's guide to jets

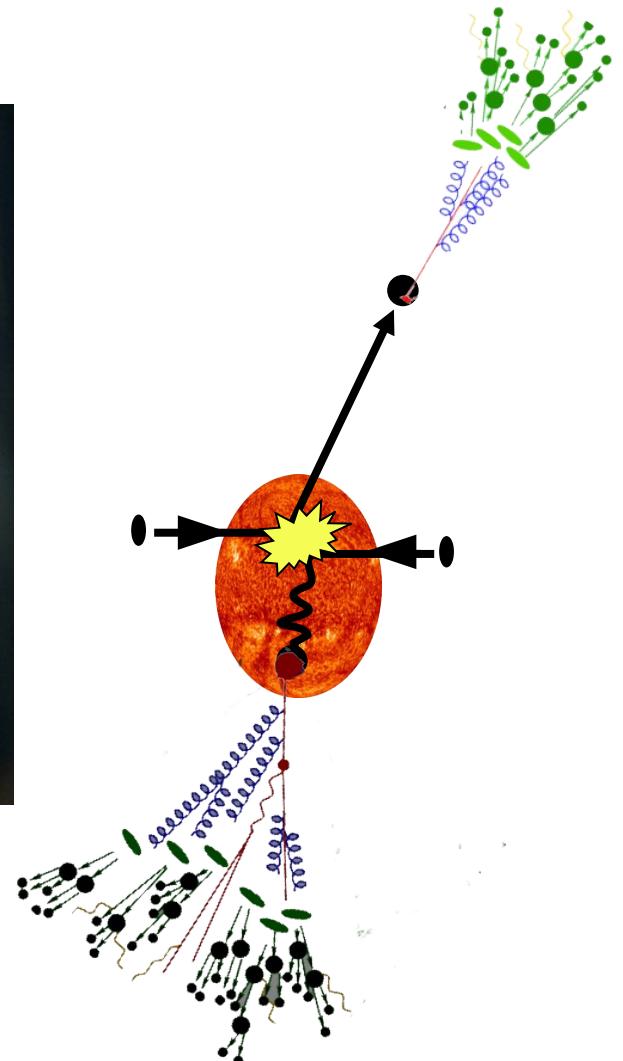
## Part 2: Where we are going



Christine Nattrass  
University of Tennessee, Knoxville



There is no partionic energy loss.



There is only partionic energy  
redistribution.

# What is jet (sub)structure?

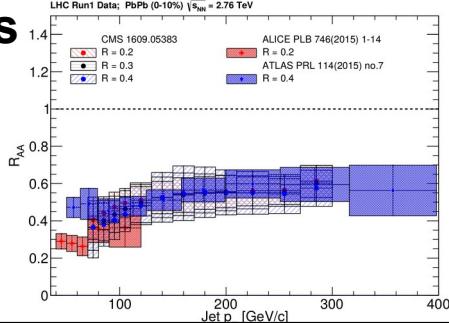
- A Whatever I am measuring!
- B Any new jet observable
- C Any observable which measures the structure of jets.
- D A cool buzzword
- E I don't know but it sounds cool and gets me talks/grants

# Types of observables

## I. Minimally sensitive to structure

### Observables

- (Jet)  $R_{AA}$
- $A_j$
- $I_{AA}$
- (Jet)  $v_2$



Jet properties:  
• E

Higher precision

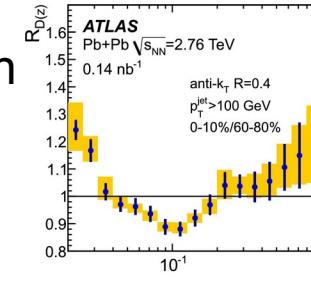
Higher/different sensitivity?

Jets not required

## II. Sensitive to <structure> of <jets>

### Observables

- Fragmentation functions
- Jet shapes
- Correlations
- ...



Jet properties:  
• E  
• Const.  $p_T$ ,  $\phi, \eta$

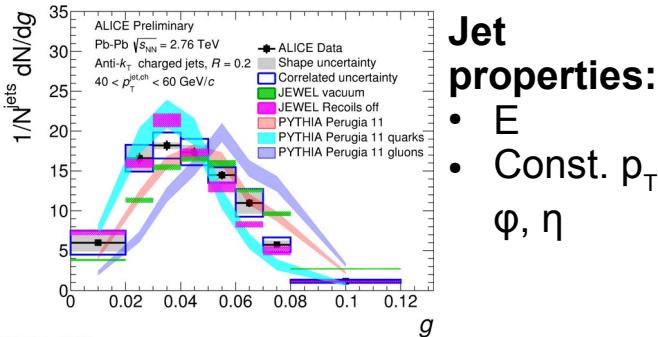
Average background subtraction OK

Need new background subtraction technique

## III. Sensitive to distribution of structures

### Observables

- Girth
- Dispersion
- $p_T D$
- Jet mass
- ...

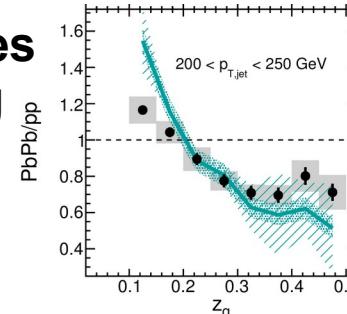


Jet properties:  
• E  
• Const.  $p_T$ ,  $\phi, \eta$

## IV. Sensitive to parton shower structure

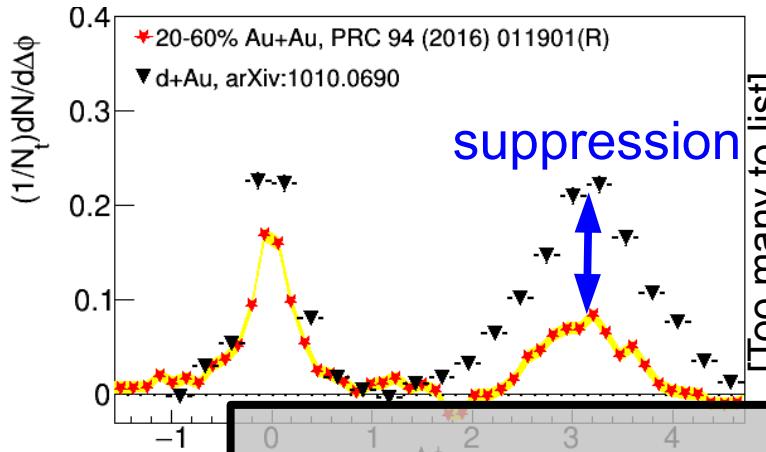
### Observables

- Grooming
- $N_{\text{subjettiness}}$
- ...

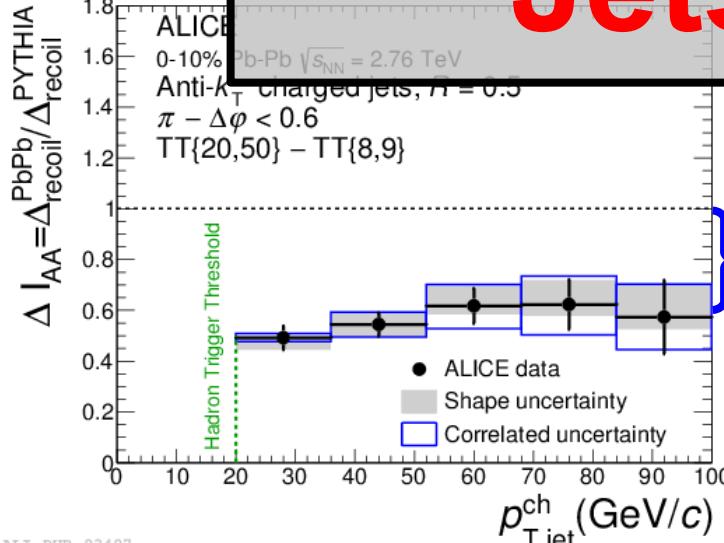


Jet properties:  
• E  
• Const.  $p_T$ ,  $\phi, \eta$   
• Multi-const. correlations

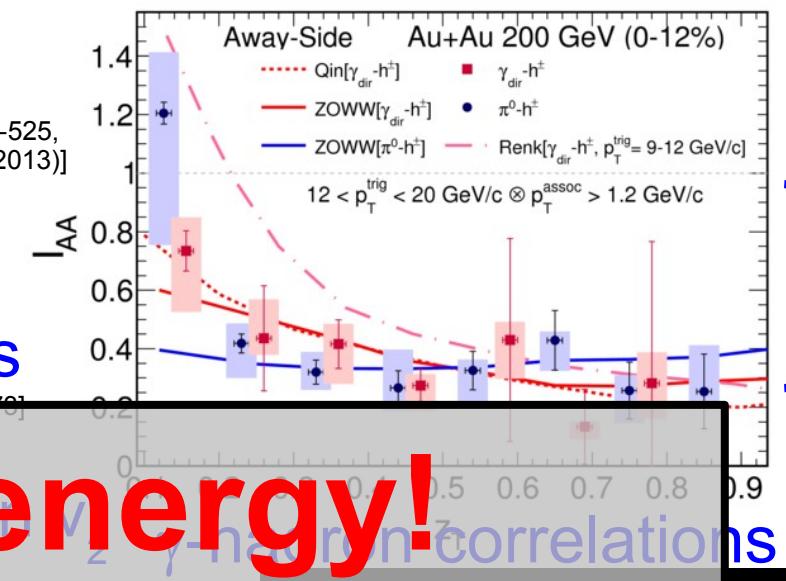
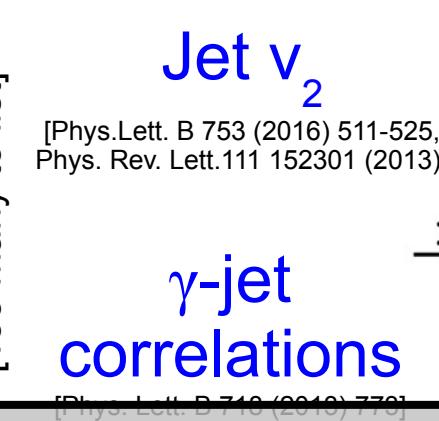
# Type I: Energy loss



Di-hadron correlations



Hadron-jet correlations



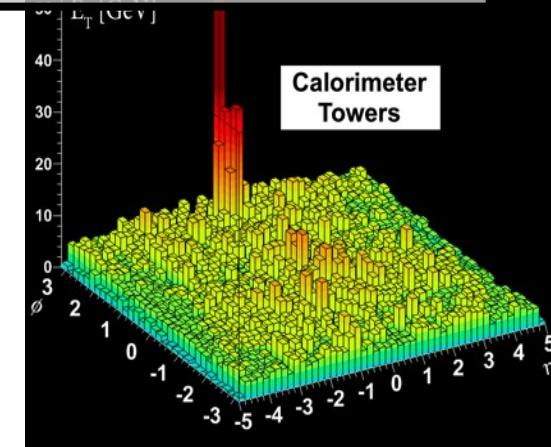
γ-jet correlations

[Phys.Rev.C80:024908,2009,  
 Phys.Rev.D82:072001,2010,  
 Phys.Rev.C82:034909,2010  
 Physics Letters B 760 (2016)]

Au+Au  $\sqrt{s_{NN}} = 200$  GeV  
 $\hat{q} = 1.2 \pm 0.3$  GeV $^2$   
 Pb+Pb  $\sqrt{s_{NN}} = 2.76$  TeV  
 $\hat{q} = 1.9 \pm 0.7$  GeV $^2$

[JHEP 09 (2015) 170,  
 Phys. Rev. C 96, 024905 (2017)]

[Phys. Rev. C 90, 014909 (2014)]

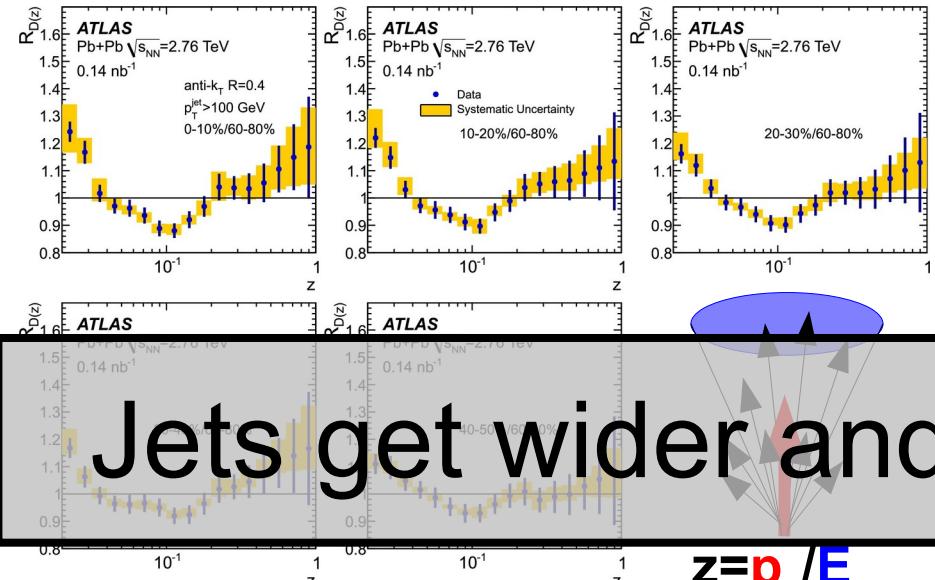


Dijet asymmetry

[Phys. Rev. C84:024906,2011,  
 Phys. Lett. B 712 (2012) 176,  
 Phys. Rev. Lett. 105:252303,2010,  
 Phys. Rev. Lett. 119, 062301 (2017)]

## Type II: Fragmentation

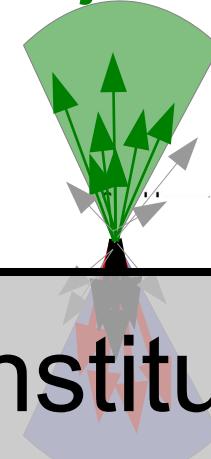
# Fragmentation functions with jets



Jets get wider and constituents get softer

$$z = p_T / E_\gamma$$

Leading jet



Subleading jet



## Di-hadron correlations

[Lots of papers]

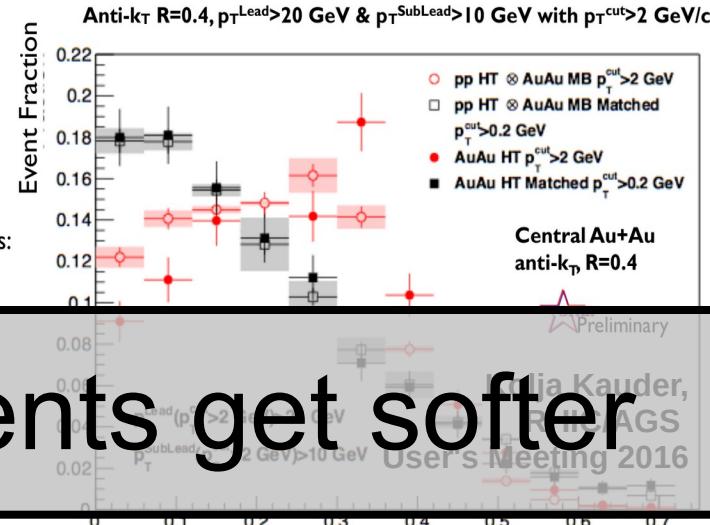
### Jet shapes

[arXiv:1708.09429,  
arXiv:1512.07882,  
arXiv:1704.03046]

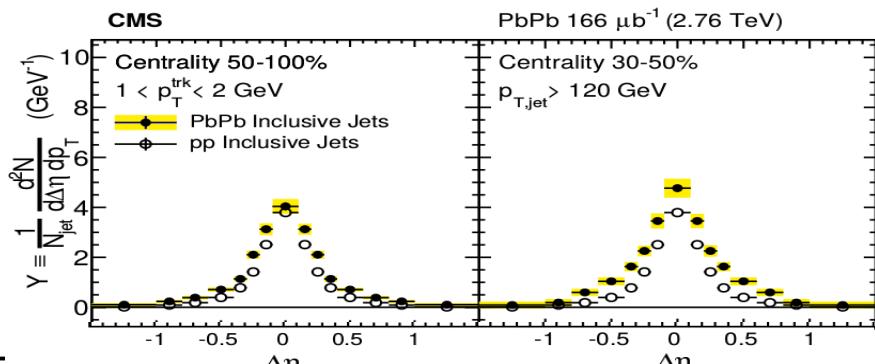
## Jet-hadron correlations

# Di-jet asymmetry

arXiv:1609.03878

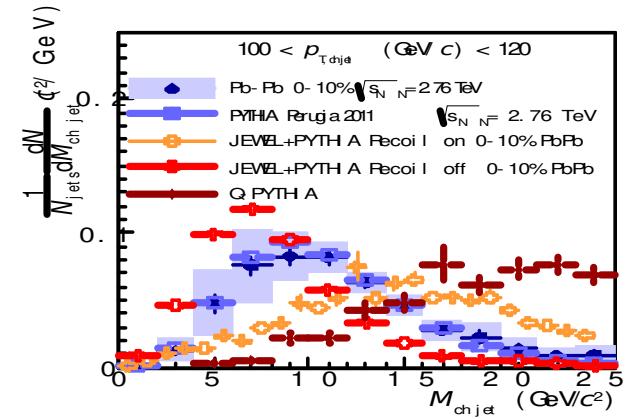
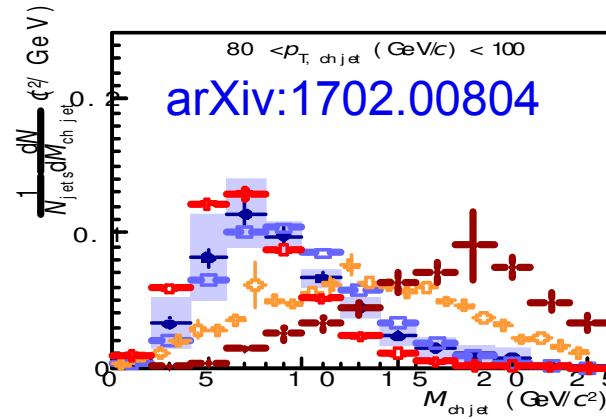
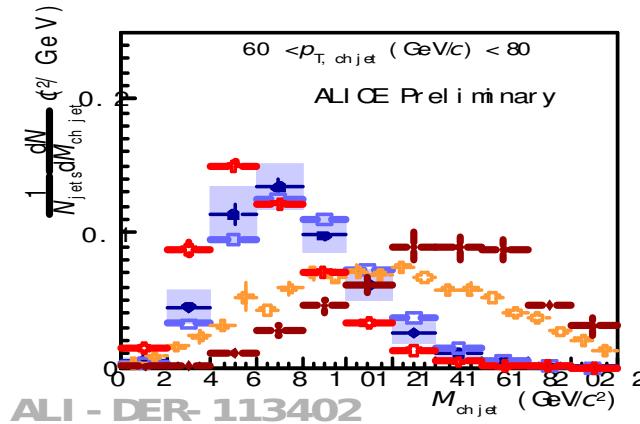


$$A_j = \frac{p_T^{\text{leading}} - p_T^{\text{subleading}}}{p_T^{\text{leading}} + p_T^{\text{subleading}}}$$



## Type III: Distribution of properties

# Jet mass

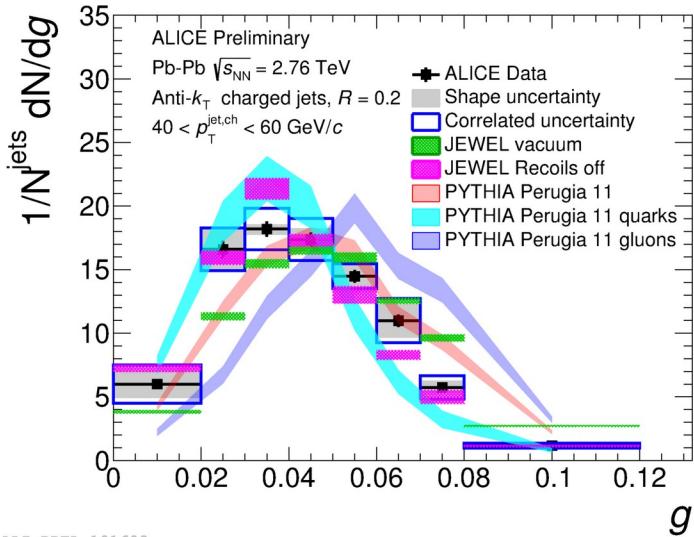


$$M = \sqrt{p^2 - p_T^2 - p_z^2}$$

$$p = \sum_{i=1}^n p_{Ti} \cosh \eta_i. \quad p_z = \sum_{i=1}^n p_{Ti} \sinh \eta_i$$

- Quenching models (**JEWEL**, **Q-PYTHIA**) show a larger mass than pp-like **PYTHIA** jets
- Pb-Pb measurement can discriminate among these predictions

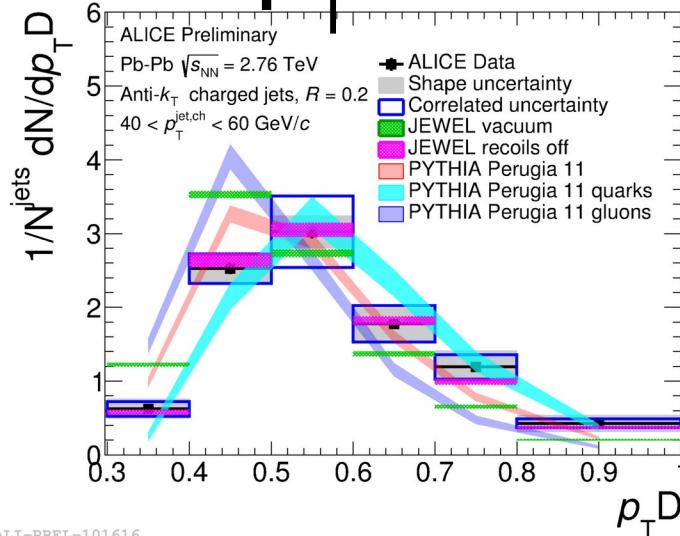
# Girth g



ALI-PREL-101608

$$g = \sum_{i \in \text{jet}} \frac{p_T^i}{p_T^{\text{jet}}} r_i$$

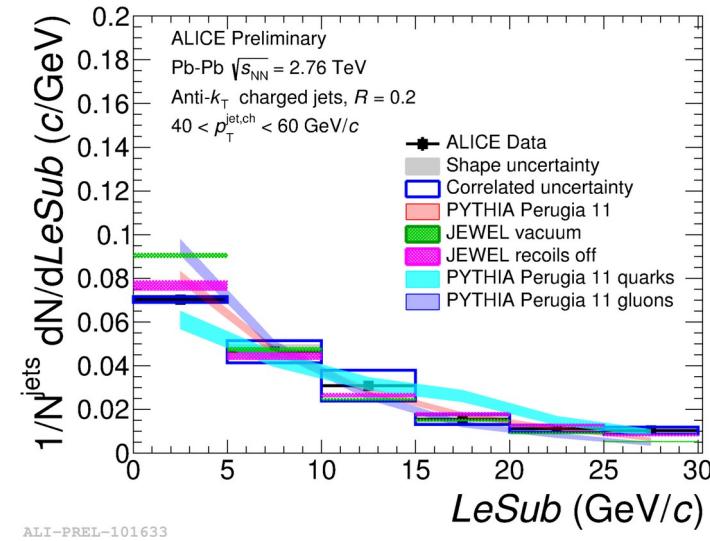
# Dispersion $p_T D$



ALI-PREL-101616

$$p_T D = \frac{\sqrt{\sum_{i \in \text{jet}} (p_T^i)^2}}{\sum_{i \in \text{jet}} p_T^i}$$

# LeSub



ALI-PREL-101633

$$\text{LeSub} = p_T^{\text{leading}} - p_T^{\text{subleading}}$$

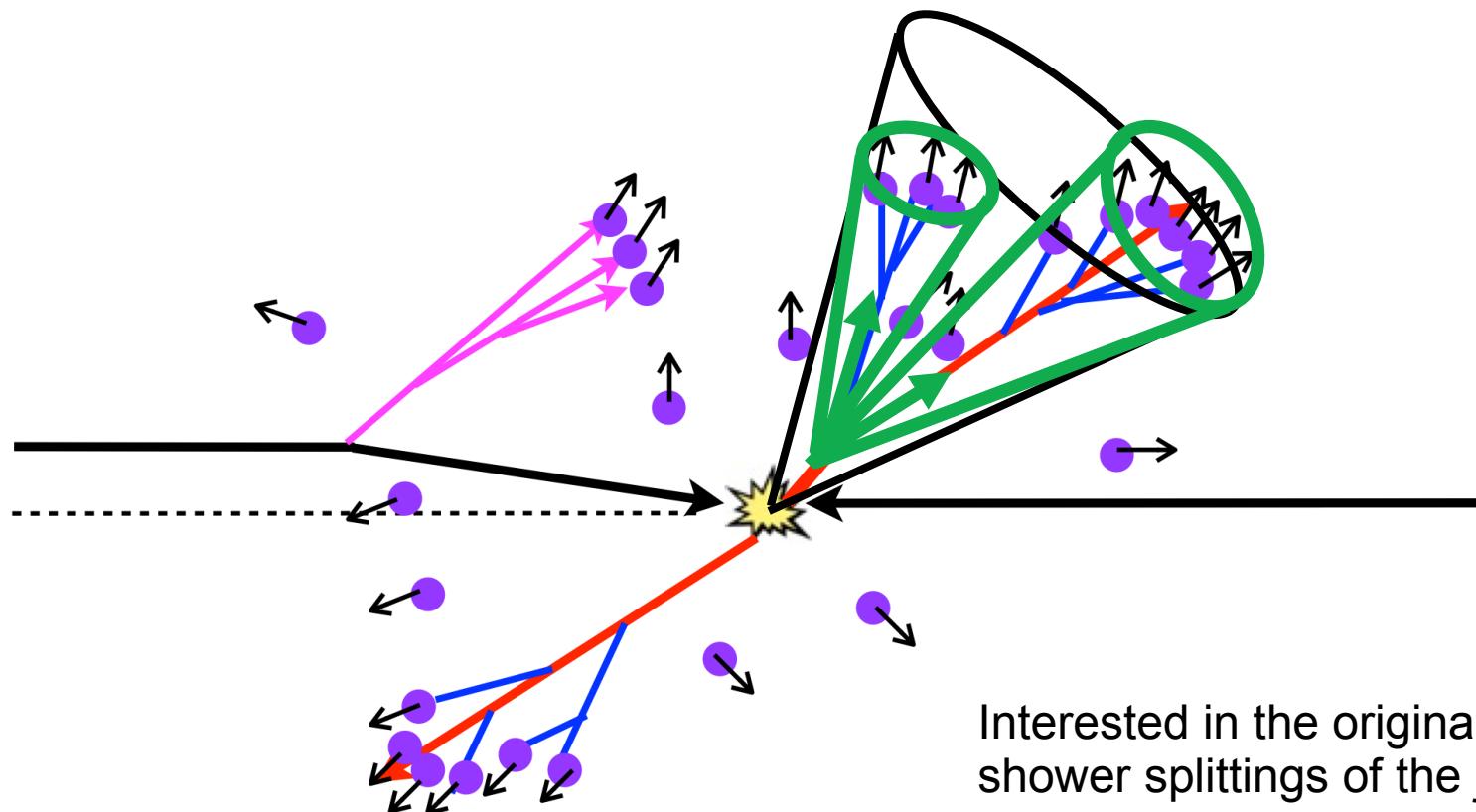
Jets are slightly more collimated than in pp      Agrees with PYTHIA

## Type IV: Declustering

**Note: These slides are from Laura Havener**

\*A selection. Don't be offended if I skip your favorite.

# New tool: jet splittings

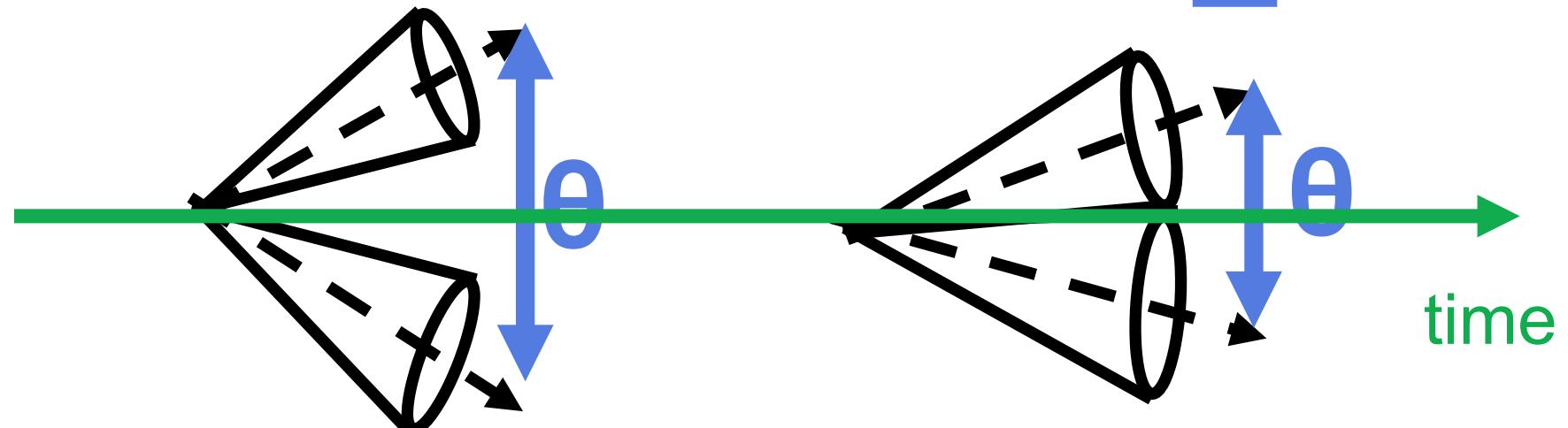


Interested in the original parton  
shower splittings of the jet  
Which form subjets inside the jet!

# Jet splittings: in vacuum

Vacuum jets splittings form at different times

$$t_f^{\text{vac}} = \frac{1}{\theta^2 \omega}$$

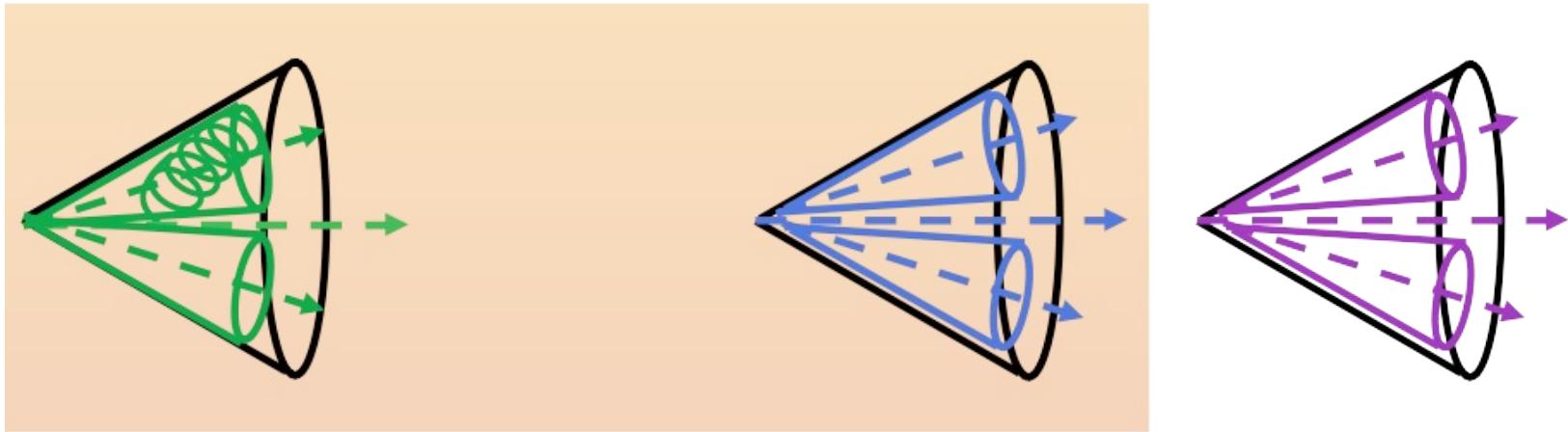


Wider jets form earlier and narrower jets form later

# Jet splittings: in medium

Vacuum splittings *in/out* of the medium

$$t_f^{\text{vac}} = \frac{1}{\theta^2 \omega}$$



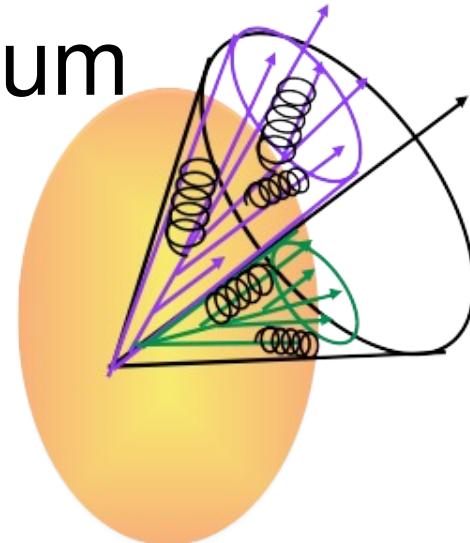
Medium-induced splittings from *gluon radiation*

$$t_g^{\text{med}} = \sqrt{\frac{\omega}{\hat{q}}}$$

# Jet splittings: in medium

Coherence: subjets  
*unresolved* and jet loses energy  
as a whole

Decoherence: medium  
*resolves* the subjets resulting in a  
stronger e-loss

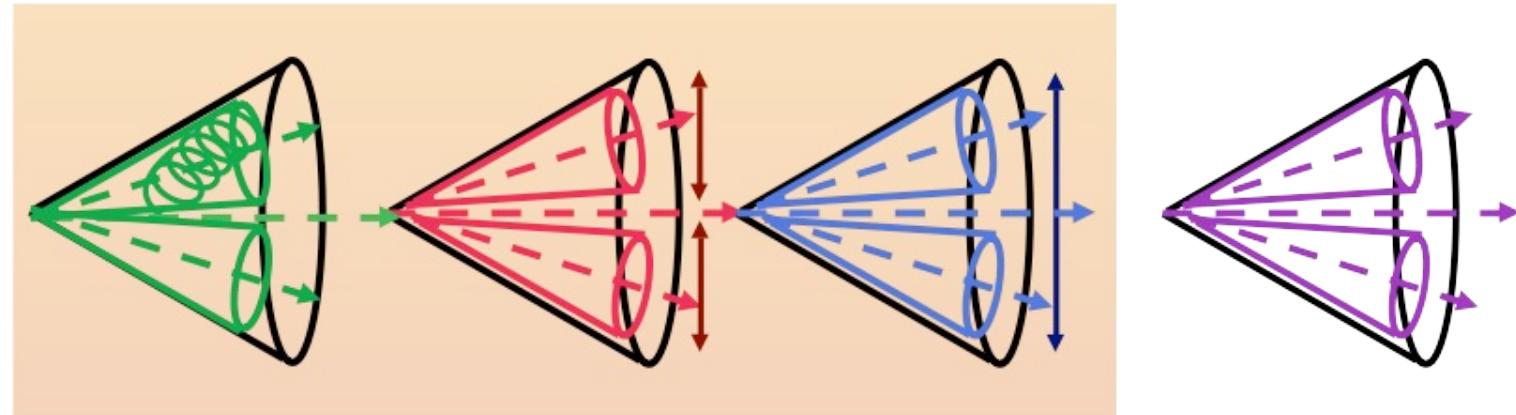


Medium-induced  
splittings

Vacuum splittings  
inside medium,  
resolved

Vacuum splittings  
inside medium,  
unresolved

Vacuum splittings  
outside medium

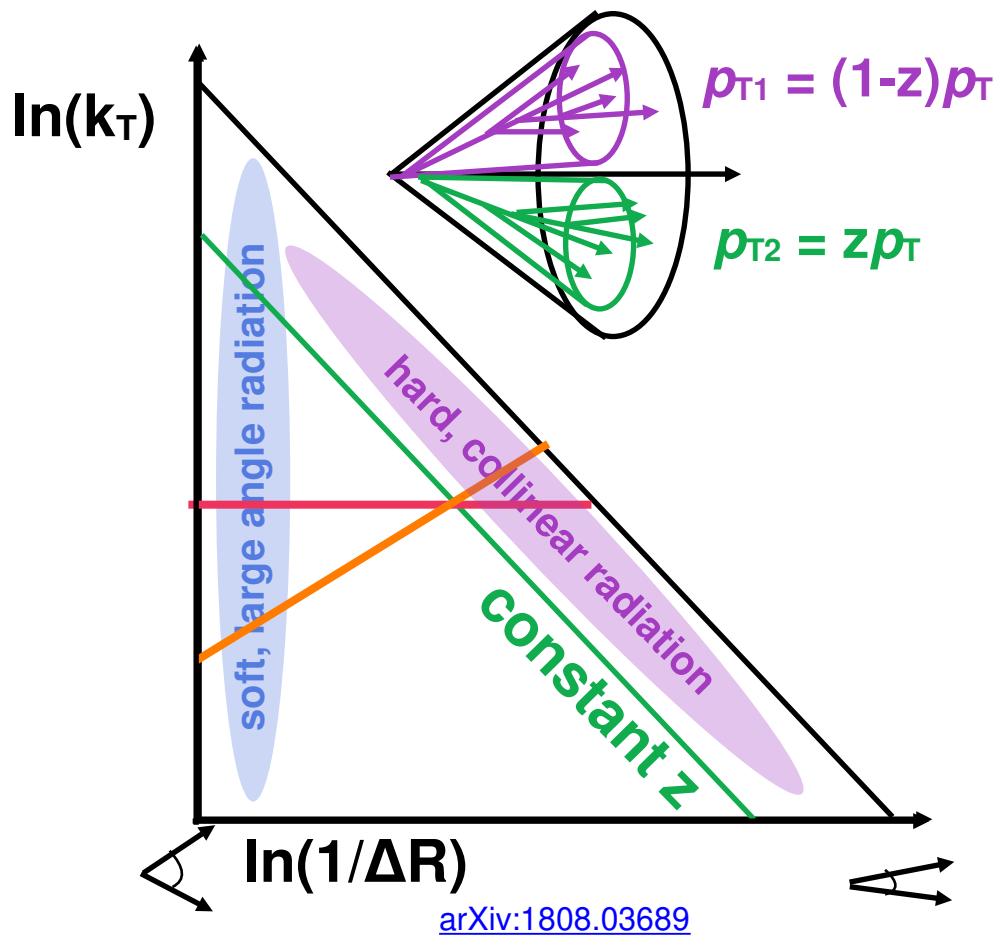


# Exploring the Lund Plane: in vacuum

- Lund Diagram\*: phase space of jet splitting
  - \*Z. Phys. C43 (1989)
  - JHEP 12 (2018)
- $\log(k_T) > 0$  separates perturbative from non-perturbative regime
- Formation time: how long until the splitting occurred

$$t_f = \frac{1}{(1-z)k_T \Delta R}$$

Y. L. Dokshitzer, et.al.

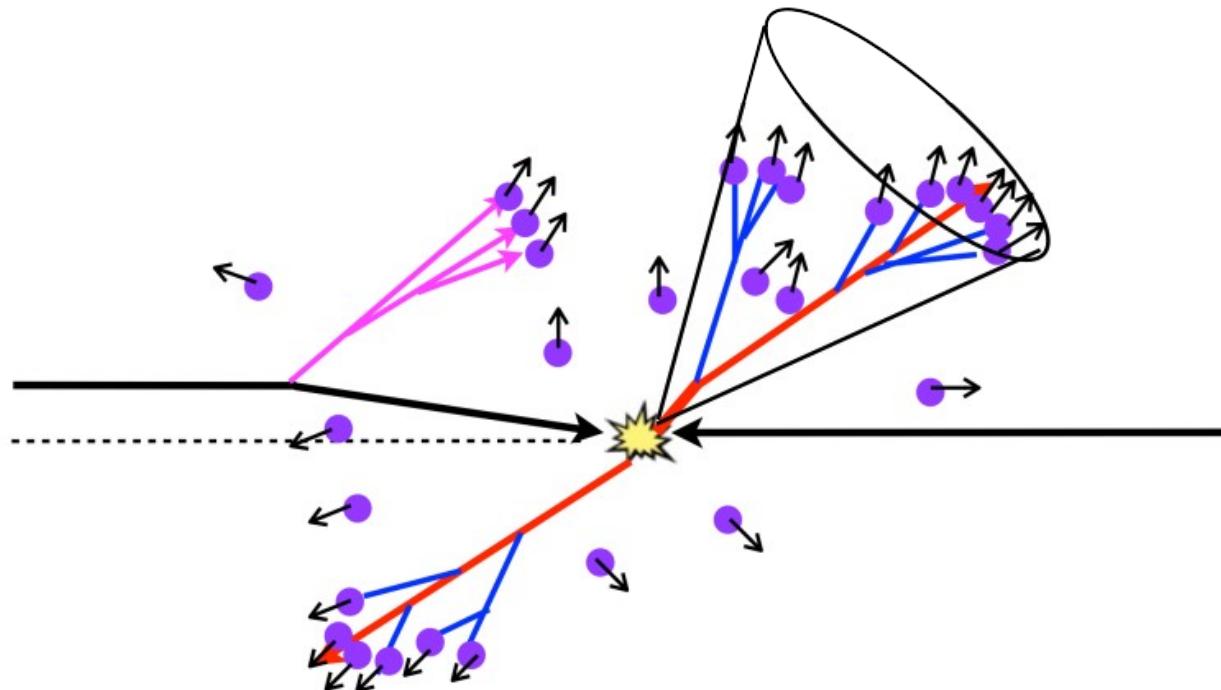


arXiv:1808.03689

# Soft drop grooming

- Reconstruct anti- $k_T$   $R=0.4$  charged jets with jet-by-jet constituent background subtraction\*

\*JHEP 06 (2014) 092



# Soft drop grooming

- Reconstruct anti- $k_T$   $R=0.4$  charged jets with *jet-by-jet constituent background subtraction*\*  
\*JHEP 06 (2014) 092

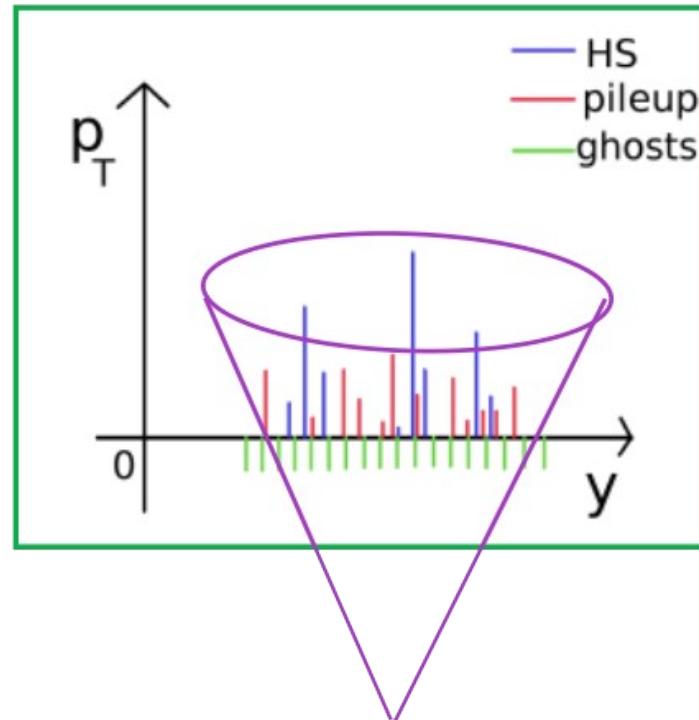
Remove from each constituent inside the jet instead of from the whole jet

Jet-by-jet:

$$p_T^{\text{jet,corr}} = p_T^{\text{jet}} - \rho A$$

Track-by-track (i) in jet:

$$p_T^{i,\text{corr}} = p_T^i - \rho A$$



# Groomed variables

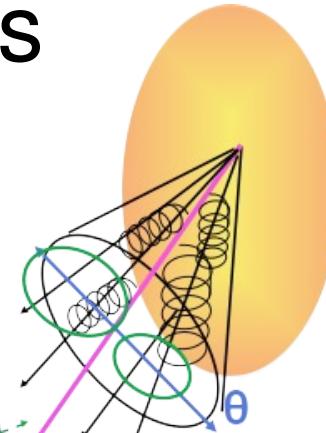
- Soft drop grooming variables probe jet splitting



$z_g$ : shared momentum

fraction between two hardest  
subjets in parton shower

$$z_g = \frac{\min(p_{Ti}, p_{Tj})}{p_{Ti} + p_{Tj}}$$



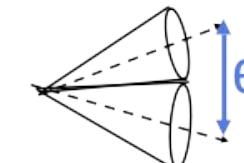
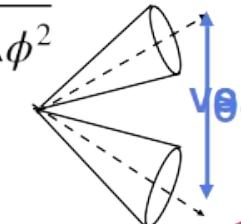
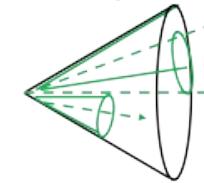
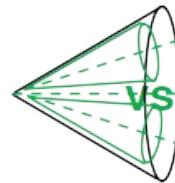
How symmetric is the  
jet splitting?



$R_g$ : distance

between subjets

$$R_g = \sqrt{\Delta\eta^2 + \Delta\phi^2}$$

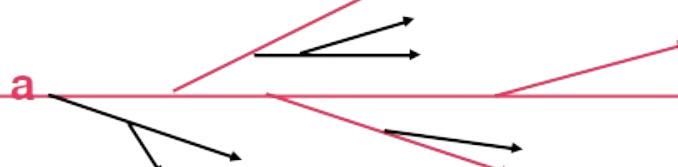


How far apart are the subjets?



$n_{SD}$ : number of splittings  
passing Soft Drop

Number of subjets within a  
jet?

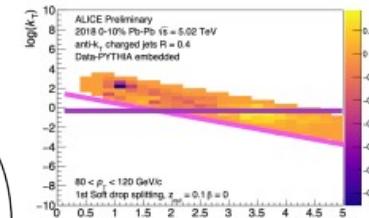


# $z_g$ : jet splitting

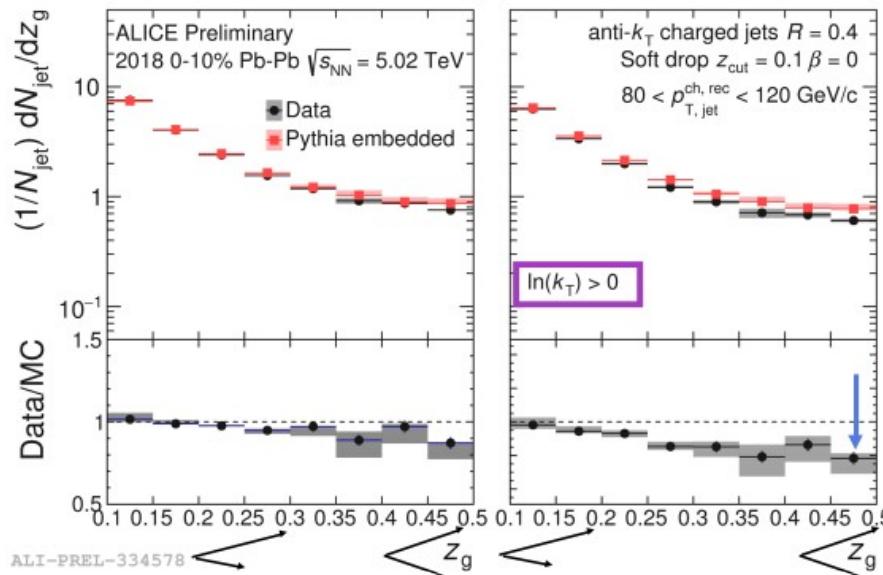
asymmetric splitting: low  $z_g$

symmetric splitting: high  $z_g$

$$z_g = \frac{\min(p_{Ti}, p_{Tj})}{p_{Ti} + p_{Tj}}$$

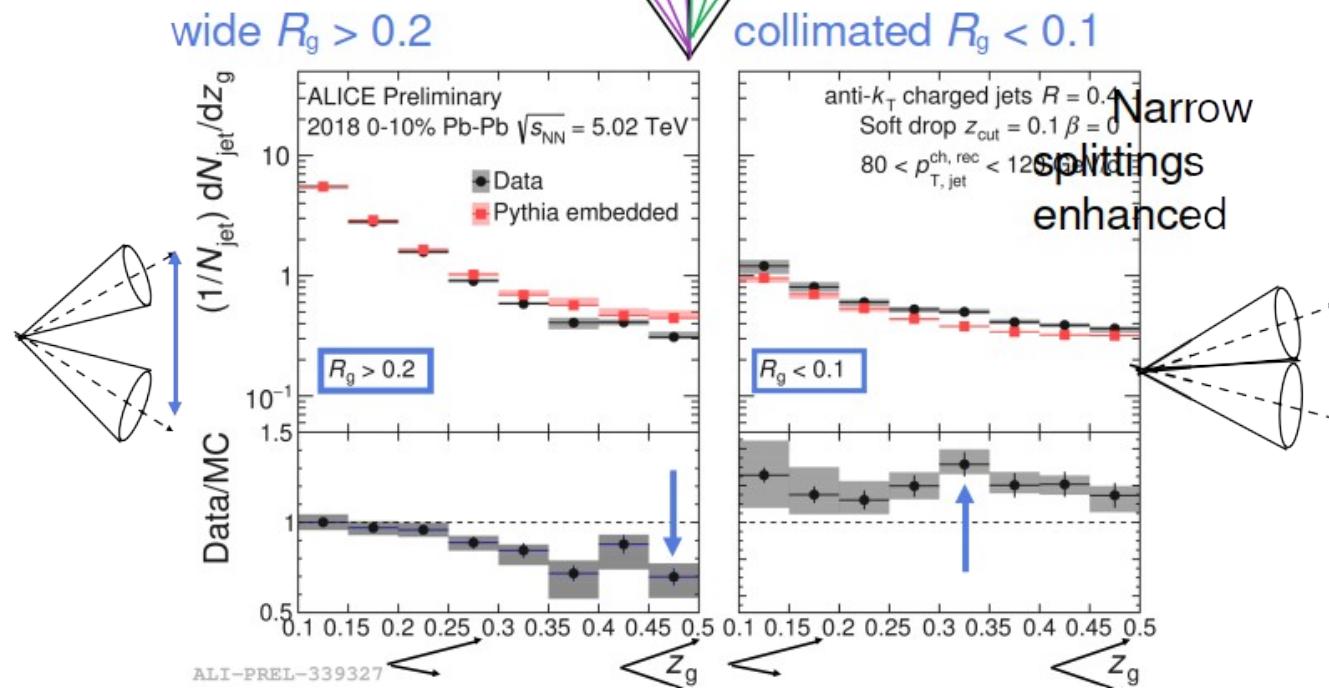
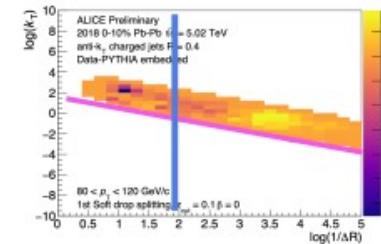
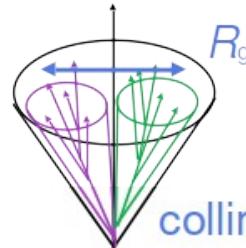


Suppression of  
symmetric  
splittings



# $z_g$ : opening angle

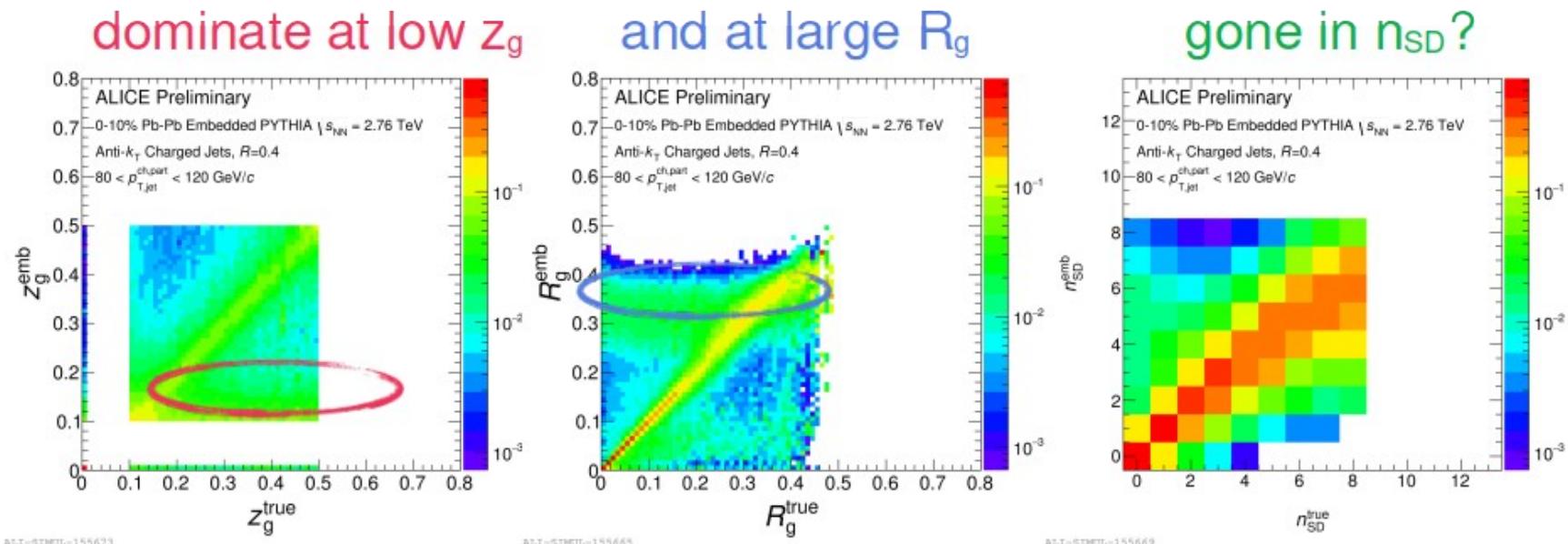
Wide: more significant suppression of symmetric splittings



# Background

# Unfolding: jet splitting

Uncorrelated background leads to subjets being picked up as incorrect or “fake” splittings



Non-diagonal response prohibits unfolding

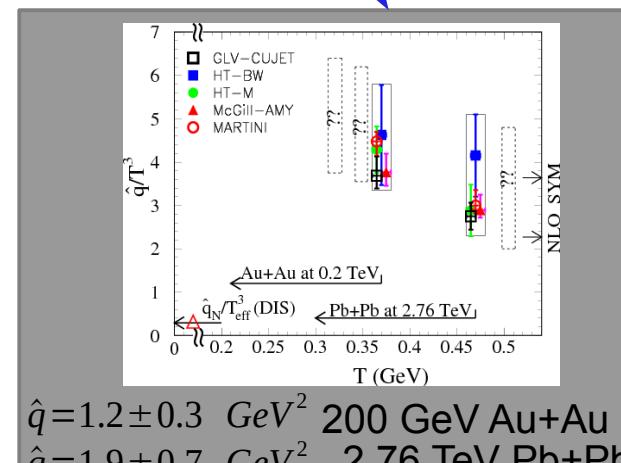
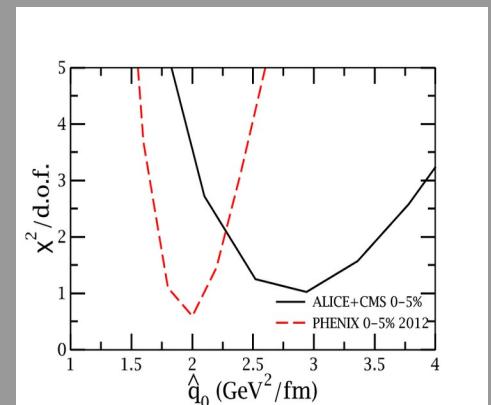
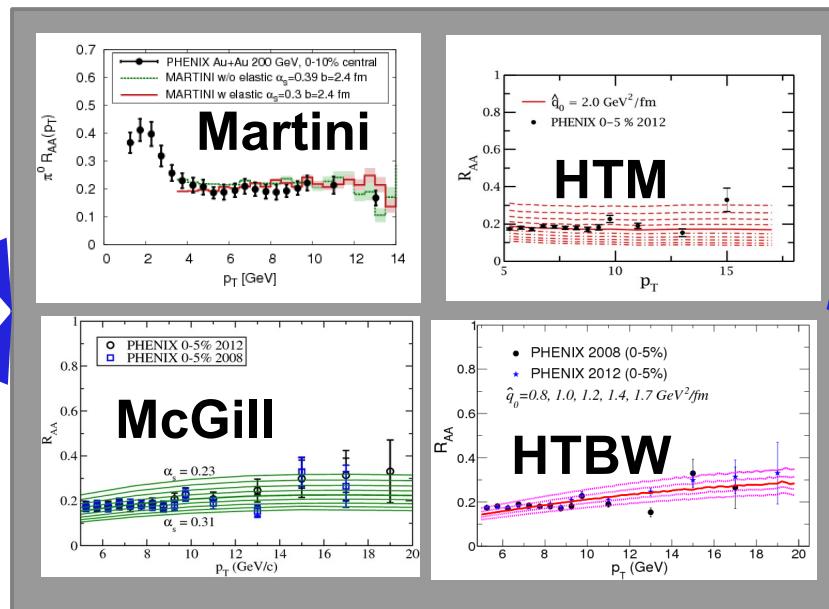
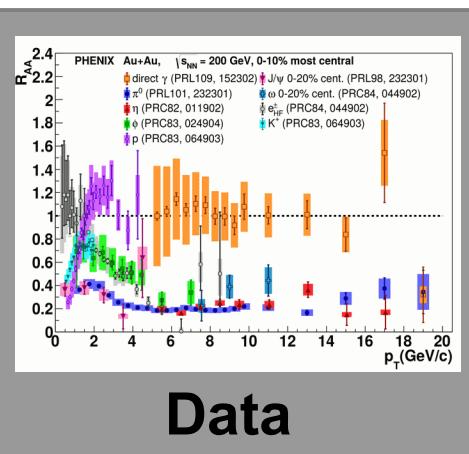
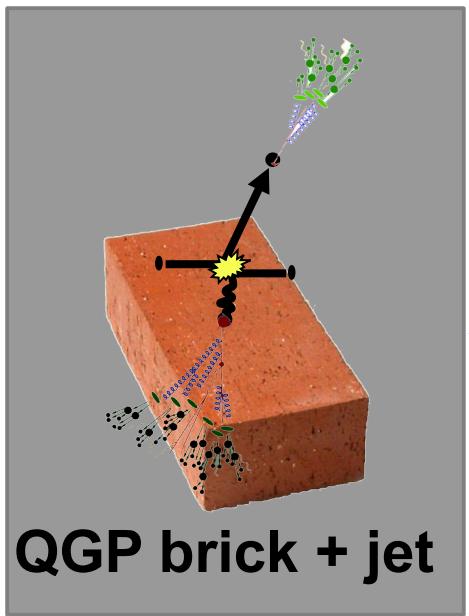
# Mini-summary

- “Jet substructure” is used inconsistently
- Search for new observables
  - Haven’t really used most of the “old” ones!
- So far it’s a mixed bag
  - Many are insensitive
  - Some may have some promise
  - Background tricky

# JETSCAPE

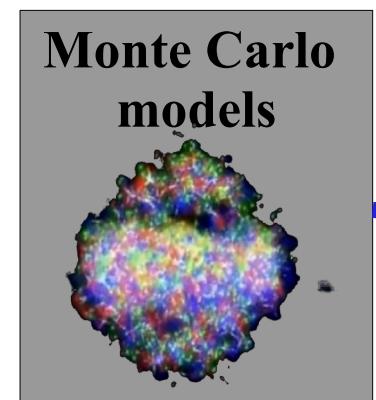
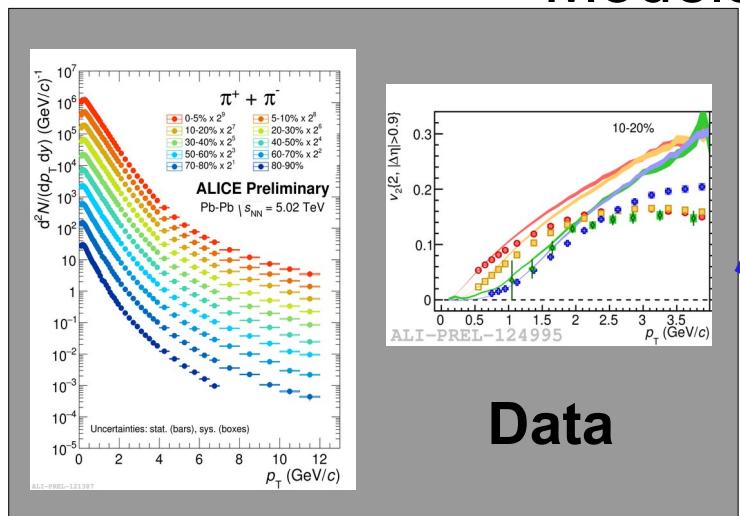
# JET collaboration

Phys. Rev. C 90, 014909 (2014)

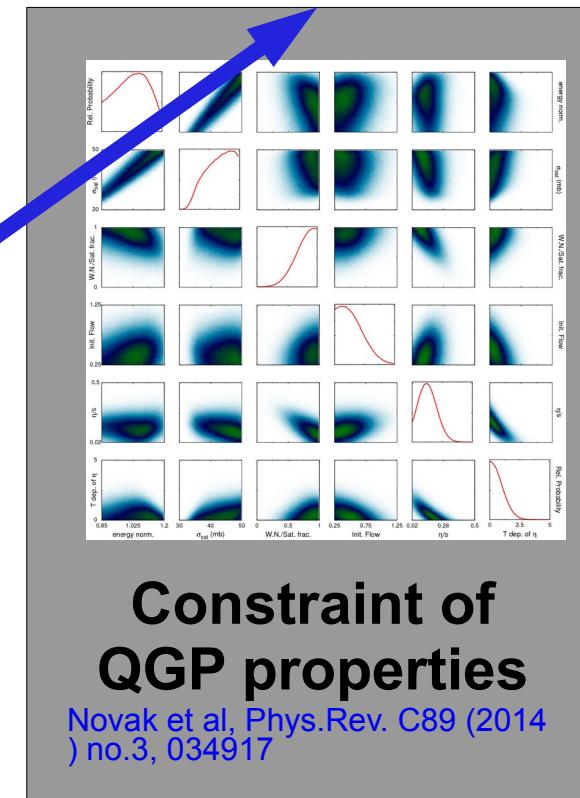
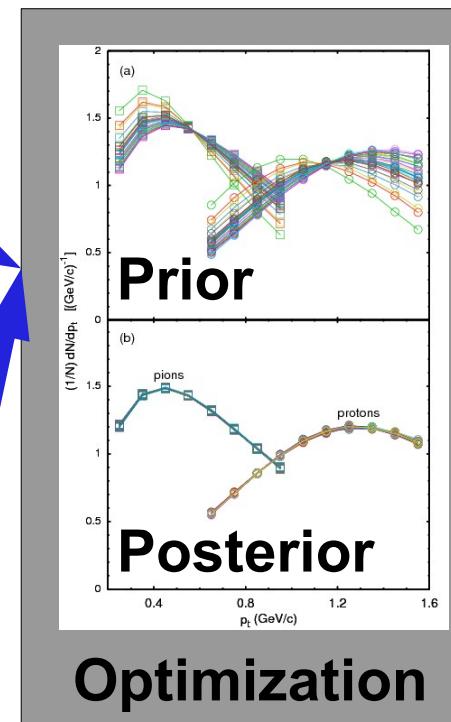


# Bayesian Statistical Analysis Models and Data Analysis Initiative

<http://madai.us>



- Model emulation**
- 1) Run full model  $\sim 1000$  times
  - 2) MCMC parameter search uses emulator (interpolator) in lieu of full model

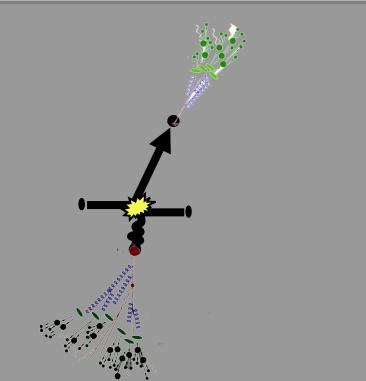
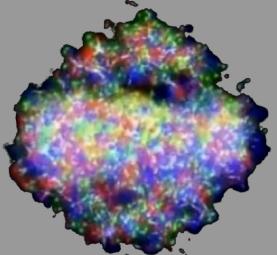


# JETSCAPE Event generator

Jet Energy-loss Tomography with a Statistically and Computationally Advanced Program Envelope

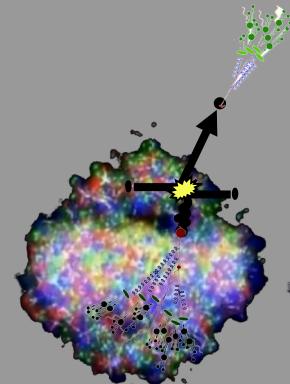
<http://jetscape.wayne.edu/>

Realistic  
medium



Realistic jets

Realistic Monte  
Carlo Model

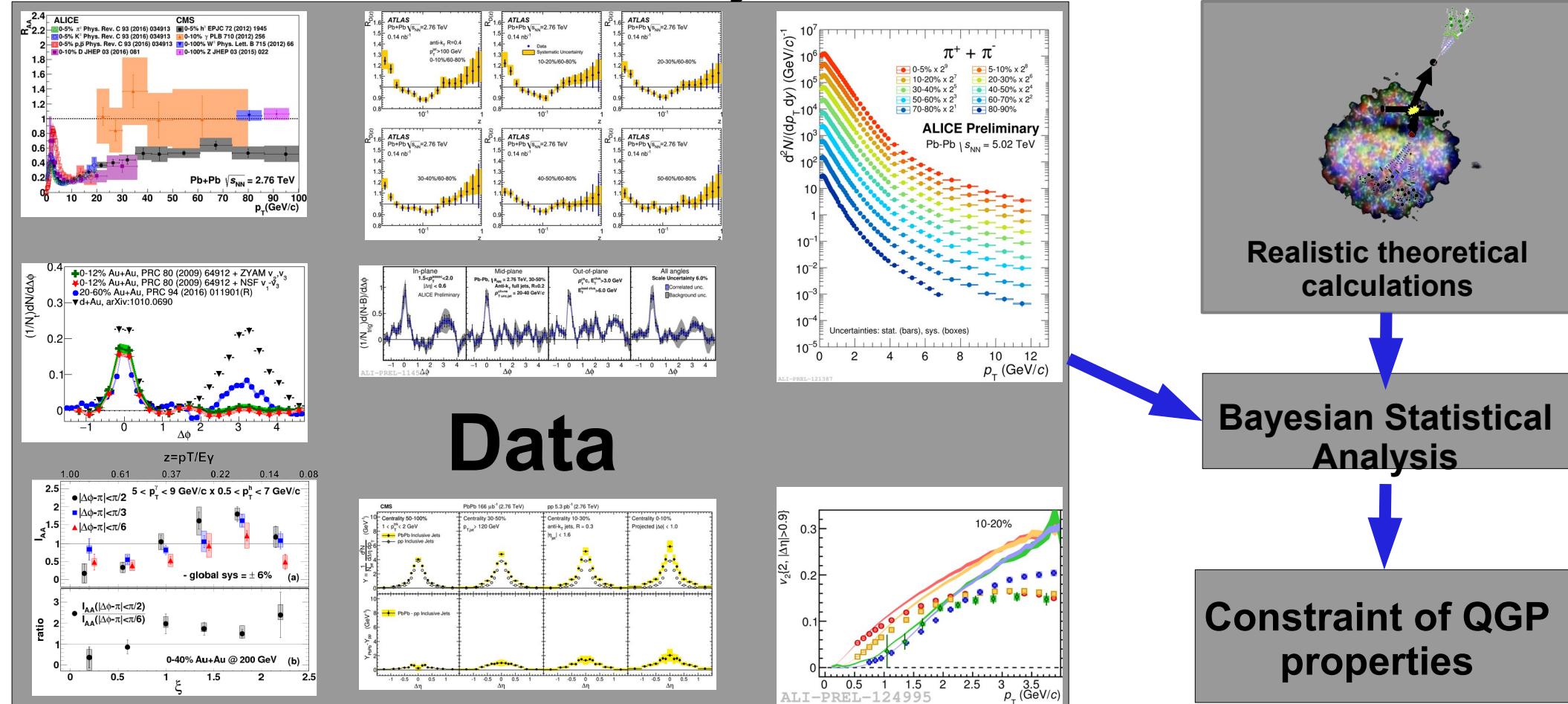


Experimental  
techniques

Realistic  
theoretical  
calculations



# Event Generator + Bayesian Statistical analysis



# Conclusions

# Conclusions

- Jets are complicated and hard to measure to high precision
- Much of the physics we want does not require them
- Extra insight from studying them anyways
- Be skeptical, especially of background subtraction
- Make sure the measurement is comparable to model

The End

# Backup

# Exploring the Lund Plane: in medium

- Jet splittings in heavy-ion (HI) collisions



Splittings happen at different times

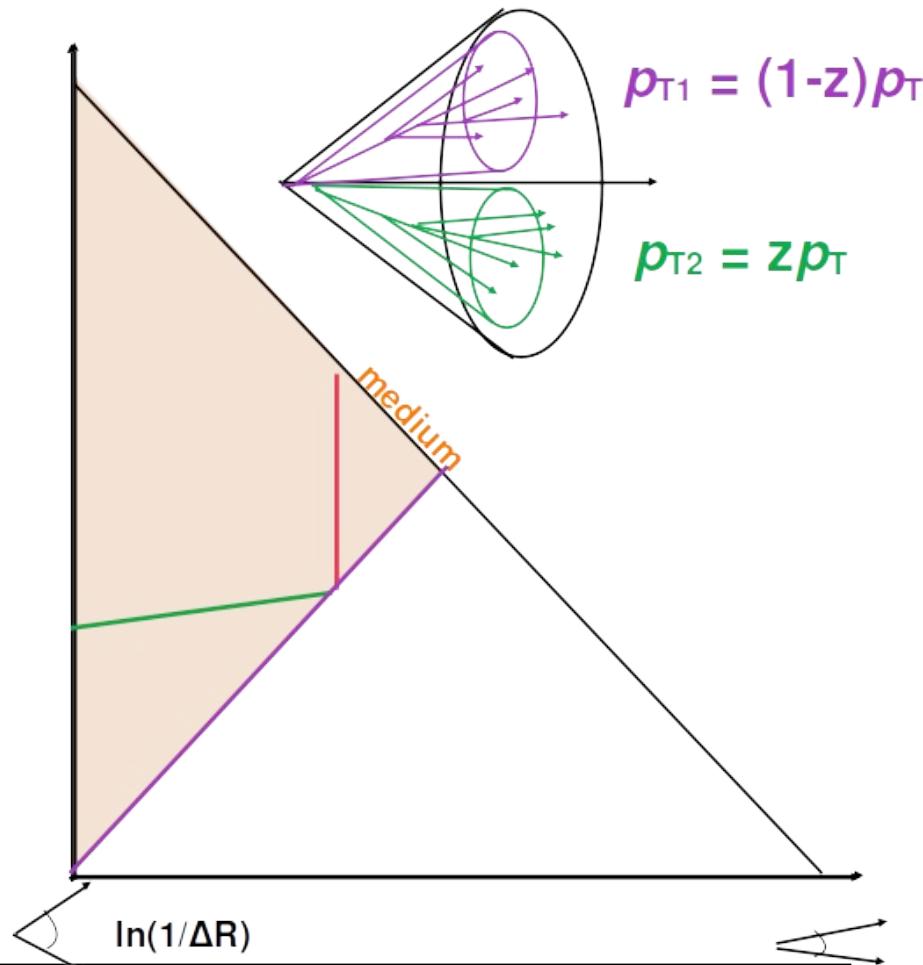
- ▶ Earlier/wider splittings experience more medium



Vacuum splittings vs. non-perturbative in-medium splittings



Coherence vs. decoherence



# Exploring the Lund Plane: in medium

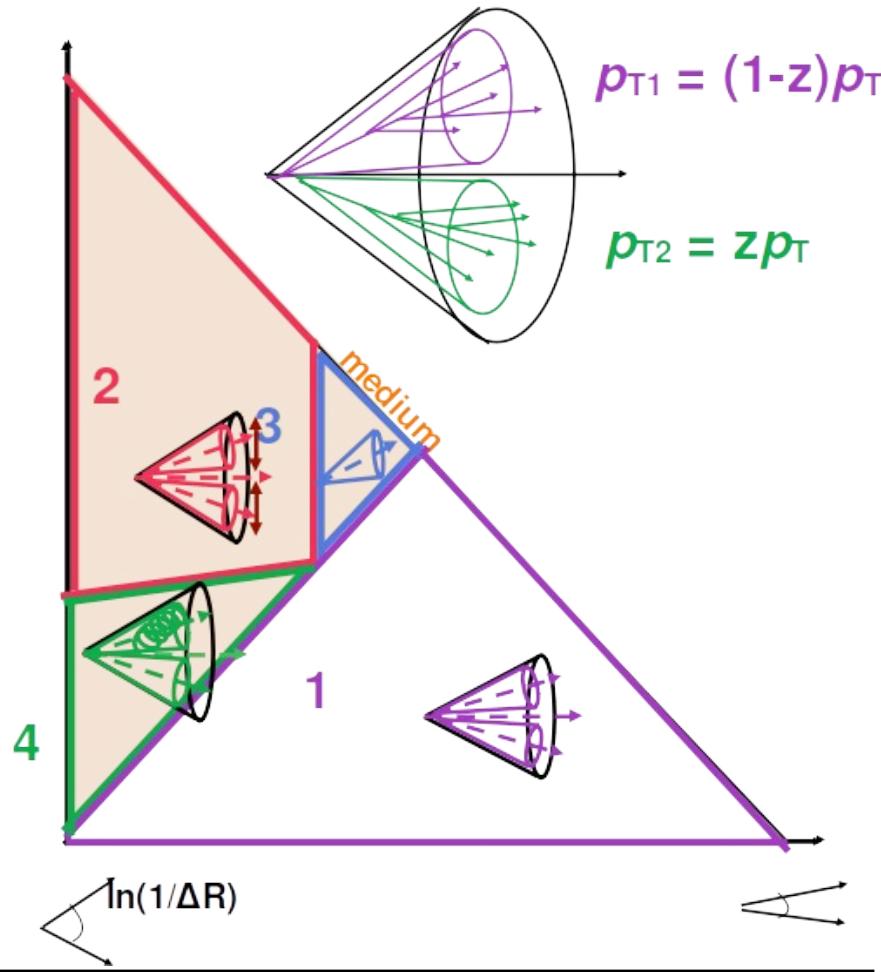
- Jet splittings in heavy-ion (HI) collisions

1: Vacuum splitting outside of medium

2: Vacuum splitting in-medium, resolved (decoherence)

3: Vacuum splittings in-medium, unresolved (coherence)

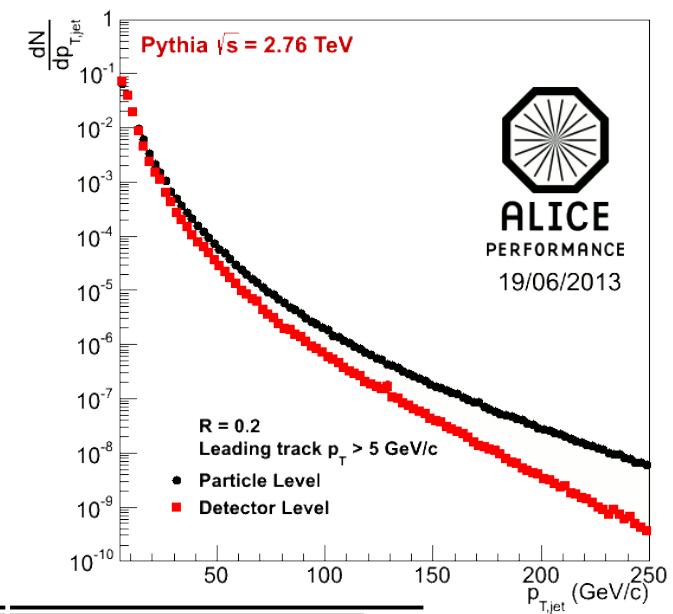
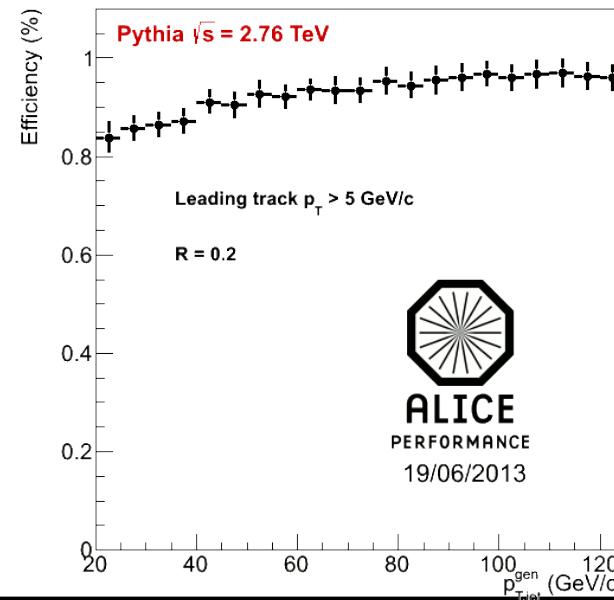
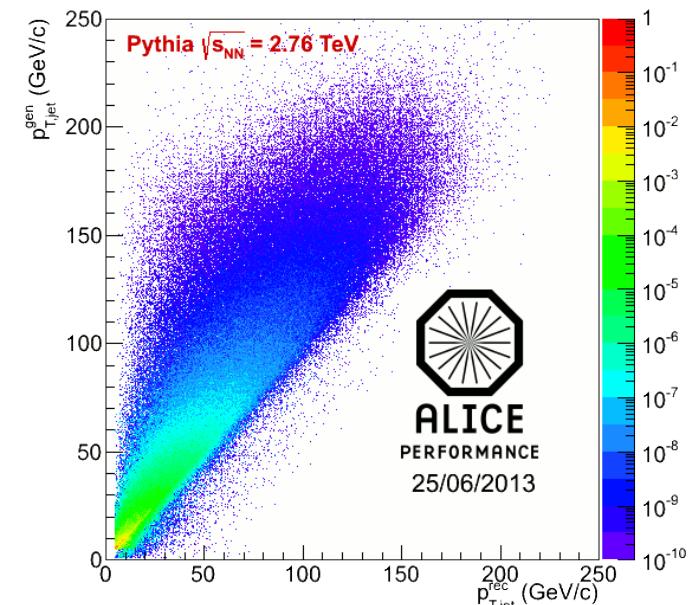
4: Medium-induced splittings



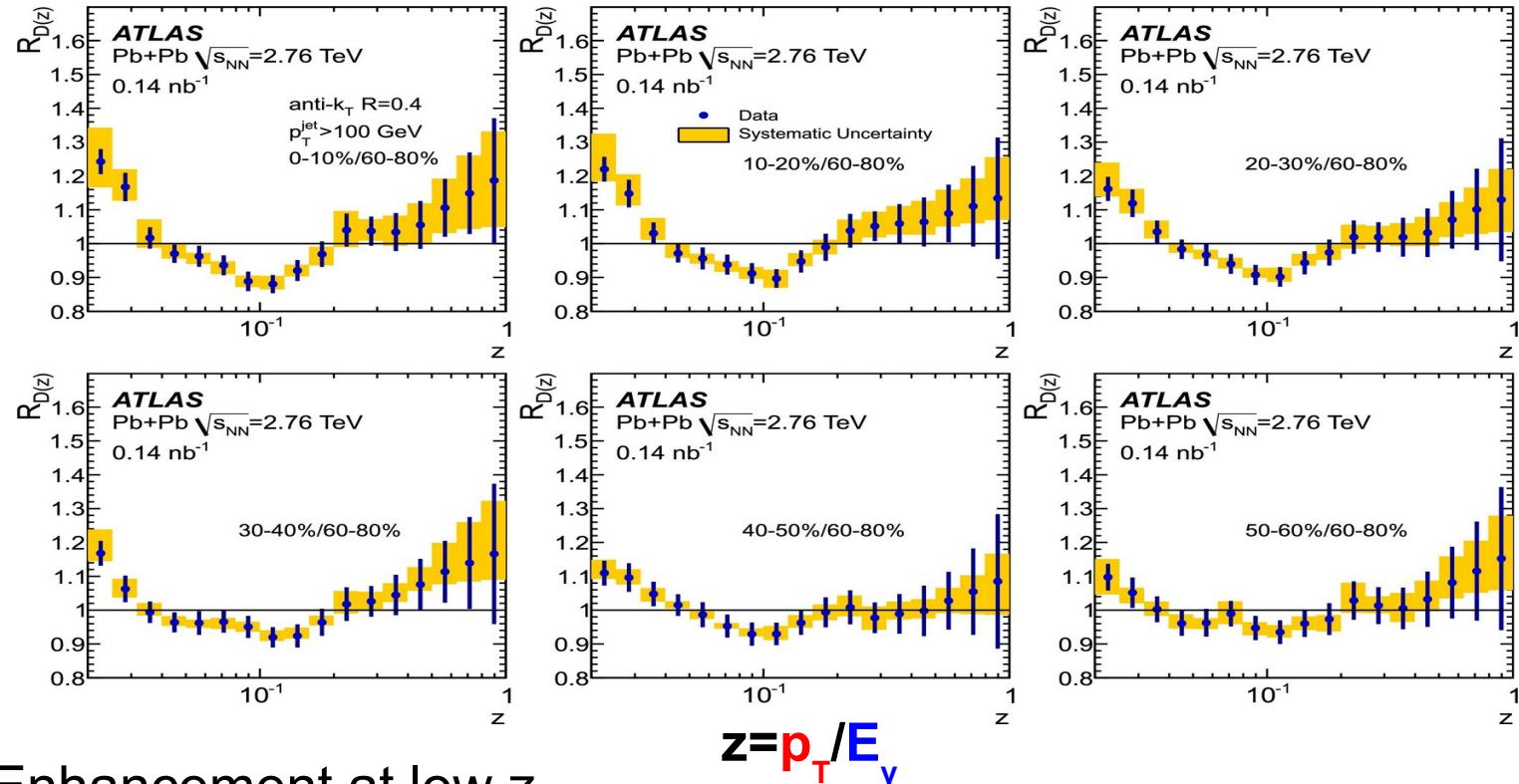
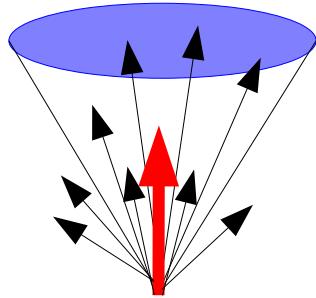
# Jets in ALICE: Response matrix RM<sub>det</sub>

RM<sub>det</sub> quantifies detector response to jets

- “Particle” level jets – defined by jet finder on MC particles
- Pythia with Pb-Pb tracking efficiency
- “Detector” level jets – defined by jet finder after event reconstruction through GEANT
- Particle level jets are geometrically matched to detector level jets
- Matrix has a dependence on spectral shape and fragmentation
- Jet-finding efficiency is probability of a matched particle level jet



# Modified fragmentation



$$z = p_T / E_V$$

- Enhancement at low  $z$
- No modification/enhancement at high  $z$ ?

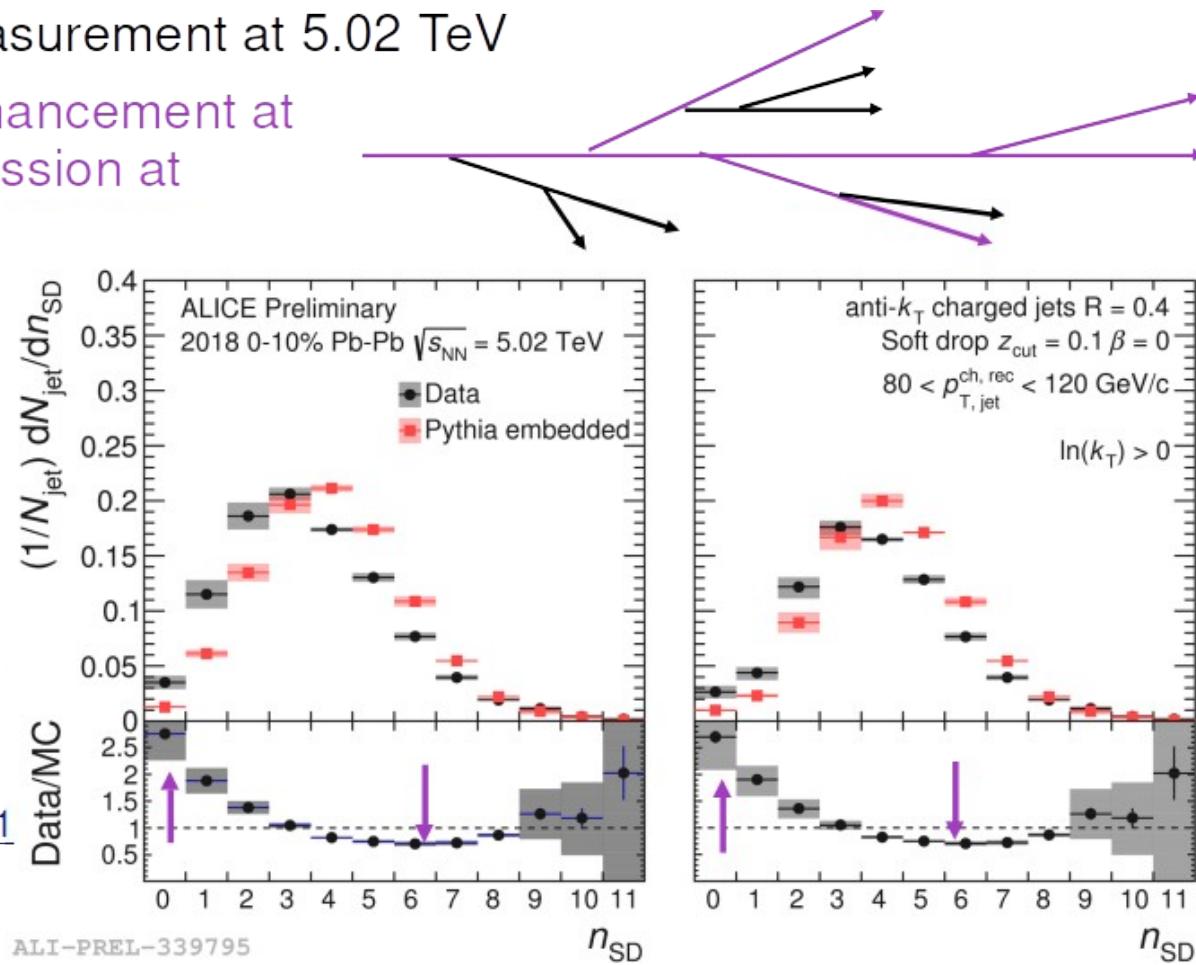
# $n_{SD}$ : iterative declustering

New ALICE measurement at 5.02 TeV

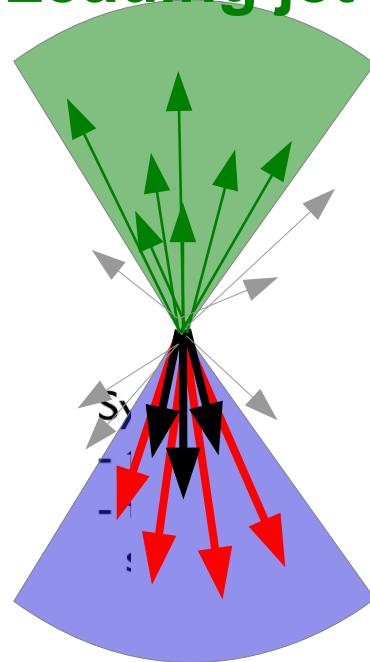
Modification: enhancement at small  $n_{SD}$  and suppression at intermediate  $n_{SD}$

Consistent with wider/earlier being suppressed in the medium, leading to more jets with lower  $n_{SD}^*$

[arXiv:1907.11248v1](https://arxiv.org/abs/1907.11248v1)



# Leading jet

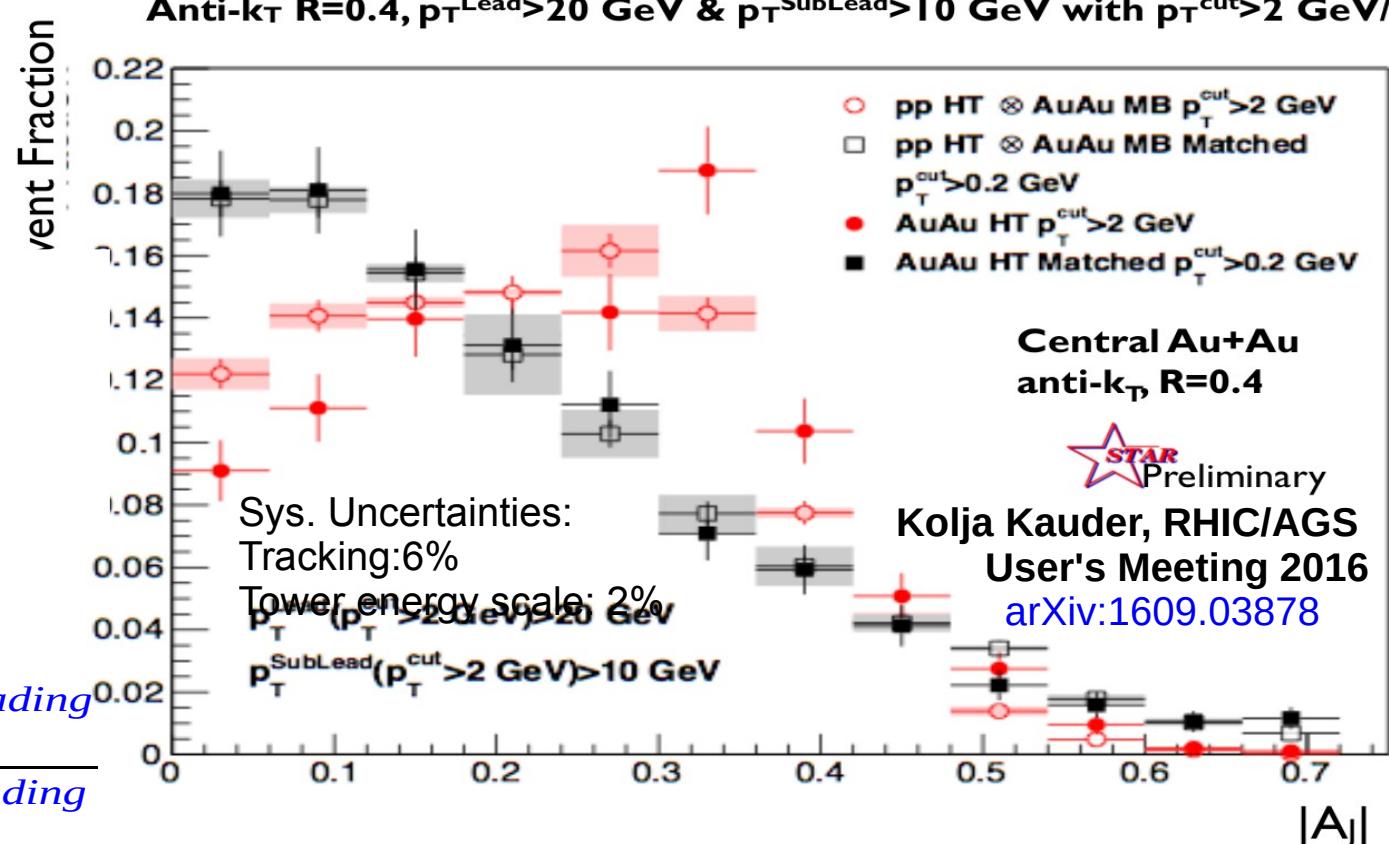


# Subleading jet

$$A_j = \frac{p_T^{\text{leading}} - p_T^{\text{subleading}}}{p_T^{\text{leading}} + p_T^{\text{subleading}}}$$

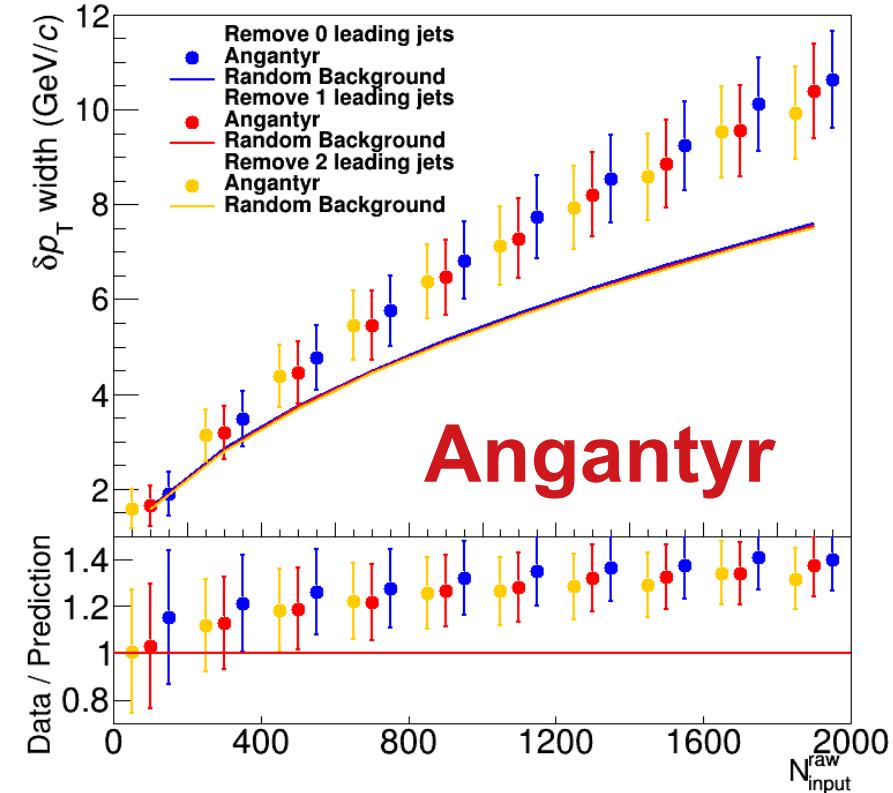
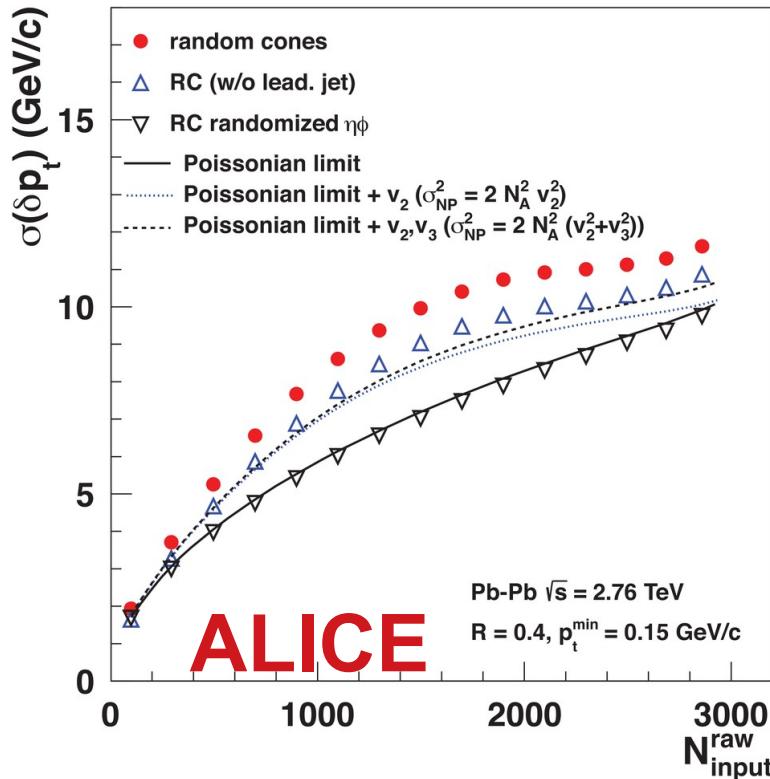
# Di-jet asymmetry

Anti- $k_T$  R=0.4,  $p_T^{\text{Lead}} > 20 \text{ GeV}$  &  $p_T^{\text{SubLead}} > 10 \text{ GeV}$  with  $p_T^{\text{cut}} > 2 \text{ GeV}/c$



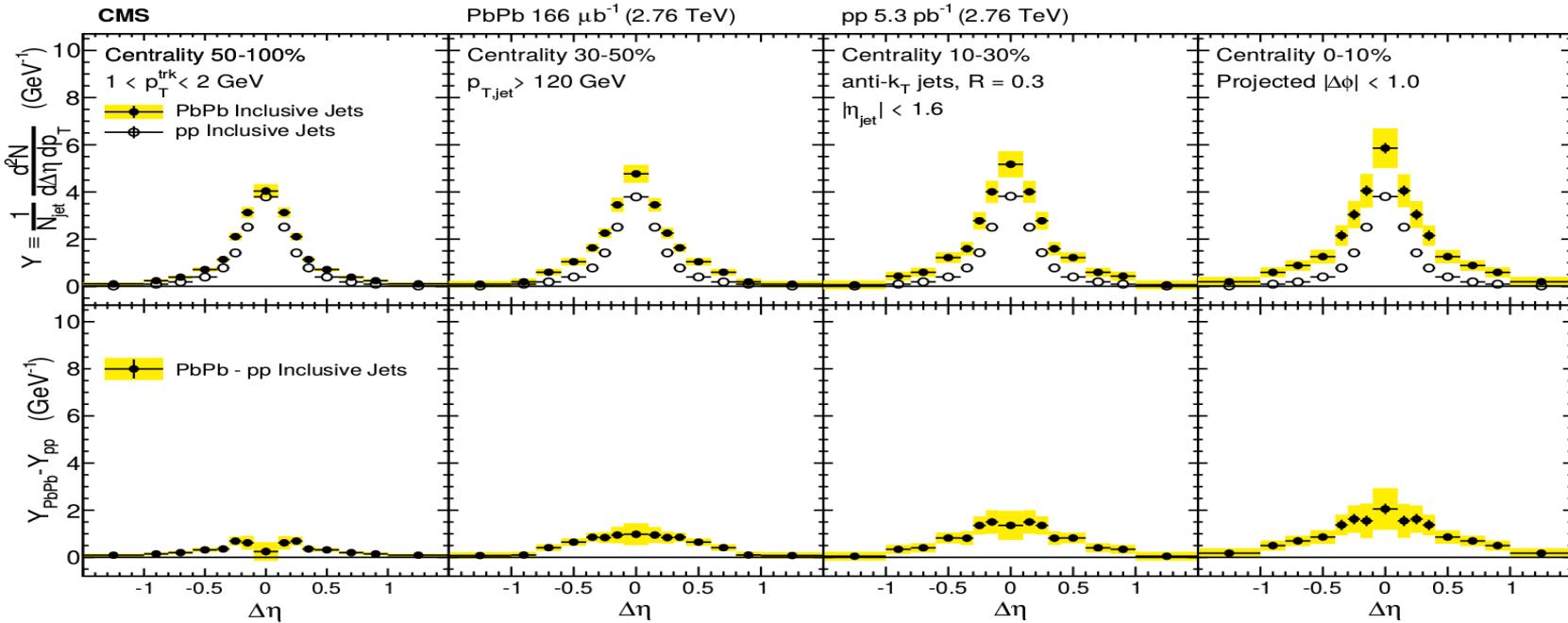
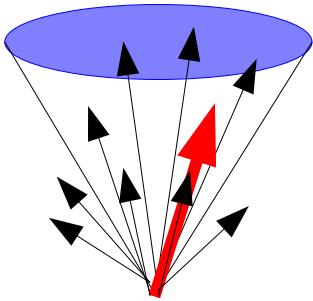
Au+Au di-jets more imbalanced than p+p for  $p_{T\text{cut}} > 2 \text{ GeV}/c$

# Width vs multiplicity



**Discrepancy not from an excess of jets!**

# Jet-hadron correlations



- Jets are broader, constituents are softer
- Also seen in:
  - Di-hadron correlations [Lots of papers]
  - Jet shapes [arXiv:1708.09429, arXiv:1512.07882, arXiv:1704.03046]
  - Dijet asymmetry with soft constituents [PRL119 (2017) 62301]