

$$E_T = \sqrt{p_T^2 + m_0^2} \quad \text{sing} \quad 1 \quad E_T = E_T^+ + E_T^- \quad d^2 N \dots$$

$$\approx \frac{\sqrt{p_T^2 + m_0^2}}{m_T} = m_T \quad = 3E_T^+ + E_T^- + 2E_T^+ + 2E_T^-$$

$$\rightarrow \frac{dE_T}{d\eta}$$

$$= \begin{cases} m_T & \text{meson} \\ m_T + m_0 & \text{antibaryon} \\ m_T - m_0 & \text{meson} \end{cases} \quad 2\pi p_T \, dy \, dp_T$$

$$E = \frac{1}{Ac\ell} \frac{dE}{dy} = \frac{1}{Ac\ell} \frac{dE}{d\eta}$$

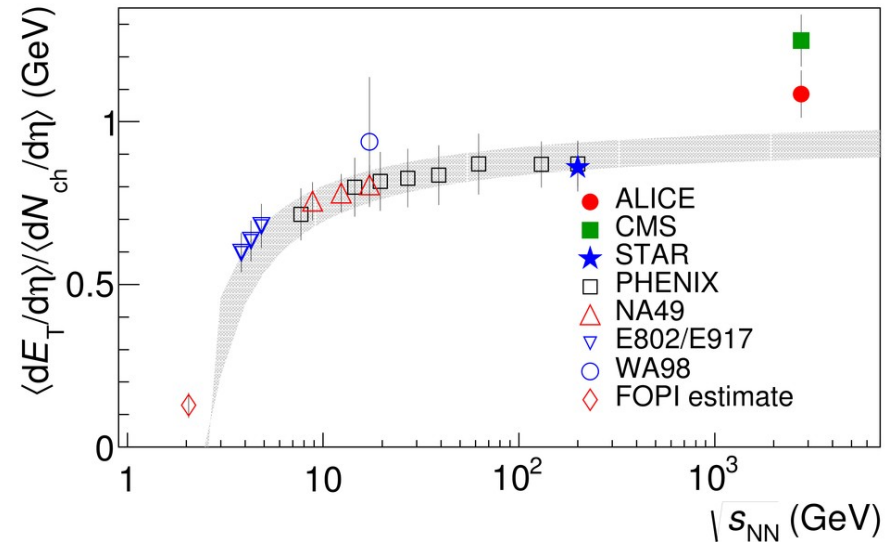
using STAR Data

Christine Nattrass, Biswas Sharma, Soren Sorensen, Ben Smith, Tanner Mengel, Charles Hughes, Nathan Webb

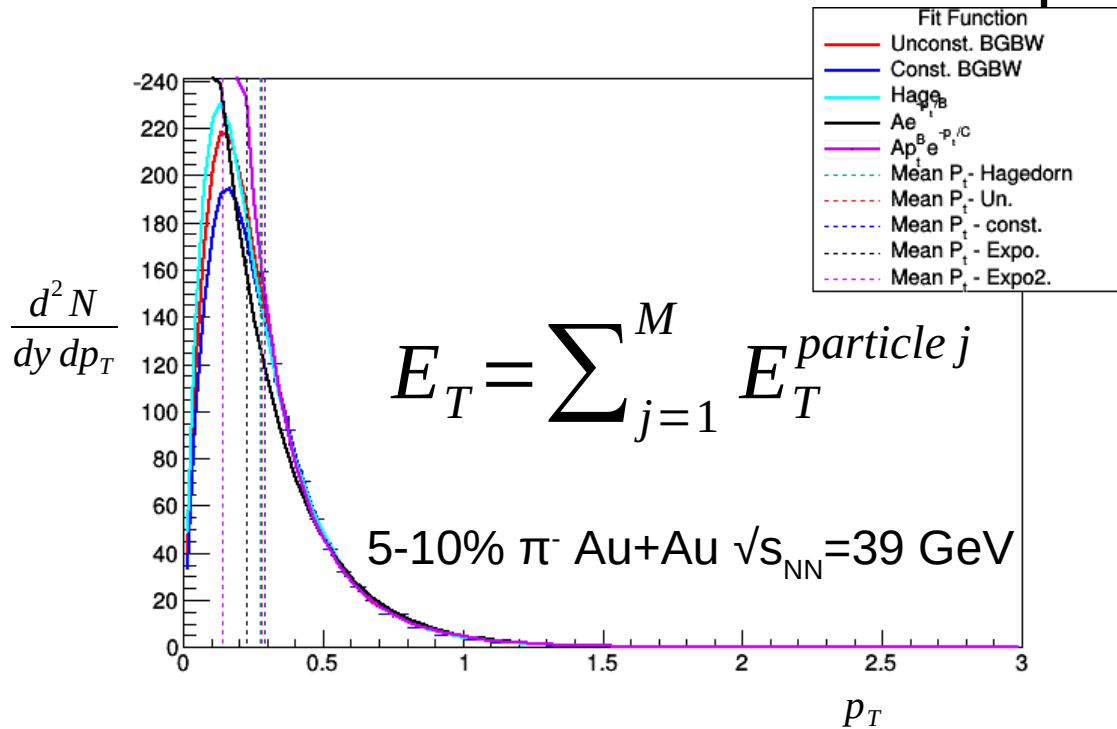
Motivation

$$\epsilon = \frac{1}{V} \frac{dE_T}{dy} = \frac{J}{A_T \tau c} \frac{dE_T}{d\eta}$$

- Cross check data
- Study PID distribution of energy
- Understand E_T/N_{ch} better



Calculating E_T from spectra



- Strange hadron production in Au+Au collisions at $\sqrt{s_{NN}} = 7.7, 11.5, 19.6, 27, \text{ and } 39$ GeV
[Phys. Rev. C 102, 034909 \(2020\)](#)
- Bulk Properties of the Medium Produced in Relativistic Heavy-Ion Collisions from the Beam Energy Scan Program
[Phys. Rev. C 96, 044904 \(2017\)](#)
 $\pi^\pm, K^\pm, p,$
 Distance of closest approach to primary vertex < 3 cm
 - **Includes most but not all daughters**

$$E_T^{PID} = \int_0^{p_T^{min}} f(p_T) E_T dp_T + \sum_{i=1}^N \frac{d^2 N_i}{dy dp_T} E_T(p_T^i, m) + \int_{p_T^{max}}^{\infty} f(p_T) E_T dp_T$$

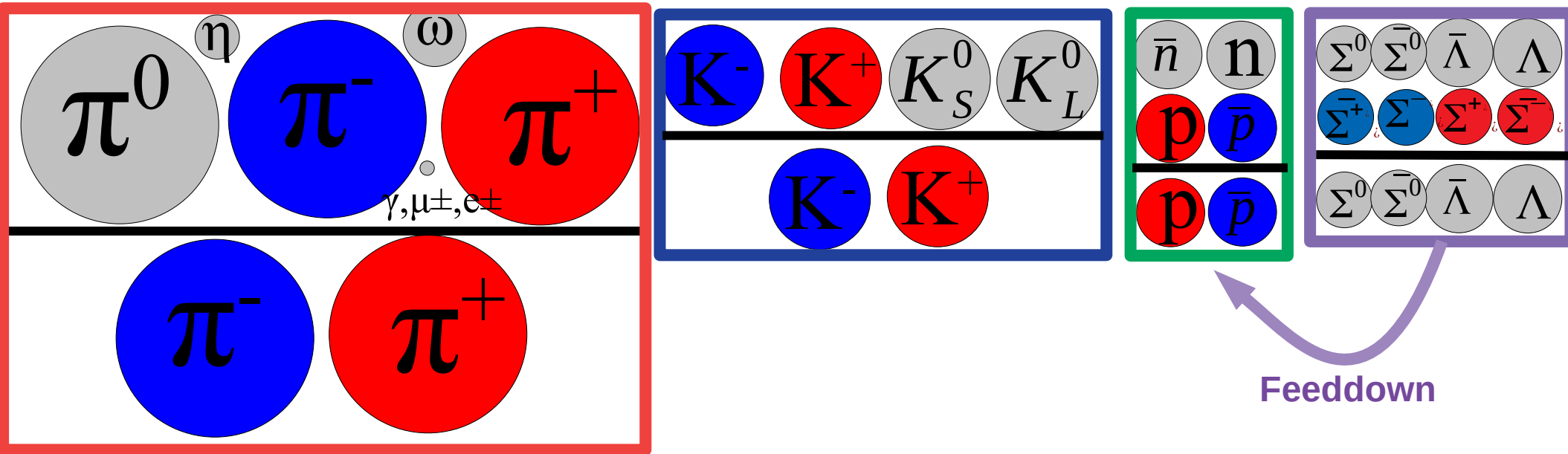
Fit

Data

Fit

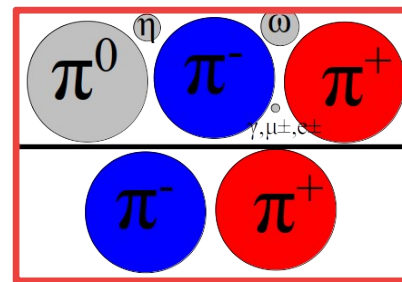
Calculating E_T from published spectra

$$E_T = f_{\pi} E_T^{\pi^{\pm}} + f_K E_T^{K^{\pm}} + f_p E_T^{p, \bar{p}} + f_{\Lambda} E_T^{\Lambda, \bar{\Lambda}}$$

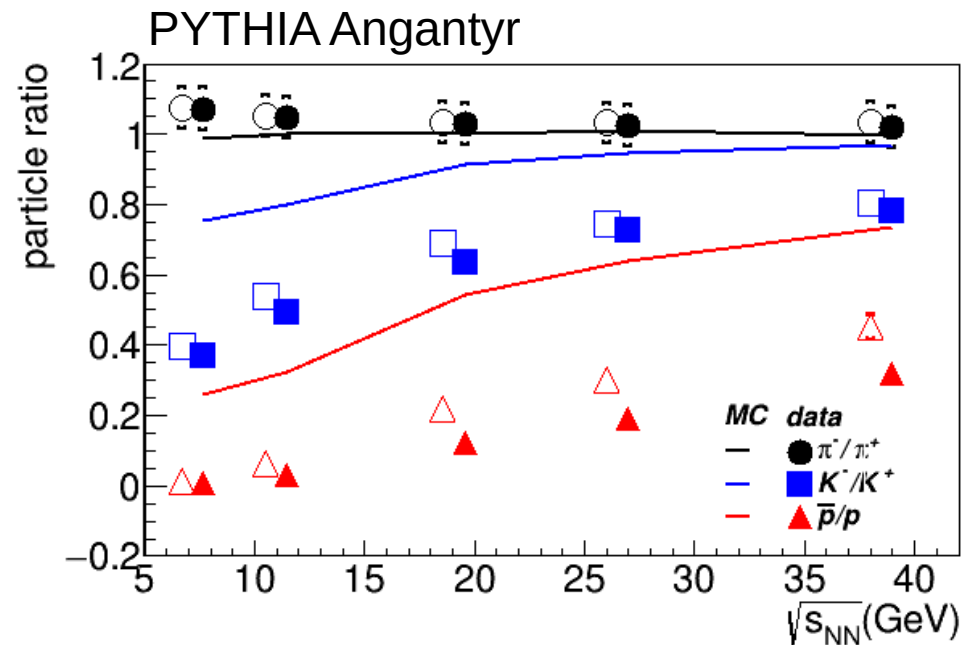


Pion correction f_π

- Pion ratios influenced by short-lived resonances, dominated by η & ω
- Measured ratio of π^0/π^\pm roughly consistent with PYTHIA*



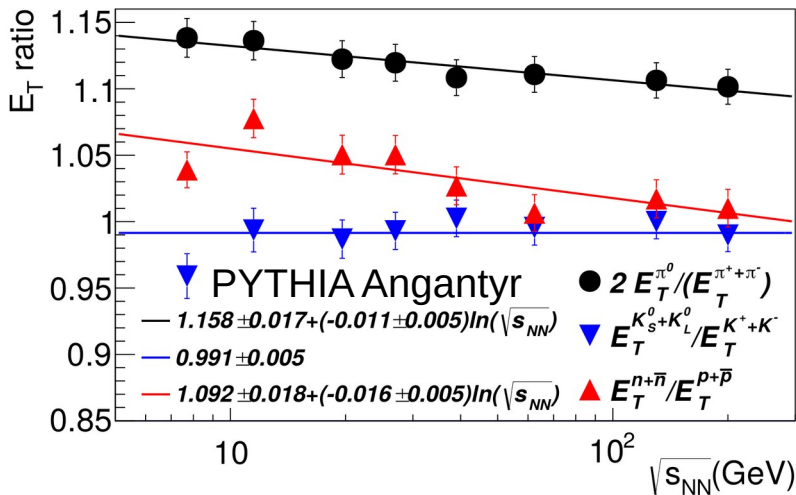
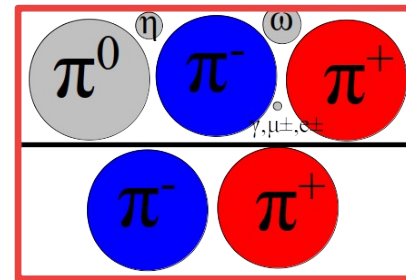
decay	BR (%)
$\eta \rightarrow \gamma\gamma$	39.4
$\eta \rightarrow \pi^0\pi^0\pi^0$	32.7
$\eta \rightarrow \pi^+\pi^-\pi^0$	22.9
$\eta \rightarrow \pi^+\pi^-\gamma$	4.2
$\omega \rightarrow \pi^+\pi^-\pi^0$	89.2
$\omega \rightarrow \pi^0\gamma$	8.3
$\omega \rightarrow \pi^+\pi^-$	1.5



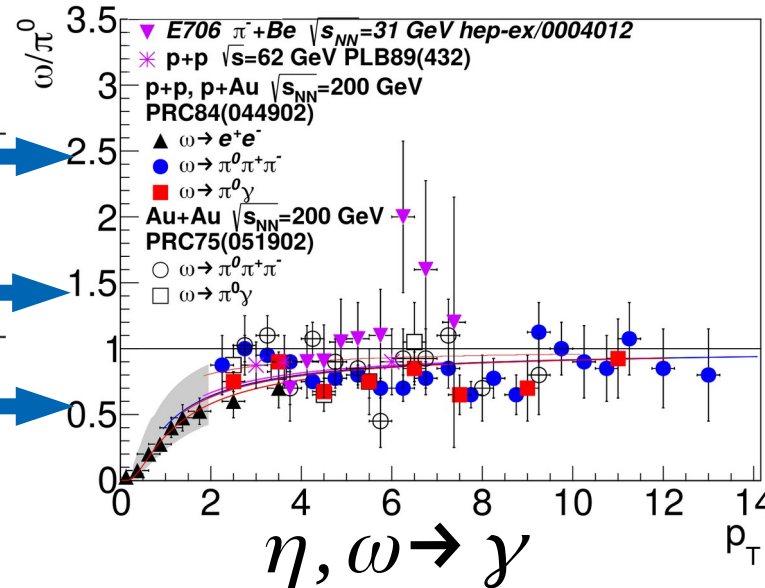
*Yuri Kharlov, internal ALICE presentation

Pion correction

f_π



decay	BR (%)
$\eta \rightarrow \gamma\gamma$	39.4
$\eta \rightarrow \pi^0 \pi^0 \pi^0$	32.7
$\eta \rightarrow \pi^+ \pi^- \pi^0$	22.9
$\eta \rightarrow \pi^+ \pi^- \gamma$	4.2
$\omega \rightarrow \pi^+ \pi^- \pi^0$	89.2
$\omega \rightarrow \pi^0 \gamma$	8.3
$\omega \rightarrow \pi^+ \pi^-$	1.5



$$\eta, \omega, X \rightarrow \pi^0, \pi^\pm$$

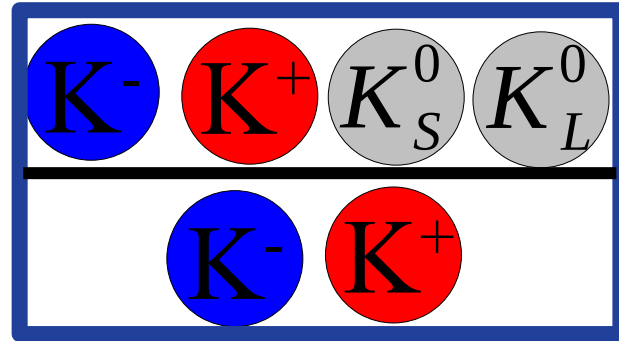
$$f_\pi = 1.56 \pm 0.02$$

- m_T scaling
- match to η/π^0 & ω/π^0 data
- 100% uncertainties

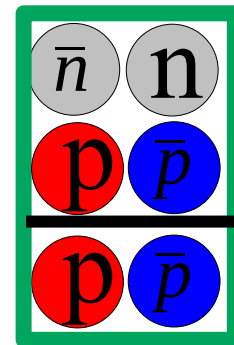
Kaon correction f_K

- Also potentially impacted by resonances
- Used ratios of the (preliminary) yields from BES data

$$f_K = 1.8 \pm 0.2$$



Proton correction f_p



- Lower limit: $f_p = 2$
- Upper limit:
Yield=Primordial+Generated
Antibaryons=Generated
Baryons=Primordial+Generated
Primordial $n/p = N/Z$

$$\frac{N_n + N_{\bar{n}}}{N_p + N_{\bar{p}}} = \frac{N/Z + (2 - N/Z) N_{\bar{p}}/N_p}{1 + N_{\bar{p}}/N_p}$$

$\sqrt{s_{NN}}$	$\frac{N_{\bar{p}}}{N_p}$	Ref.	f_p
7.7	$0.0073 \pm 0.0002 \pm 0.0006$	[3]	2.49 ± 0.49
11.5	$0.0331 \pm 0.0002 \pm 0.0028$	[3]	2.46 ± 0.46
14.5	$0.0641 \pm 0.0005 \pm 0.0109$	[2]	2.43 ± 0.43
19.6	$0.1216 \pm 0.0003 \pm 0.0104$	[3]	2.39 ± 0.39
27	$0.1892 \pm 0.0003 \pm 0.0162$	[3]	2.34 ± 0.34
39	$0.3204 \pm 0.0003 \pm 0.0274$	[3]	2.25 ± 0.25
62.4	0.469 ± 0.026	[5]	2.18 ± 0.18
130	0.708 ± 0.036	[5]	2.08 ± 0.08
200	0.769 ± 0.055	[5]	2.06 ± 0.06

- [1] J. Adam et al. (ALICE), Phys. Rev. C94, 034903 (2016), 1603.04775.
 [2] J. Adam et al. (STAR) (2019), 1908.03585.
 [3] L. Adamczyk et al. (STAR), Phys. Rev. C96, 044904 (2017), 1701.07065.
 [4] J. Adam et al. (STAR) (2019), 1906.03732.
 [5] B. I. Abelev et al. (STAR), Phys. Rev. C79, 034909 (2009), 0808.2041.

Lambda correction f_Λ

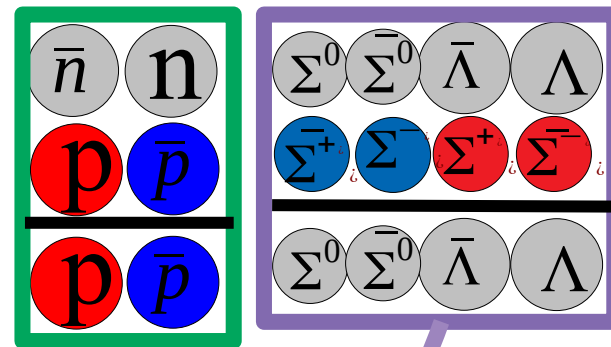
- **Sigma:** Yield ratios
 - Isospin scaling: 1.5
 - PYTHIA: 1.67
 - HIJING: 1.532
- **Feeddown:** STAR published spectra at $\sqrt{s_{NN}}=200$ GeV (Phys.Rev.Lett.97:152301,2006) with and without feeddown*

→ Does not provide a lot of constraint

→ Use branching ratio

$$\rightarrow 0.68 \pm 0.32$$

$$f_\Lambda = 1.08 \pm 0.51$$

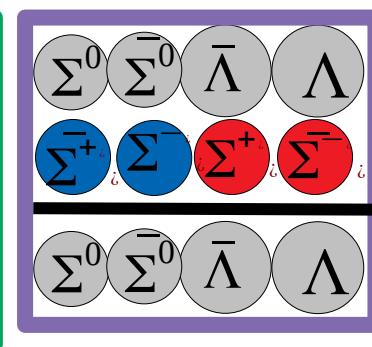
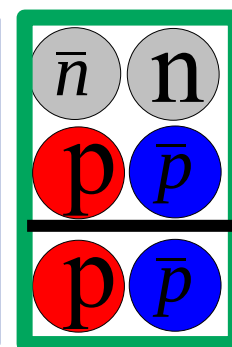
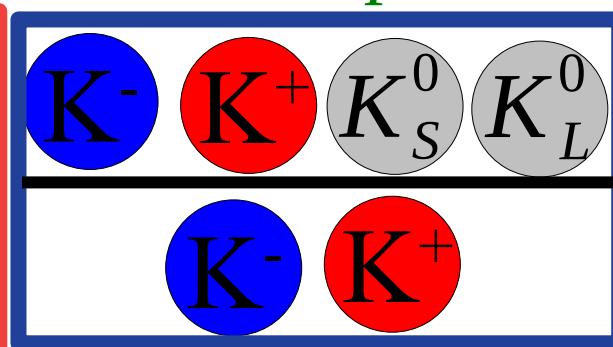
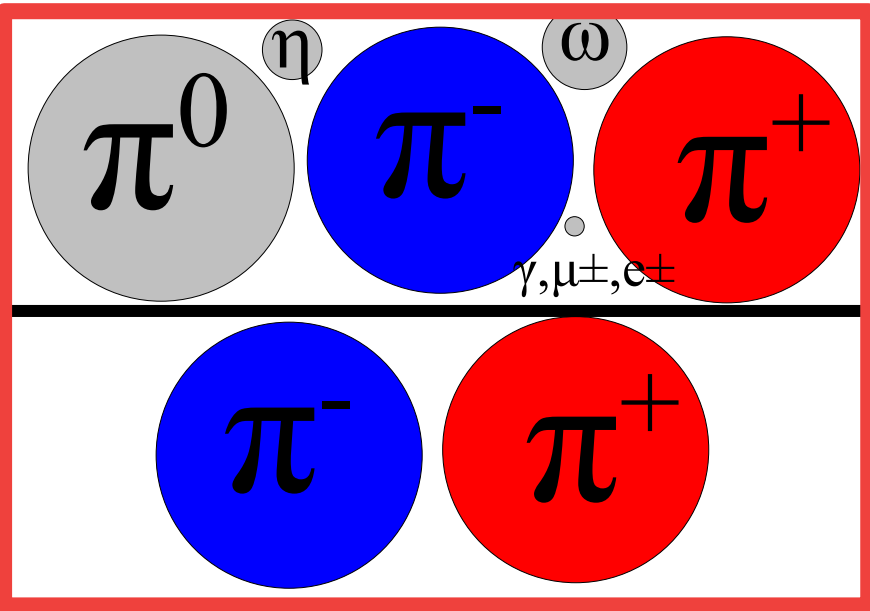


decay	$c\tau$ (cm)
$\Lambda \rightarrow p\pi^-$ (64%)	7.9
$\Lambda \rightarrow n\pi^0$ (36%)	
$K_S^0 \rightarrow \pi^+\pi^-$ (69%)	2.7
$K_S^0 \rightarrow \pi^0\pi^0$ (31%)	
$K_L^0 \rightarrow \pi^\pm e^\mp \nu_e$	1534

*Thanks to Ron Belmont for pointing this out to us

Calculating E_T from published spectra

$$E_T = f_\pi E_T^{\pi^\pm} + f_K E_T^{K^\pm} + f_p E_T^{p, \bar{p}} + f_\Lambda E_T^{\Lambda, \bar{\Lambda}}$$



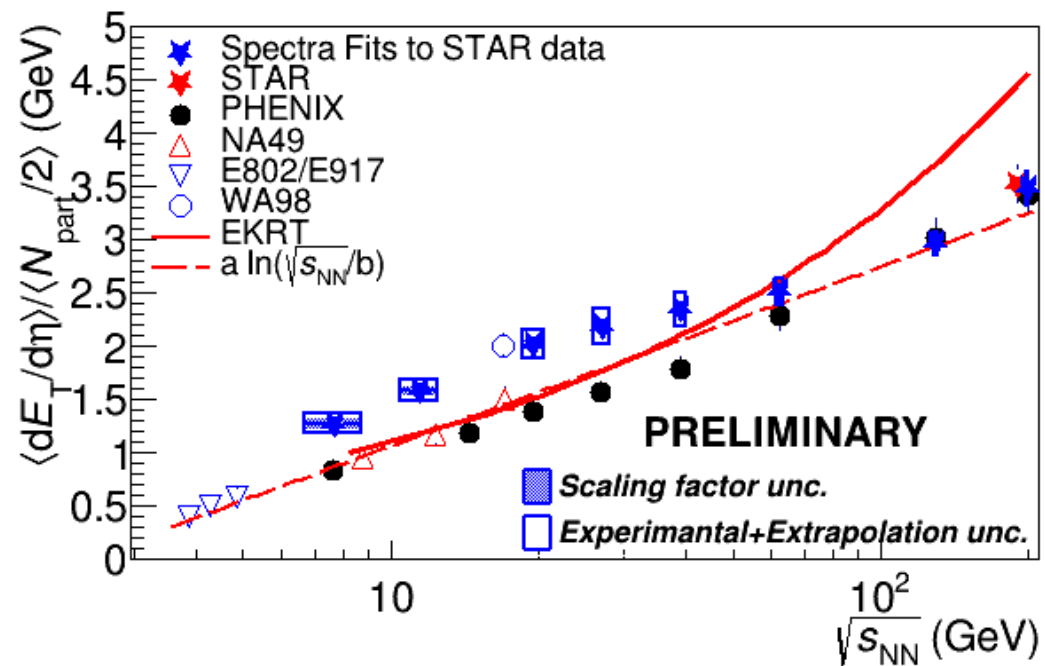
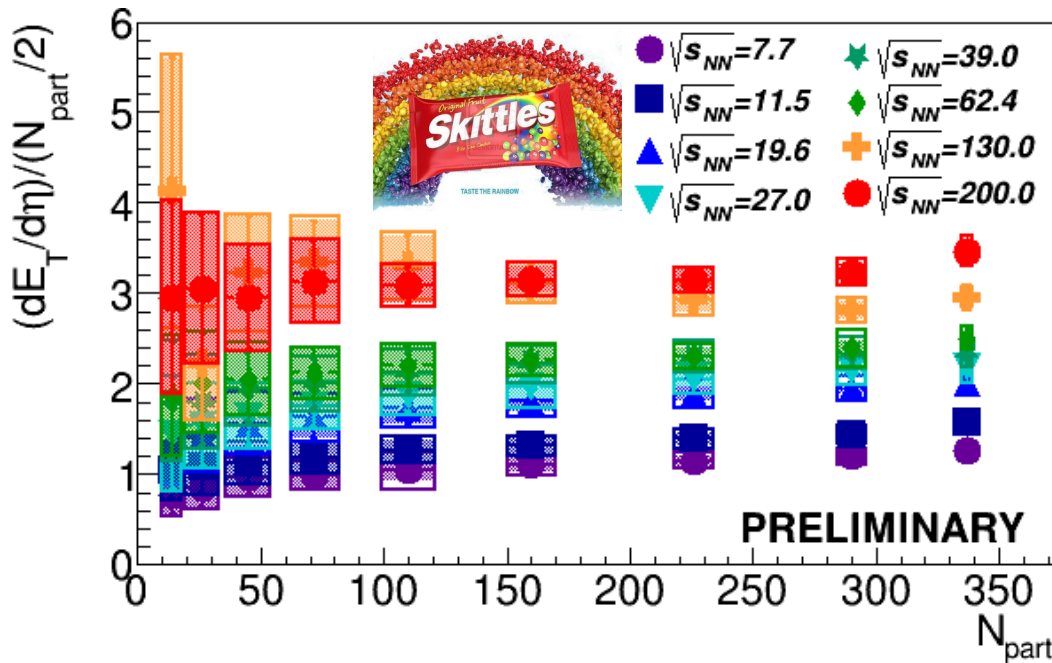
$$f_K = 1.8 \pm 0.2$$

$$2 < f_p < 3$$

$$f_\Lambda = 1.08 \pm 0.51$$

$$f_\pi = 1.56 \pm 0.02 + (E_T^\eta + E_T^\omega) / (E_T^\pi)$$

Results & conclusions



- Tracking detectors can measure E_T well
- E_T calculated from STAR spectra do not agree with PHENIX E_T

What we need to do

- Double check fits
- Separate uncertainties from extrapolation to $p_T=0$
- Finalize corrections and uncertainties
- Write the paper
- Calculations in small systems?

Suggestions

- STAR: BES E_T measurement
- PHENIX: BES spectra measurements
- sPHENIX E_T measurement

Q&A

Q: Why not do this for PHENIX spectra as well?

A: PHENIX spectra only for $p_T > 0.5$ GeV/c, large extrapolation uncertainty

Q: Why not look at energy distribution by particle type?

Q: Why not look at E_T/N_{ch} ?

A: We are. To be continued...

Q: Why not look at small systems?

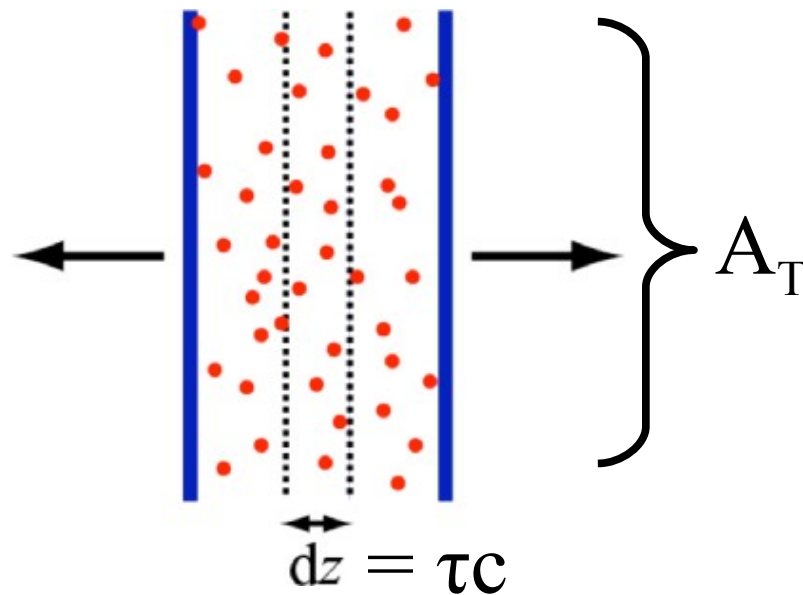
A: We will. To be continued...

How can we estimate the energy density?

- Transverse energy (E_T)
 - sum of particle energies in transverse direction
- Volume $V = A_T \tau c$
- τ = formation time
- Energy density ϵ

$$\epsilon = \frac{1}{V} \frac{dE_T}{dy} = \frac{J}{A_T \tau c} \frac{dE_T}{d\eta}$$

- QGP formation for $\epsilon > 0.5 \text{ GeV}/\text{fm}^3$

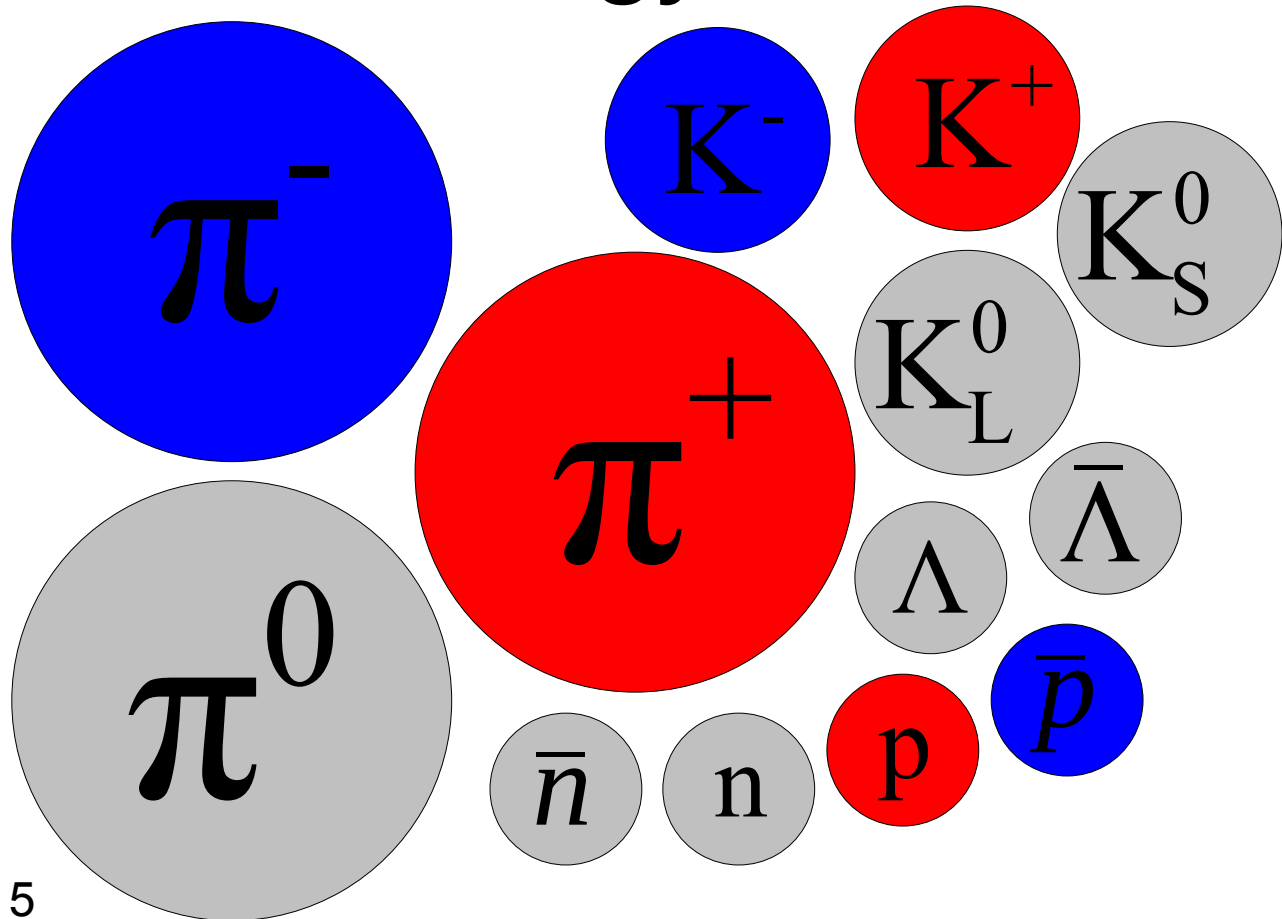
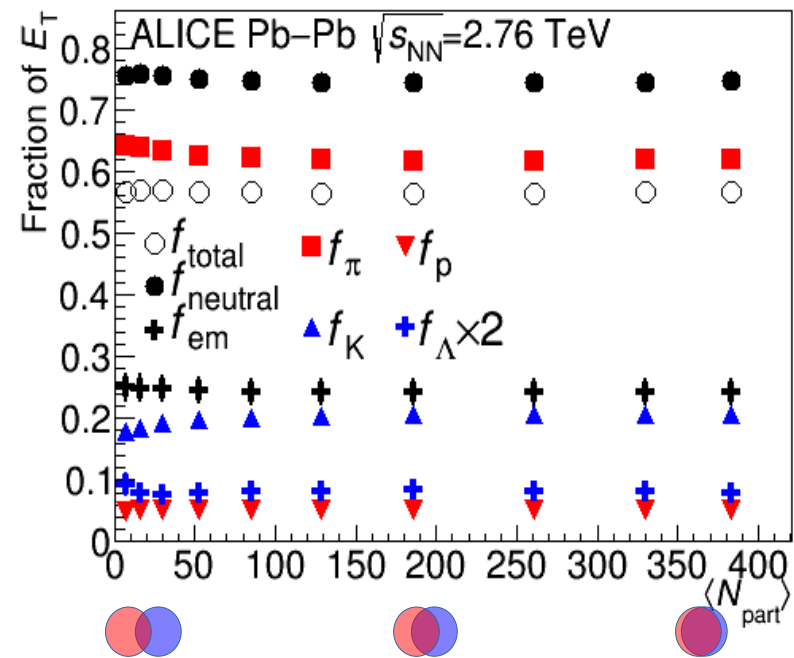


Methods for measuring E_T

- CMS: Tracking + electromagnetic calorimeter + hadronic calorimeter
- PHENIX: Electromagnetic calorimeter
- STAR: Tracking + Electromagnetic calorimeter
- ALICE: Tracking*

*Other methods used as cross checks

Where is the energy?

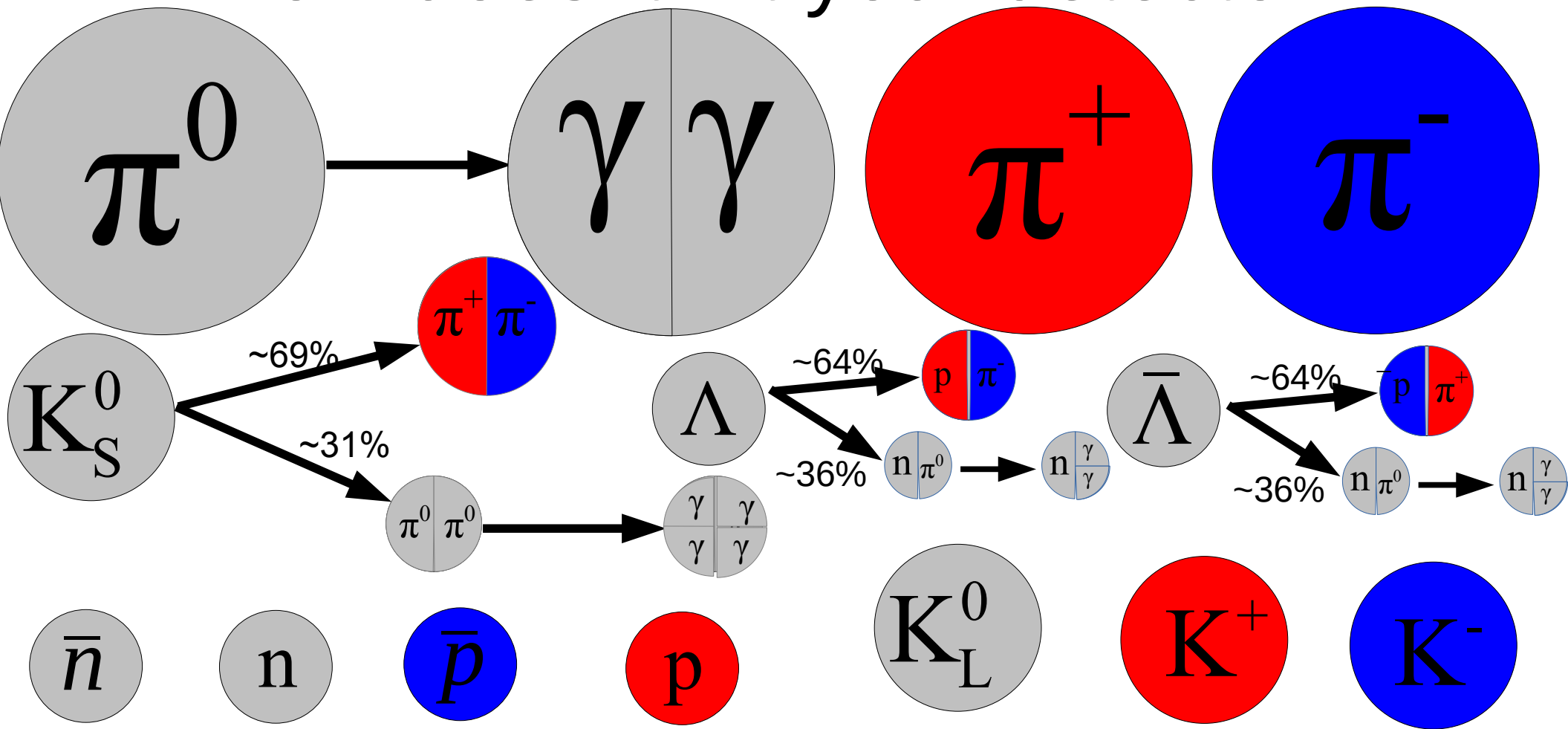


Scale: diameter in inches = $\sqrt{\text{fraction}} * 5$

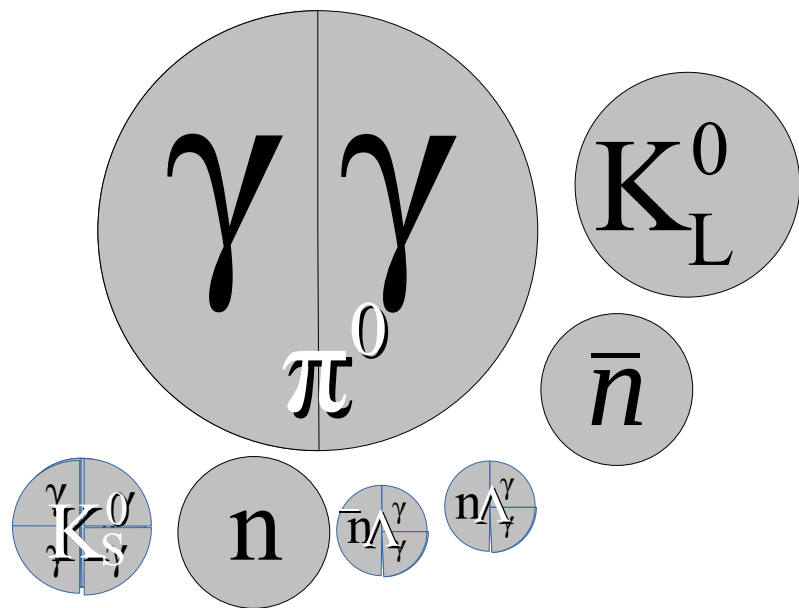
Numbers from 2.76 TeV Phys. Rev. C 94 (2016) 034903

Christine Nattrass, APS April Meeting, 19 April 2021

How does it hit your detector?

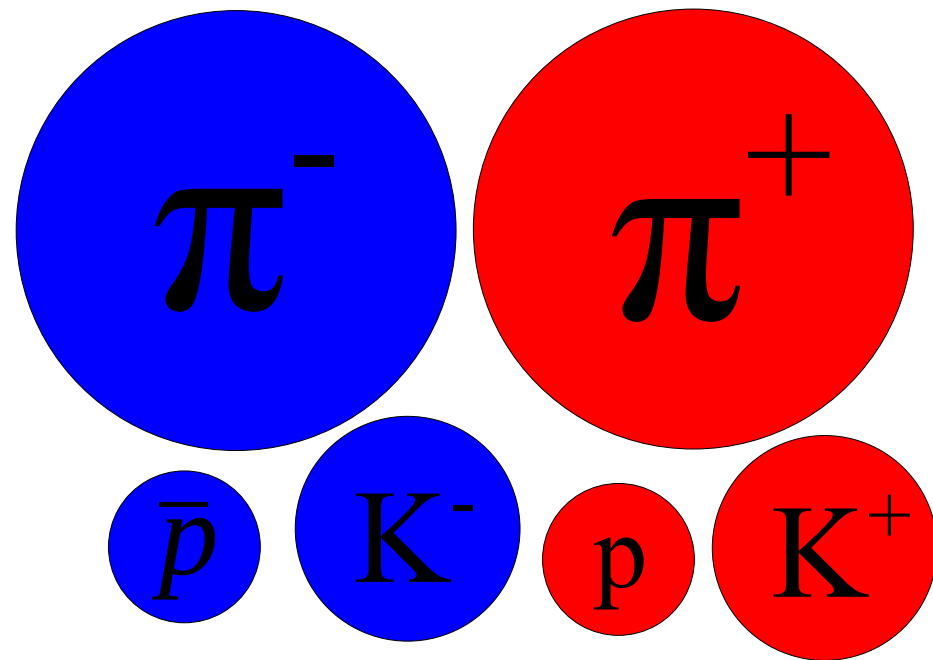


How does it hit your detector?



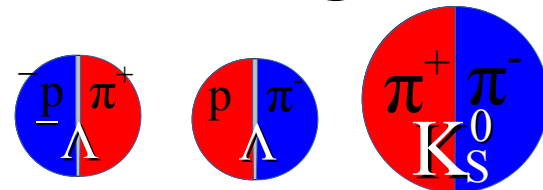
35% neutral

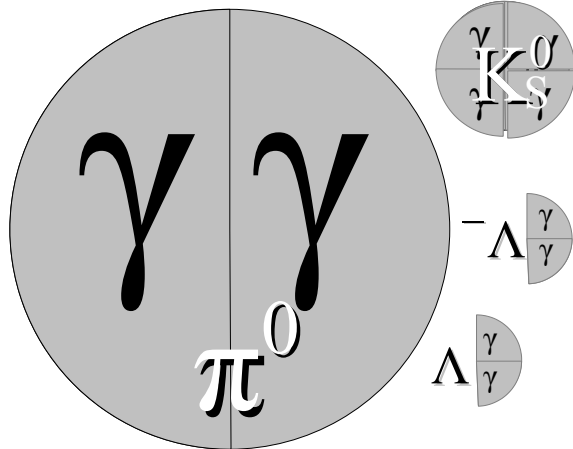
11% in neutral hadrons



65% charged

**7% in
secondaries**



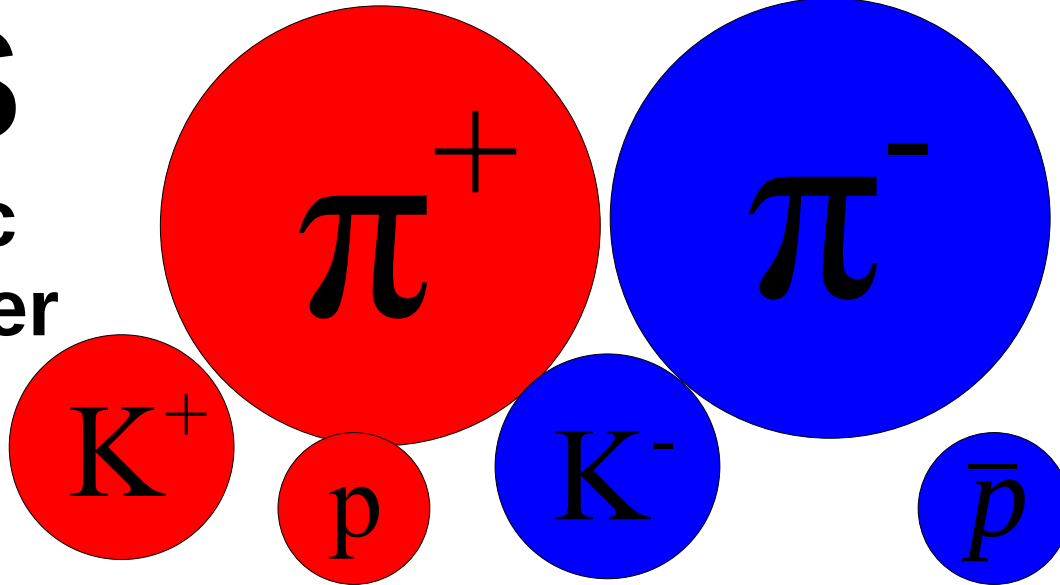


24% as a γ

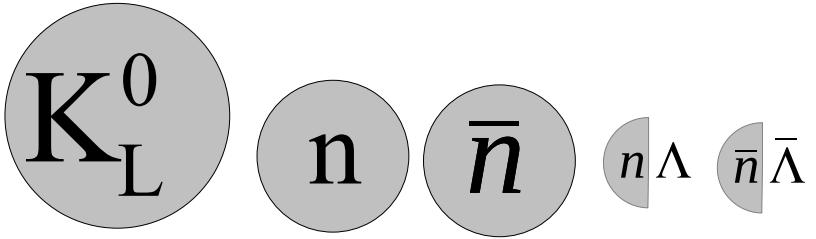
Measure in electromagnetic calorimeter

CMS

Hadronic calorimeter

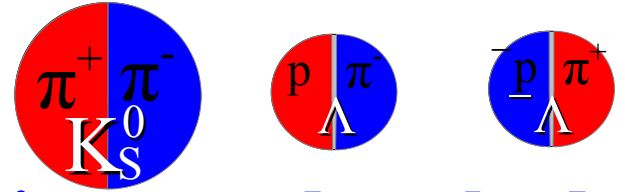


58% in primary hadrons



11% as a neutral hadron

Measure in hadronic calorimeter

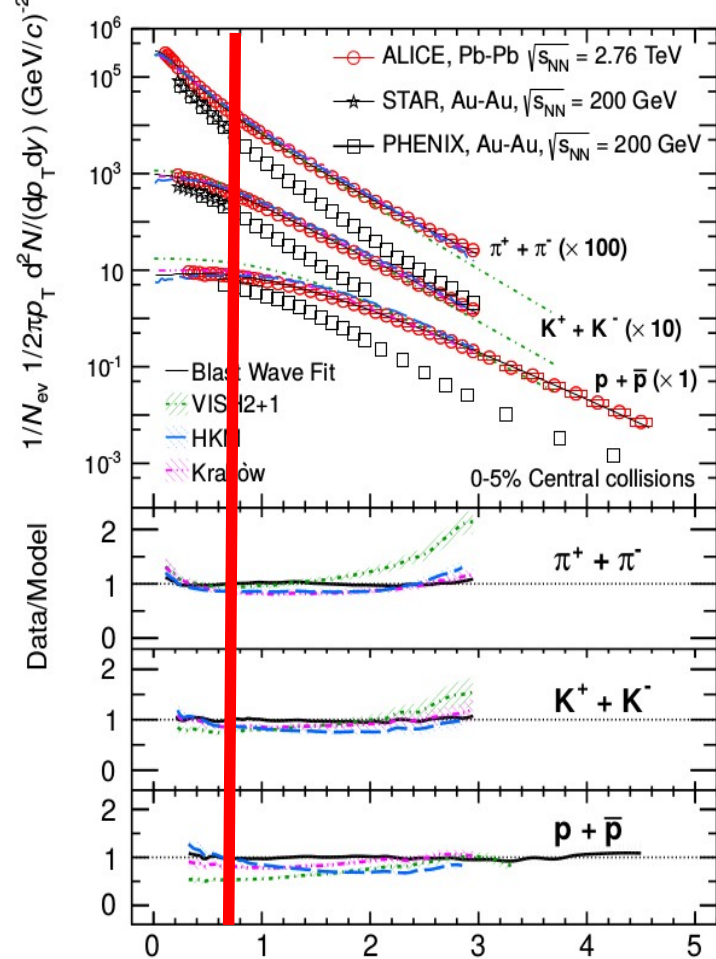


7% in secondary hadrons

Measure in tracking detectors and hadronic calorimeter

CMS

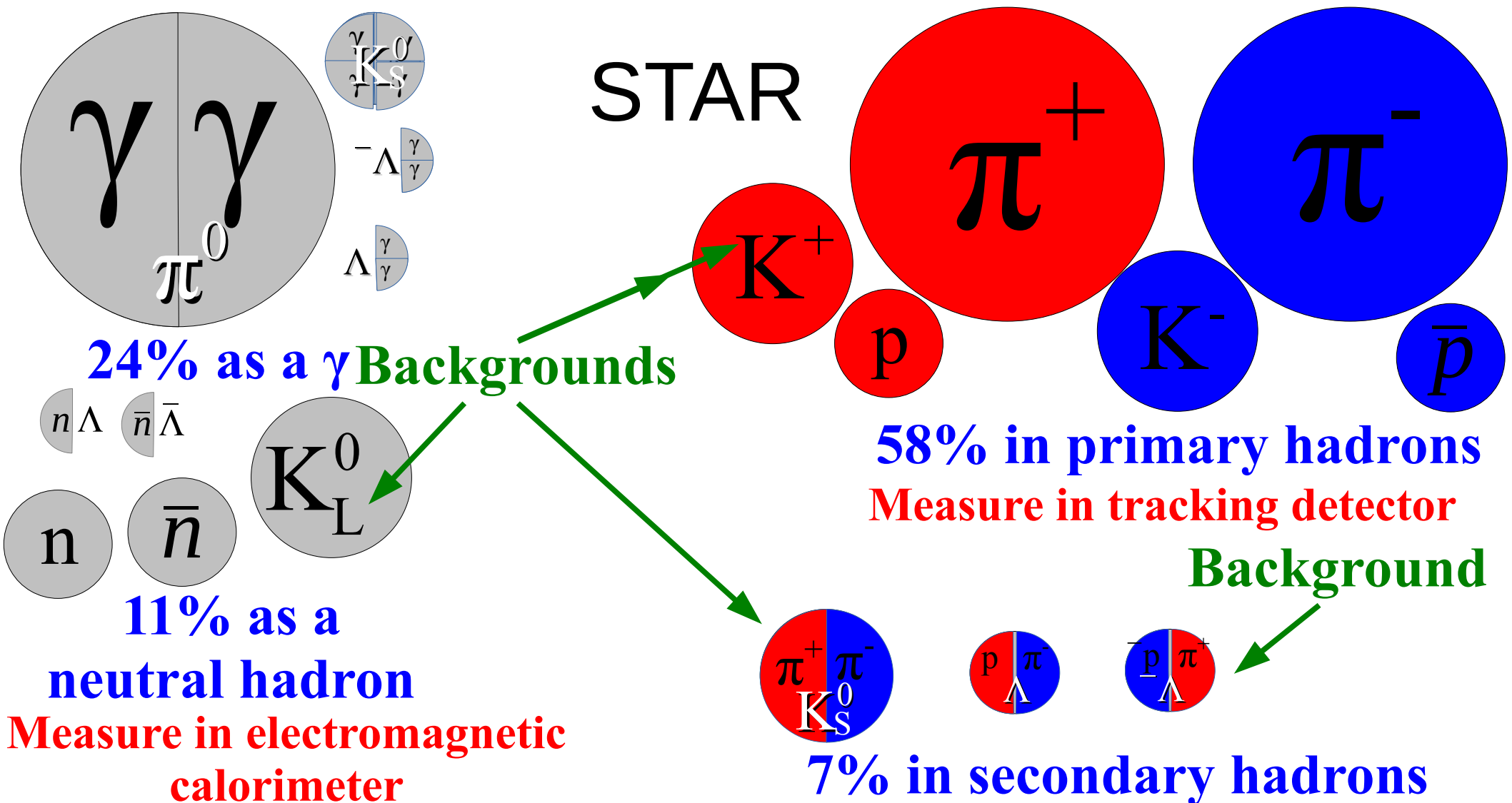
Tracks: $p_T > 900 \text{ MeV}/c$
 Clusters: limited by B
 $\rightarrow \sim 62\%$ of energy measured

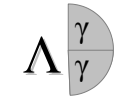
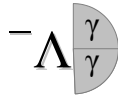
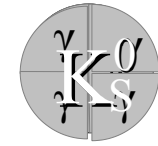
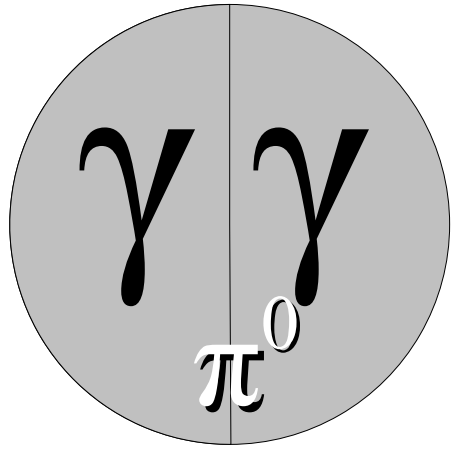


$\langle p_T \rangle \sim 700 \text{ MeV}/c$ $p_T (\text{GeV}/c)$

Phys. Lett. B 727 (2013) 371-380

Phys. Rev. Lett. 109, 252301 (2012)





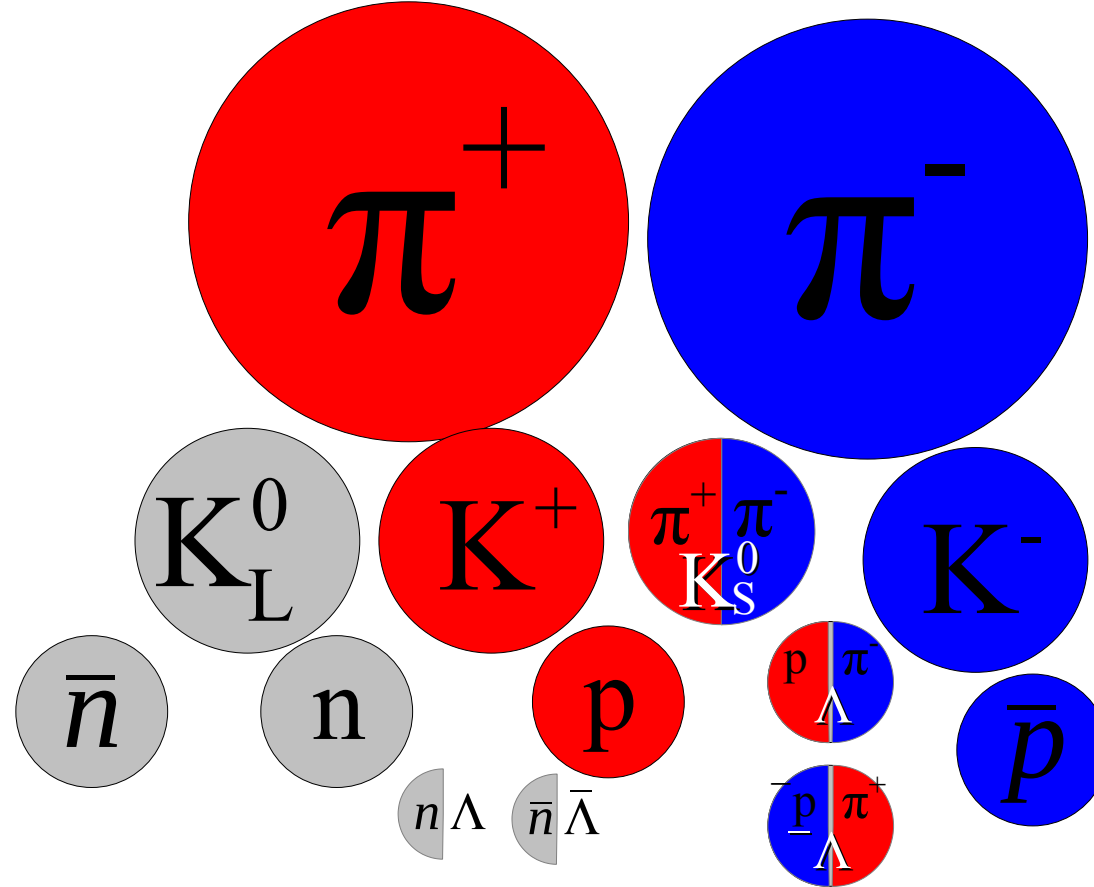
Deposit 100% of energy

35% of energy in event

PHENIX

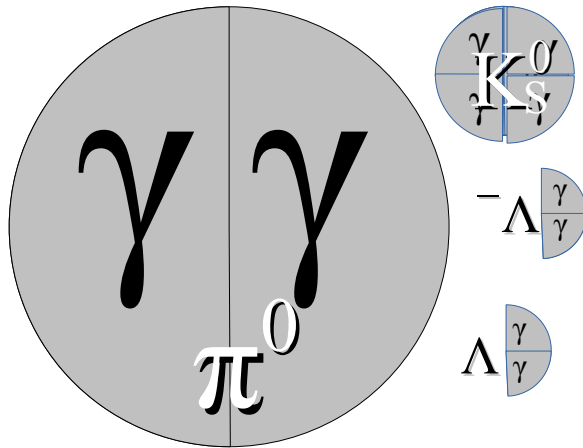
**Electromagnetic
calorimeter**

→ Measure ~57% of energy

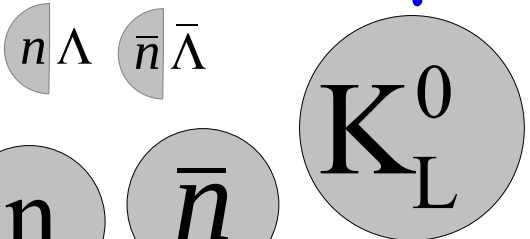


Deposit about 1/3 of energy

65% of energy in event

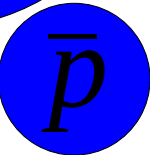
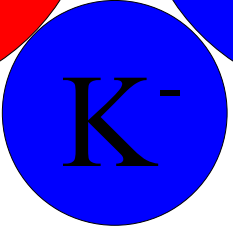
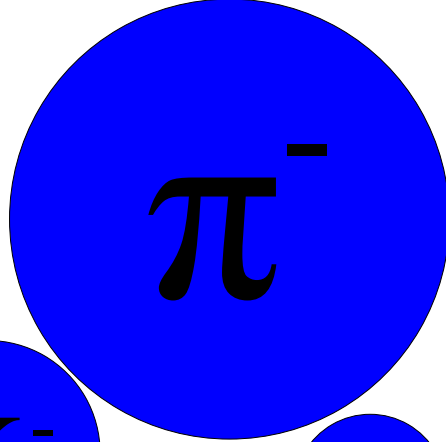
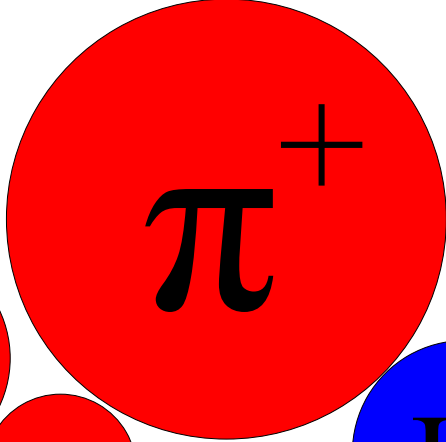
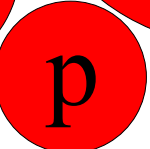
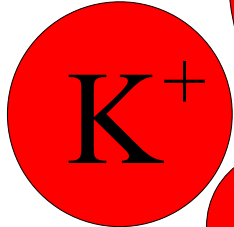


24% as a γ



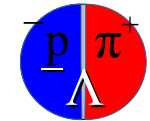
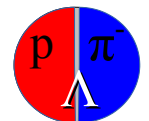
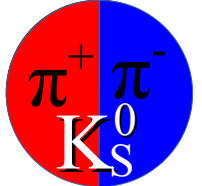
11% as a
neutral hadron
Don't measure

ALICE



Measure
~56%

58% in primary hadrons
Measure in tracking detector

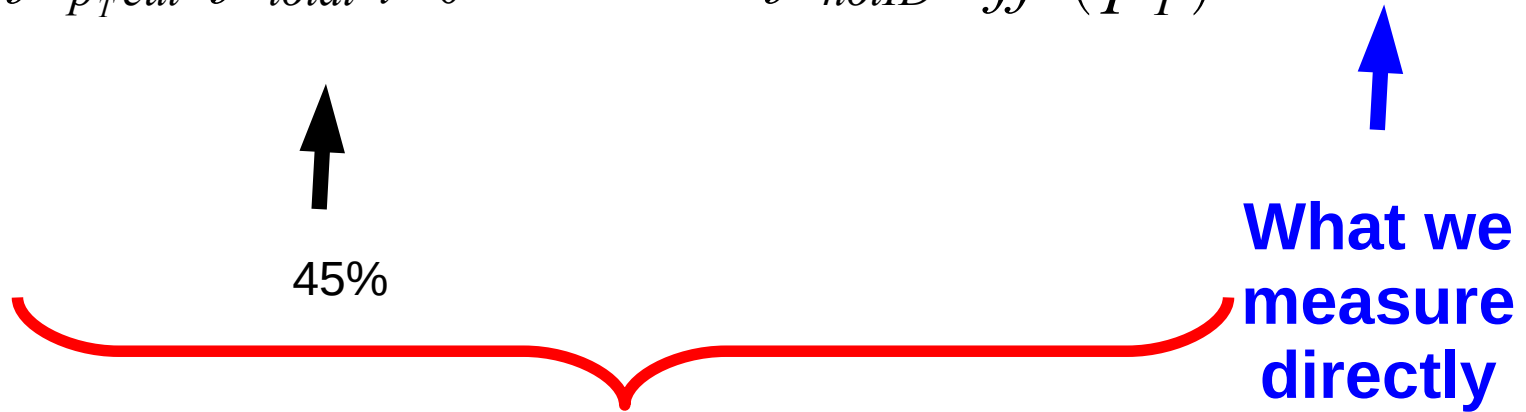


7% in secondary hadrons
Cut out using tight DCA cut

ALICE

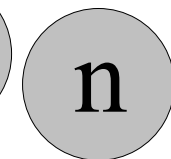
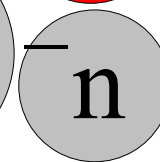
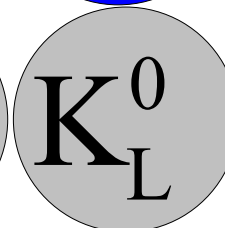
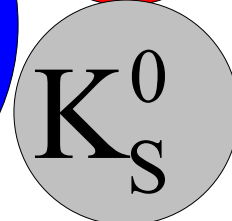
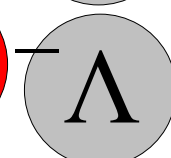
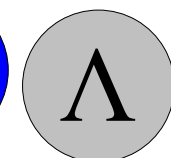
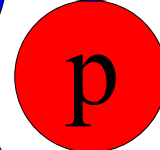
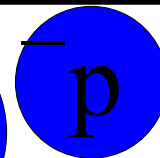
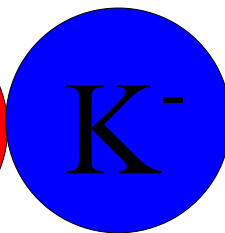
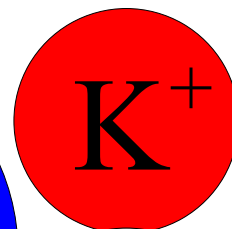
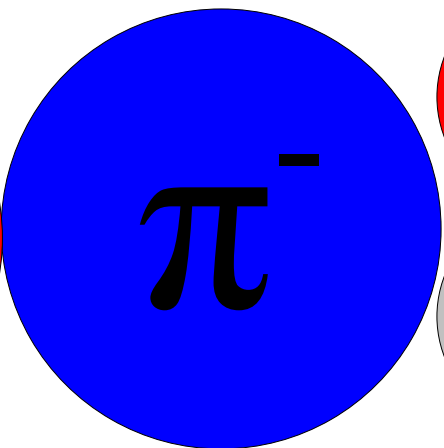
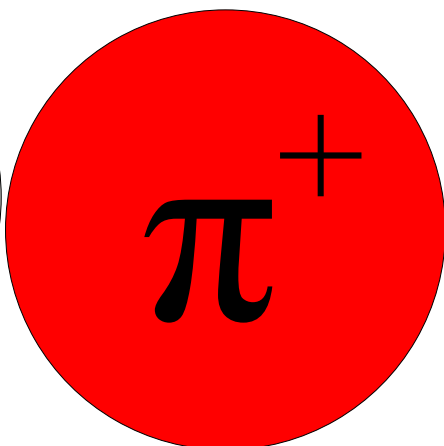
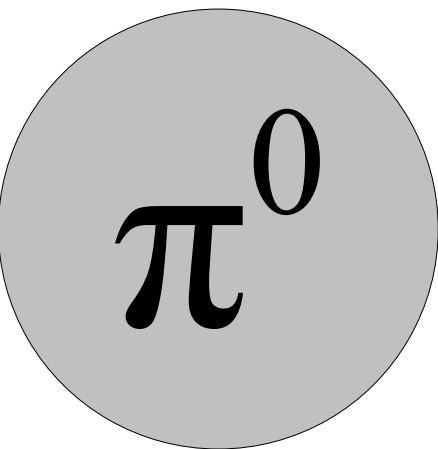
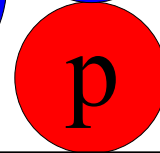
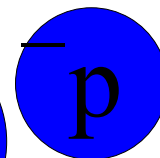
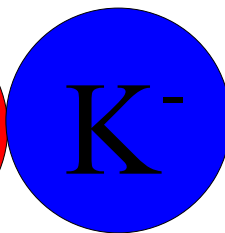
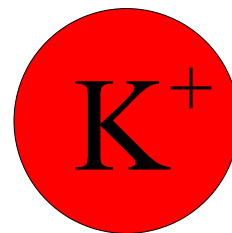
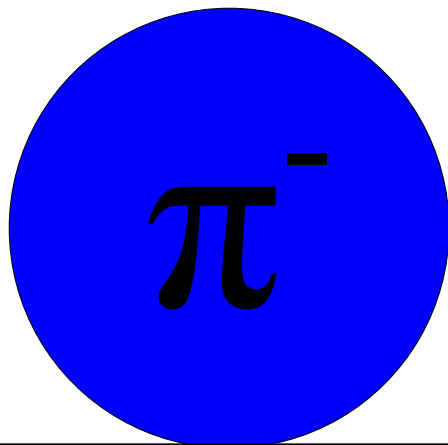
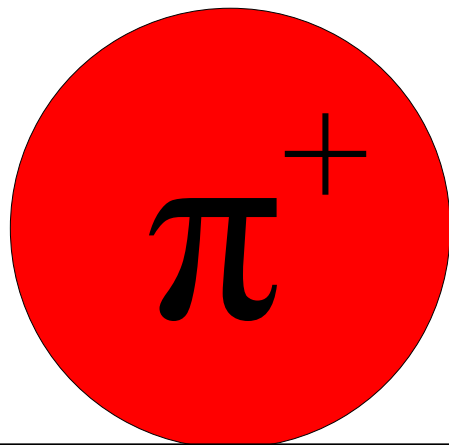
$$E_T = \frac{1}{f_{p_T \text{ cut}}} \frac{1}{f_{total}} \sum_{i=0}^n f_{bg}^i(p_T) \frac{1}{f_{notID}} \frac{1}{eff(p_T^i)} E_i \sin(\theta^i)$$

3% 2% 3% 40% But known well!

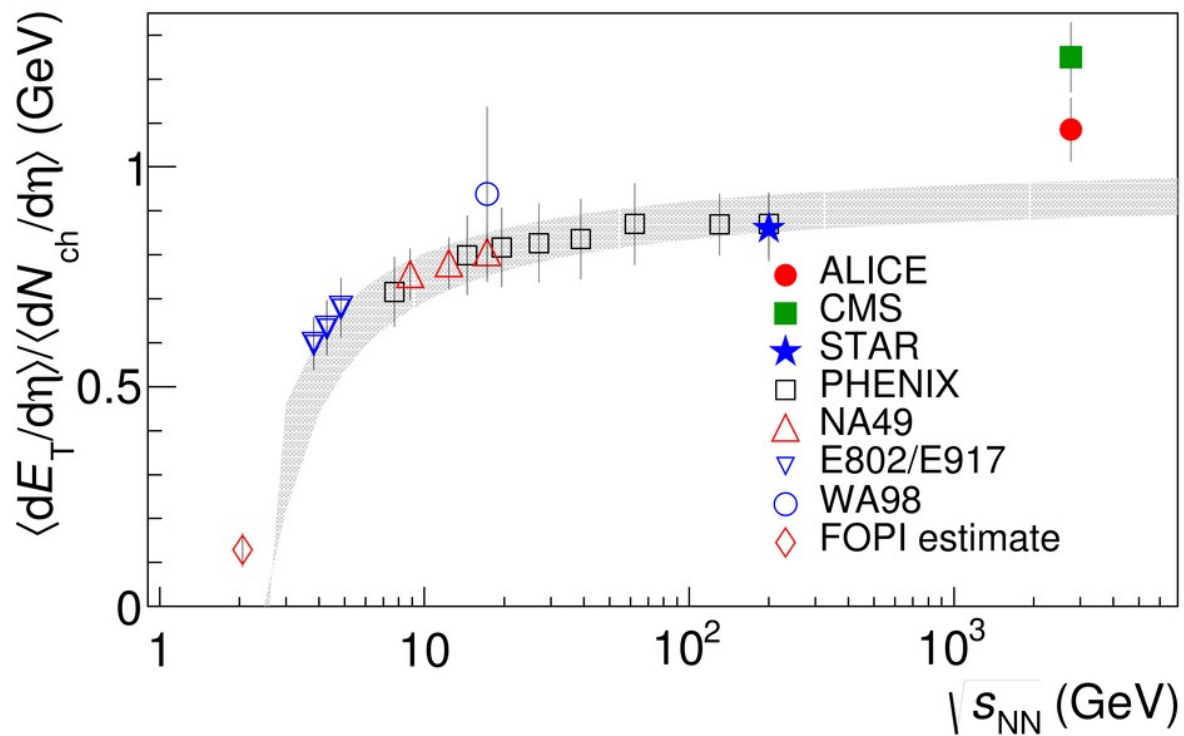


Corrections

ALICE: $f_{\text{total}} = 0.567 \pm 0.009$



ALICE E_T



Lambda correction f_Λ

- STAR BES DCA to $PV < 3$ cm
FeedException due to K_S^0 done
FeedException to p due to Λ not done
- STAR published spectra at $\sqrt{s_{NN}} = 200$ GeV
(Phys.Rev.Lett.97:152301,2006) with and without feedException*

→ Calculate E_T^Λ feedException

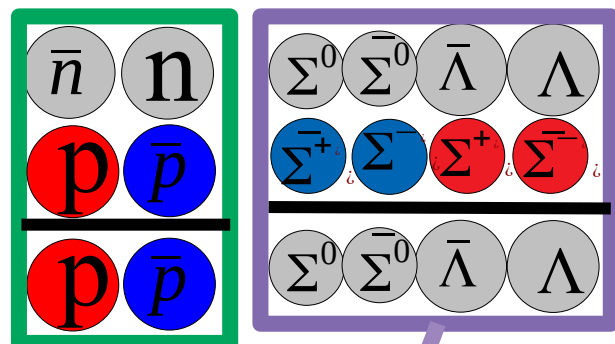
- Does not provide a lot of constraint

→ Use branching ratio

$$\rightarrow 0.68 \pm 0.32$$

$$f_\Lambda = 1.08 \pm 0.51$$

*Thanks to Ron Belmont for pointing this out to us



decay	$c\tau$ (cm)
$\Lambda \rightarrow p\pi^-$ (64%)	7.9
$\Lambda \rightarrow n\pi^0$ (36%)	
$K_S^0 \rightarrow \pi^+\pi^-$ (69%)	2.7
$K_S^0 \rightarrow \pi^0\pi^0$ (31%)	
$K_L^0 \rightarrow \pi^\pm e^\mp \nu_e$	1534

centrality	E_T^{fd} / E_T^Λ
0–12%	0.68 ± 0.18
10–20%	0.78 ± 0.22
20–40%	0.79 ± 0.2
40–60%	0.80 ± 0.21
60–80%	0.75 ± 0.27