Examples of 1D Motion
FIGURE 3.3

A professor paces left and right while lecturing. Her position relative to Earth is given by $x$. The +2.0-m displacement of the professor relative to Earth is represented by an arrow pointing to the right.
EXAMPLE 3.1
Velocity
Timeline of Jill’s movements.
This graph depicts Jill’s position versus time. The average velocity is the slope of a line connecting the initial and final points.
In a graph of position versus time, the instantaneous velocity is the slope of the tangent line at a given point. The average velocities between times $t_1$, $t_2$, $t_3$, and $t_4$ are shown. When $\Delta t \to 0$, the average velocity approaches the instantaneous velocity at $t_0$. 
The object starts out in the positive direction, stops for a short time, and then reverses direction, heading back toward the origin. Notice that the object comes to rest instantaneously, which would require an infinite force. Thus, the graph is an approximation of motion in the real world. (The concept of force is discussed in Newton’s Laws of Motion.)
The velocity is positive for the first part of the trip, zero when the object is stopped, and negative when the object reverses direction.
a) Position: $x(t)$ versus time.

b) Velocity: $v(t)$ versus time. The slope of the position graph is the velocity. A rough comparison of the slopes of the tangent lines in (a) at 0.25 s, 0.5 s, and 1.0 s with the values for velocity at the corresponding times indicates they are the same values.

c) Speed: $|v(t)|$ versus time. Speed is always a positive number.
Acceleration
An object in motion with a velocity vector toward the east under negative acceleration comes to a rest and reverses direction. It passes the origin going in the opposite direction after a long enough time.
Identify the coordinate system, the given information, and what you want to determine.
In a graph of velocity versus time, instantaneous acceleration is the slope of the tangent line.

a) Shown is average acceleration between times $t_1$ and $t_3$. When $\Delta t \to 0$, the average acceleration approaches instantaneous acceleration at time $t_0$. In view (a), instantaneous acceleration is shown for the point on the velocity curve at maximum velocity. At this point, instantaneous acceleration is the slope of the tangent line, which is zero. At any other time, the slope of the tangent line—and thus instantaneous acceleration—would not be zero.

b) Same as (a) but shown for instantaneous acceleration at minimum velocity.
The velocity-versus-time graph is linear and has a negative constant slope (a) that is equal to acceleration, shown in (b).
a) Velocity versus time. Tangent lines are indicated at times 1, 2, and 3 s. The slopes of the tangents lines are the accelerations. At $t = 3$ s, velocity is positive. At $t = 5$ s, velocity is negative, indicating the particle has reversed direction.

b) Acceleration versus time. Comparing the values of accelerations given by the black dots with the corresponding slopes of the tangent lines (slopes of lines through black dots) in (a), we see they are identical.
Acceleration Examples
Graphs of instantaneous acceleration versus time for two different one-dimensional motions.

a) Acceleration varies only slightly and is always in the same direction, since it is positive. The average over the interval is nearly the same as the acceleration at any given time.

b) Acceleration varies greatly, perhaps representing a package on a post office conveyor belt that is accelerated forward and backward as it bumps along. It is necessary to consider small time intervals (such as from 0–1.0 s) with constant or nearly constant acceleration in such a situation.
a) Velocity-versus-time graph with constant acceleration showing the initial and final velocities and . The average velocity is 60 km/h.

b) Velocity-versus-time graph with an acceleration that changes with time. The average velocity is not given by , but is greater than 60 km/h.
The airplane lands with an initial velocity of 70.0 m/s and slows to a final velocity of 10.0 m/s before heading for the terminal. Note the acceleration is negative because its direction is opposite to its velocity, which is positive.
Sketching
Velocity &
Acceleration
EXERCISE 46
EXERCISE 47

Velocity $v$

Time $t$

Points: a, b, c, d, e, f, g, h, i, j, k, l
Free Fall
A hammer and a feather fall with the same constant acceleration if air resistance is negligible. This is a general characteristic of gravity not unique to Earth, as astronaut David R. Scott demonstrated in 1971 on the Moon, where the acceleration from gravity is only 1.67 m/s² and there is no atmosphere.
The positions and velocities at 1-s intervals of a ball thrown downward from a tall building at 4.9 m/s.
A baseball hit straight up is caught by the catcher 5.0 s later.
A rocket releases its booster at a given height and velocity. How high and how fast does the booster go?
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