

Chapter 15

ACIDS, BASES

&

ACID/BASE EQUILIBRIA

Hill, Petrucci, McCreary & Perry 4th Ed.

ACIDS & BASES

The Arrhenius Definition: In Water:

- *Acid* – Substance which increases the concentration of Hydrogen Ion, $[H^+]$.
- *Base* – Substance which increases the concentration of Hydroxide Ion, $[OH^-]$.
- Strong Acids: H_2SO_4 , HI , HBr , HCl , HNO_3 , $HClO_4$.
- Strong Bases: Hydroxides of Li^+ , Na^+ , K^+ , Rb^+ , Cs^+ , Ba^{2+} , Sr^{2+} , Ca^{2+} .

ACIDS & BASES

The Bronsted-Lowry Definition: The B-L definition is *independent of solvent*.

• ***Acid*** – Substance which donates a Hydrogen Ion, H^+ .

• ***Base*** – Substance which accepts a Hydrogen Ion, H^+ .

• **Conjugate Acid Base Pairs: Species which differ by H^+ . Examples (Acid/Base):**

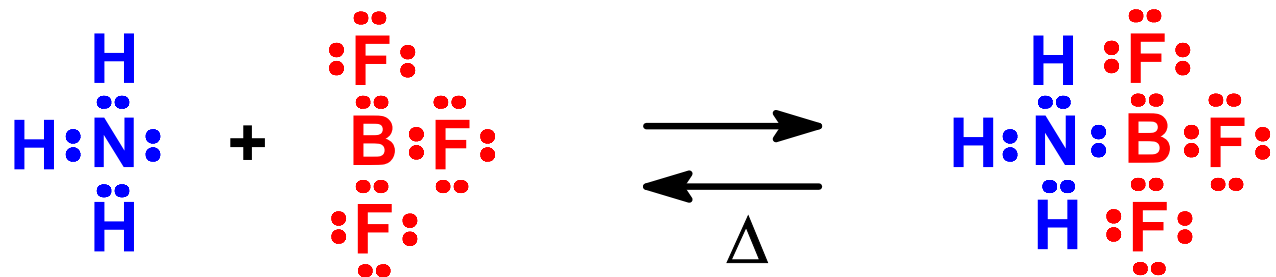
• **HCl/Cl⁻, NH₄⁺/NH₃, H₃O⁺/H₂O, H₂O/OH⁻**

ACIDS & BASES

• **The Lewis Definition:** The Lewis definition focuses on electrons and is *independent of solvent*.

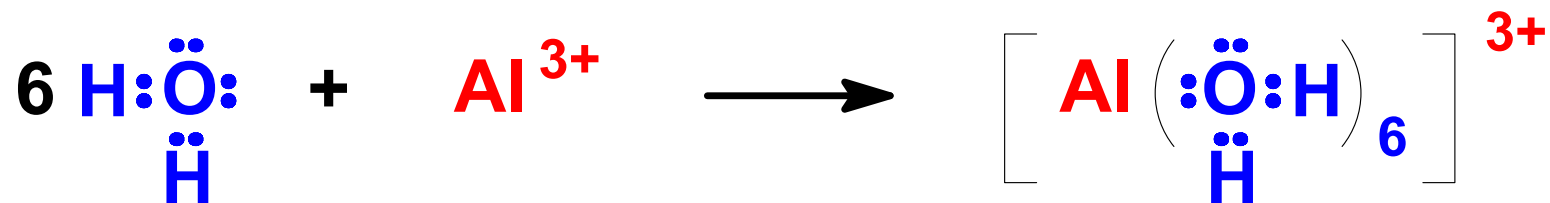
Acid – Substance which accepts an *electron pair*.

Base – Substance which donates an *electron pair*.



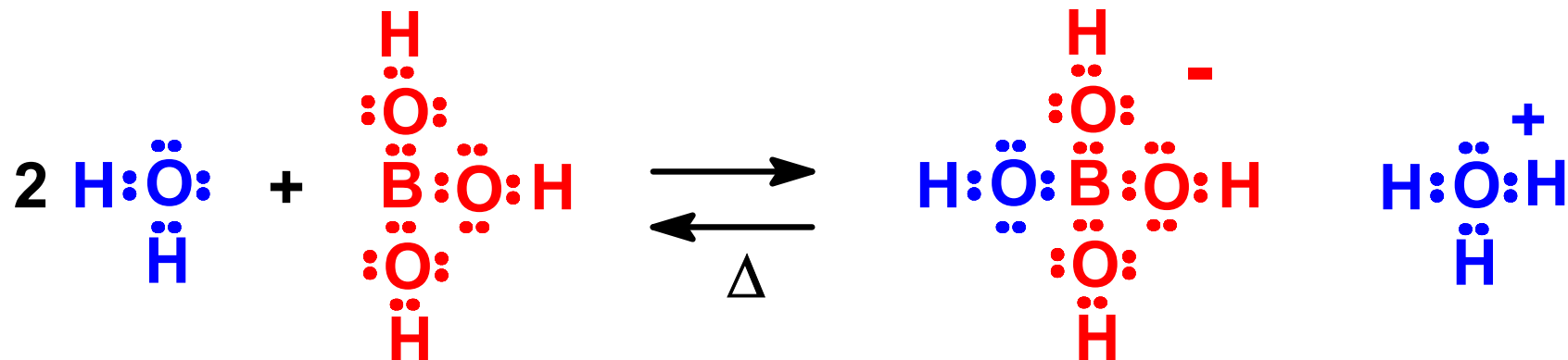
Other Lewis Acids

Many Metal Ions:



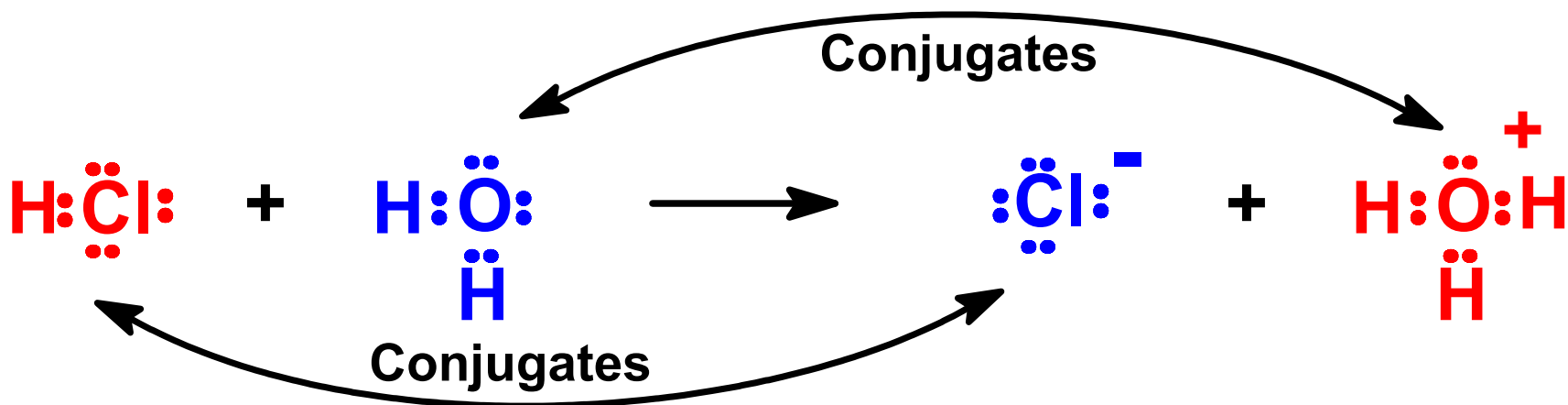
Some Acids are not what they seem: H_3BO_3

Boric Acid is not an Oxoacid, but a Lewis Acid:



Bronsted Acid/Base Reactions

A competition for Hydrogen Ion (Protons)



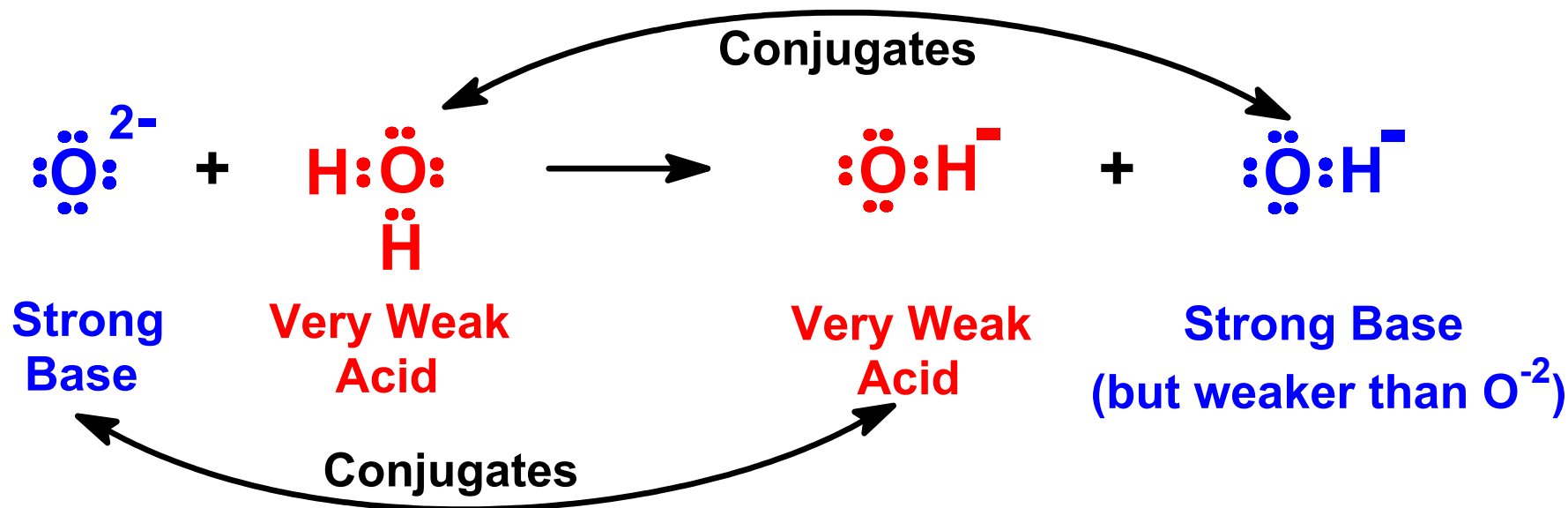
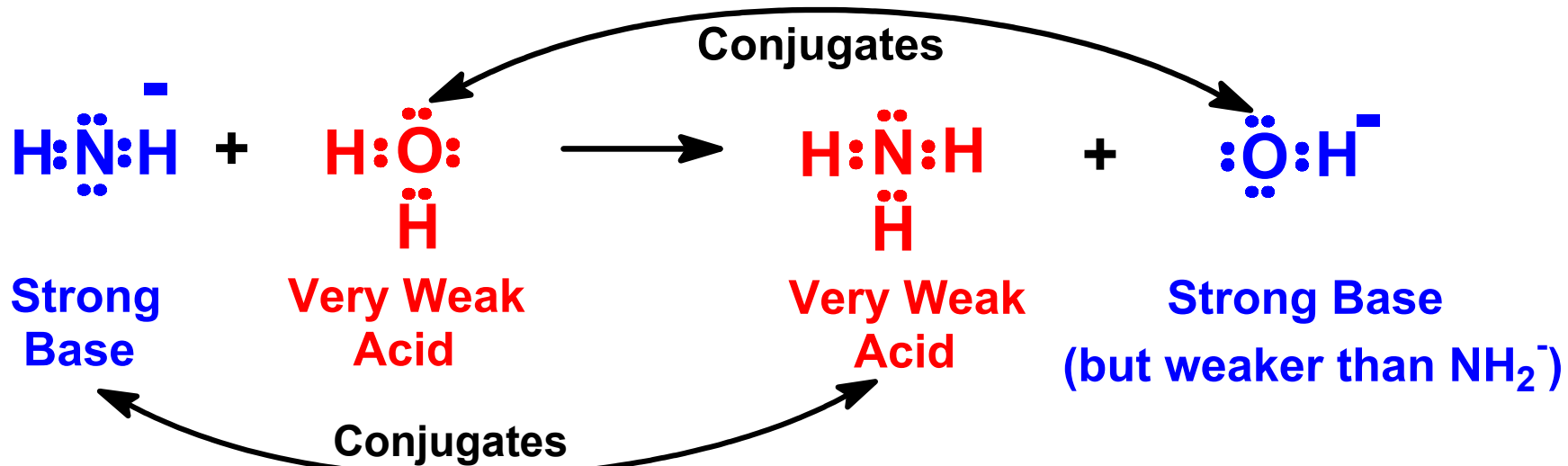
**Stronger
Acid
than
H₃O⁺**

**Stronger
Base
than
Cl⁻**

**Weaker
Base
than
H₂O**

**Weaker
Acid
than
HCl**

B/L Acids/Bases are Named by Function



B/L Acid/Base Strength Relationships

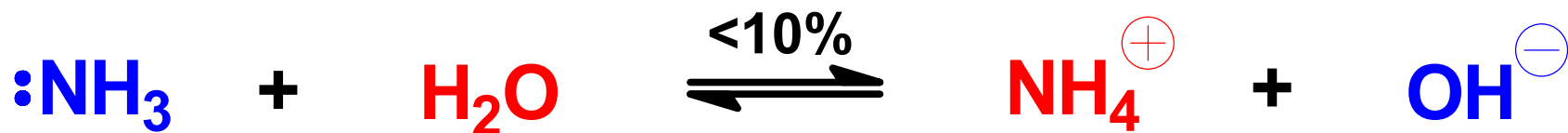
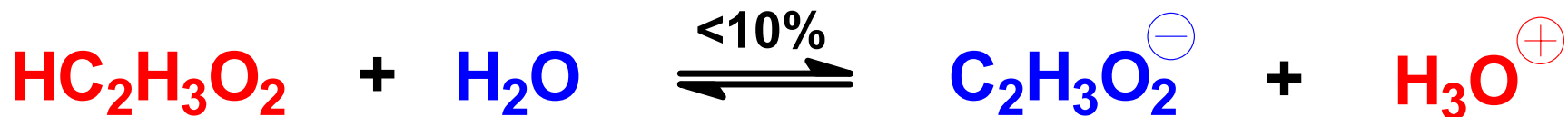
Strongest Acids \rightleftharpoons Weakest Conjugate Bases

Strongest Bases \rightleftharpoons Weakest Conjugate Acids

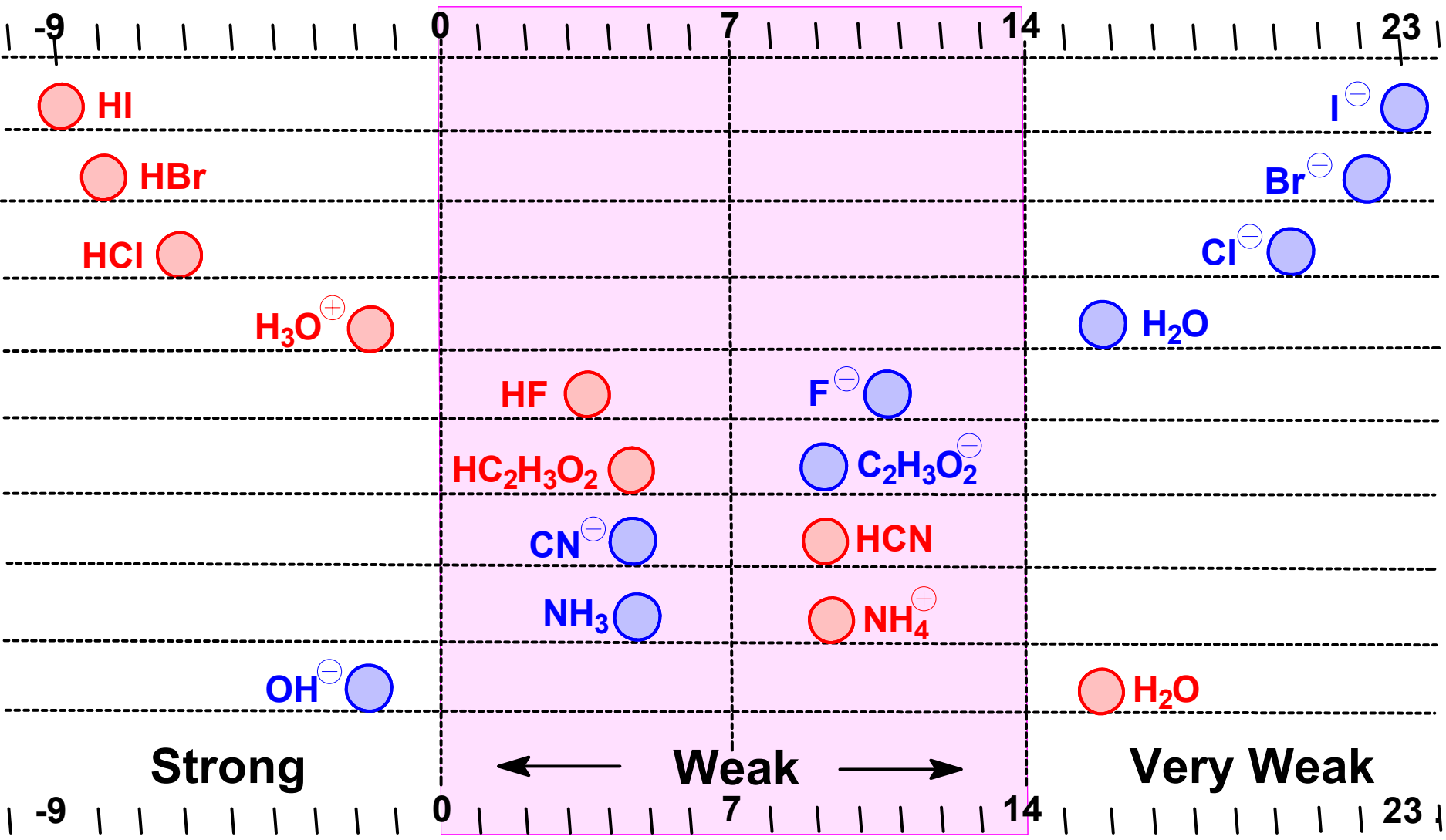
Weak Acids \rightleftharpoons Weak Conjugate Bases

Weak Acids/Bases have $\text{pK}_{\text{a/b}}$ between 2 & 12

Weak Acids & Weak Bases

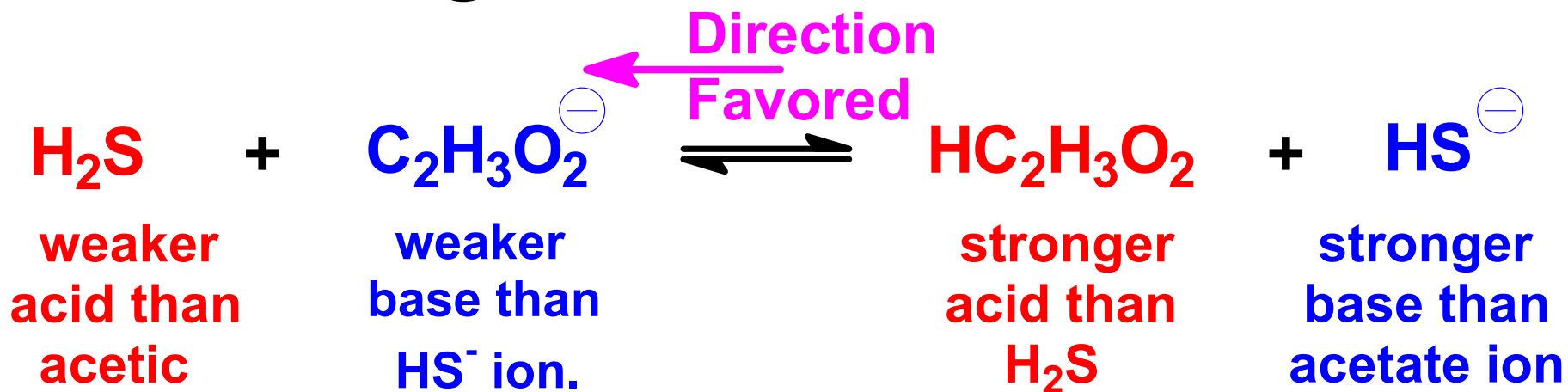


pK_a & pK_b of Conjugate Acid/Base Pairs



Competition for Protons

Determining the Direction of Reaction:

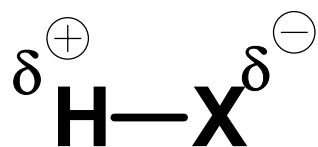


See Table 15.1, p 620, for Relative Acid/Base Strengths

The Hydrogen Sulfide Ion is a *stronger base* than the acetate ion and will successfully compete for the Hydrogen Ion.

Factors Affecting Acid Strength

1) **Polarity of the H-X Bond.** The more electronegative X is, the more polar is, more charge separation in, the bond.



Where δ^{\oplus} means not a full positive charge.

2) **Strength of the H-X Bond.** The stronger the bond the harder it is to ionize.



 This Bond must break to form ions!

Trends in Binary Acid Strength



Most **Polarity** **Least**
Greatest **Bond Strength** **Least**



In Water HF is a weak acid.

HCl, HBr and HI are strong acids.

Acidity Trends in Oxo-Acids

All Oxo-Acids contain H-O-X Bonds of near equal strength. The H-O Bond is strong!

Electronegativity Trends

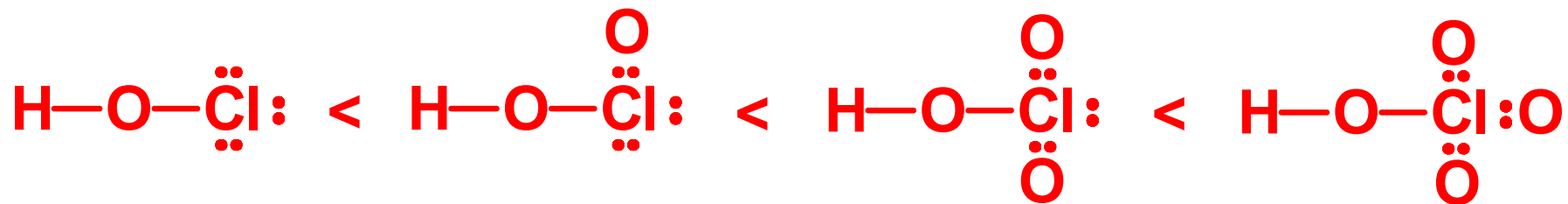


Oxygen Substitution is more important!

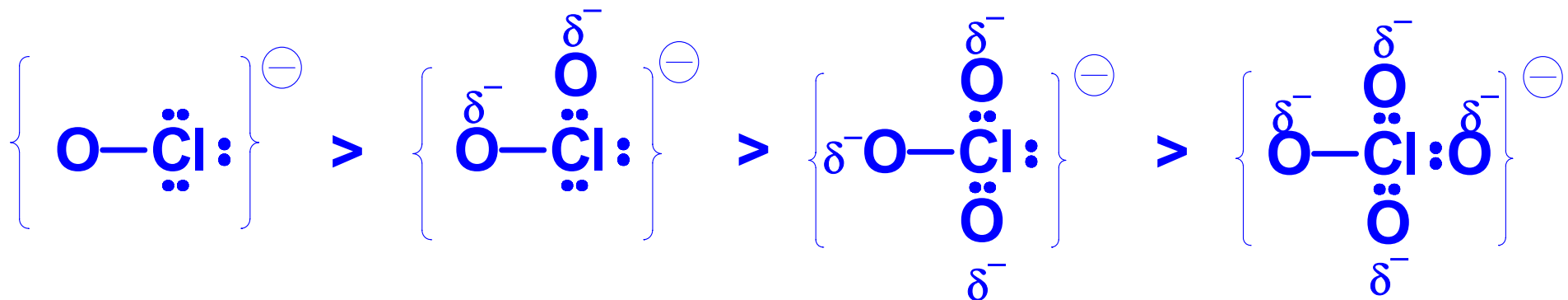


Acidity Trends in Oxo-Acids

Why Oxygen Substitution is more important!



The key is the Conjugate Base Strength!

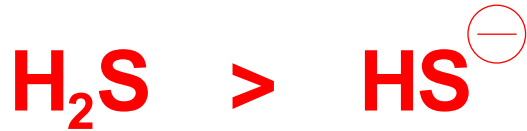


Each added Oxygen reduces the average charge!

POLYPROTIC ACIDS

More Than One Proton Ionizes

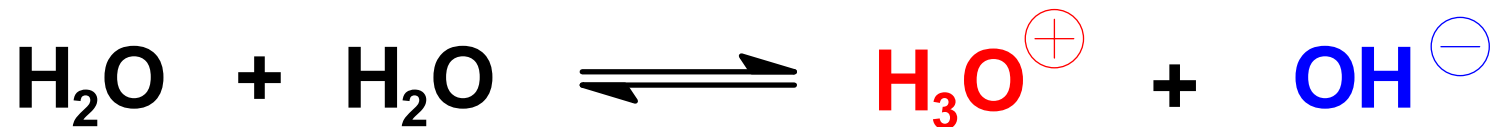
Binary Types:



Oxo-Acid Types:



The Auto-Ionization of Water



$$K_C = \frac{[\text{H}_3\text{O}^{\oplus}][\text{OH}^{\ominus}]}{[\text{H}_2\text{O}]^2} = 3.2 \times 10^{-18}$$

In dilute aqueous solution: $[\text{H}_2\text{O}] \approx \text{constant}$

$$[\text{H}_2\text{O}] = \frac{998 \text{ g/L}}{18.02 \text{ g/mol}} = 55.4 \text{ mol/L}$$

$$\begin{aligned} K_C [\text{H}_2\text{O}]^2 &= [\text{H}_3\text{O}^{\oplus}][\text{OH}^{\ominus}] \\ &= 3.2 \times 10^{-18} (55.4 \text{ mol/L})^2 \end{aligned}$$

$$K_C [\text{H}_2\text{O}]^2 \equiv K_W = [\text{H}_3\text{O}^{\oplus}][\text{OH}^{\ominus}] = \underline{\underline{1.0 \times 10^{-14}}}$$

Ion Product of Water

For Pure Water at 25° C:

$$[\text{H}_3\text{O}^+] = [\text{OH}^-] = 1.0 \times 10^{-7} \text{ M}$$

For Acid Solution:

$$[\text{H}_3\text{O}^+] \equiv [\text{H}^+] > 1.0 \times 10^{-7} \text{ M}$$

$$[\text{OH}^-] < 1.0 \times 10^{-7} \text{ M}$$

For Basic (Alkaline) Solution:

$$[\text{OH}^-] > 1.0 \times 10^{-7} \text{ M}$$

In all cases the

$$[\text{OH}^-] \times [\text{H}^+] = K_w$$

$$[\text{H}^+] < 1.0 \times 10^{-7} \text{ M}$$

pH: A Convenient Measure of $[H^+]$

$pH \equiv -\log [H^+]$ pH $[H^+]$ $[OH^-]$

Basic (Alkaline) Solution:

14	10^{-14}	1.0
13	10^{-13}	0.1

Neutral Solution:

7	10^{-7}	10^{-7}
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Acidic Solution:

1	0.1	10^{-13}
0	1.0	10^{-14}

$pOH \equiv -\log [OH^-]$

$pK_W \equiv -\log(K_W)$

$pK_W = 14.00$

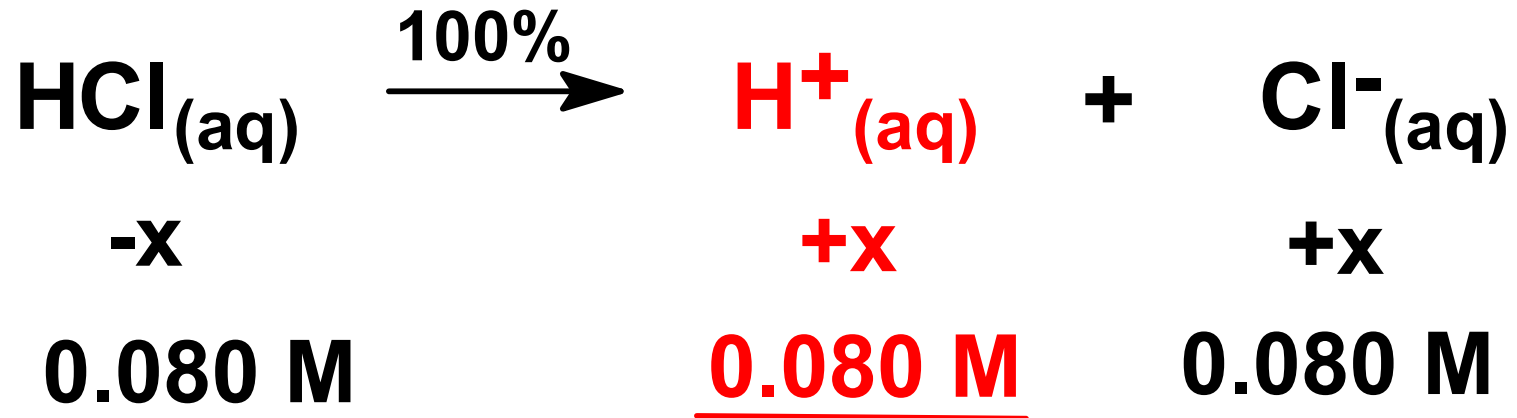
Some others
we will use
later.

$pK_a \equiv -\log(K_a)$

$pK_b \equiv -\log(K_b)$

Strong Acid Solution

A solution which is 0.080 M HCl:



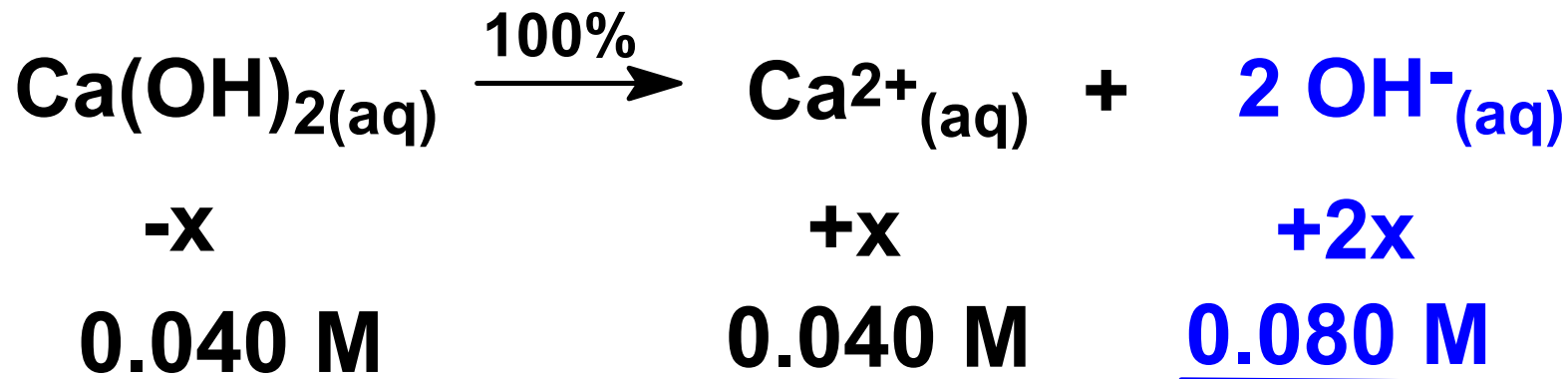
$$\text{pH} = -\log(0.080) = -(-1.10) = \underline{1.10}$$

$$[\text{OH}^-] = \frac{K_w}{0.080 \text{ M}} = \frac{1.0 \times 10^{-14}}{0.080 \text{ M}} = \underline{1.25 \times 10^{-13} \text{ M}}$$

$$\text{pOH} = -\log [\text{OH}^-] = -\log (1.25 \times 10^{-13}) = 12.90$$

A Strong Base Solution

A solution which is 0.040 M Ca(OH)_2 :



$$\text{pOH} = -\log(0.080) = -(-1.10) = \underline{1.10}$$

$$[\text{H}^+] = \frac{K_w}{0.080 \text{ M}} = \frac{1.0 \times 10^{-14}}{0.080 \text{ M}} = \underline{1.25 \times 10^{-13} \text{ M}}$$

$$\text{pH} = -\log(1.25 \times 10^{-13} \text{ M}) = -(-12.90)$$

$$\text{pH} = \underline{12.90}$$

Calculation of $[H^+]$ or $[OH^-]$ from pH
Orange juice has a pH of 3.54. Calculate the $[H^+]$ & $[OH^-]$. Note: $pH + pOH = 14.00$ (pK_w).

$$pH = 3.54 = -\log[H^+]$$

$$[H^+] = 10^{-3.54}$$

$$[H^+] = \underline{2.88 \times 10^{-4} \text{ M}}$$

Always change the sign of pH or pOH before taking the antilog.

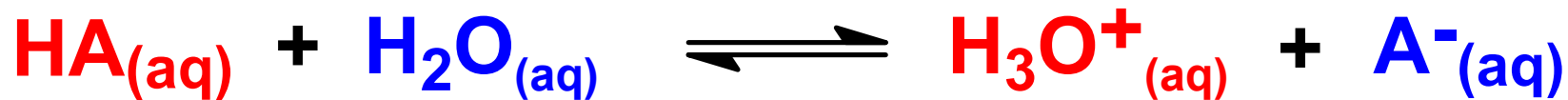
$$pOH = 14.00 - 3.54$$

$$pOH = 10.46$$

$$[OH^-] = 10^{-10.46}$$

$$[OH^-] = \underline{3.47 \times 10^{-11} \text{ M}}$$

Weak Acid Equilibria



$$K_c = \frac{[\text{H}_3\text{O}^+] [\text{A}^-]}{[\text{HA}] [\text{H}_2\text{O}]} \quad \text{but } [\text{H}_2\text{O}] \approx \text{constant!}$$

$$K_a \equiv K_c [\text{H}_2\text{O}] = \frac{[\text{H}_3\text{O}^+] [\text{A}^-]}{[\text{HA}]}$$

$$K_a \equiv \frac{[\text{H}^+] [\text{A}^-]}{[\text{HA}]}$$

Weak Acid Equilibria: 0.10 M HA in water



[initial] 0.10 M 0 M 0 M

Δ -x +x +x

[equil] 0.10 - x +x +x

$$K_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]} = \frac{(x)(x)}{(0.10 - x)}$$

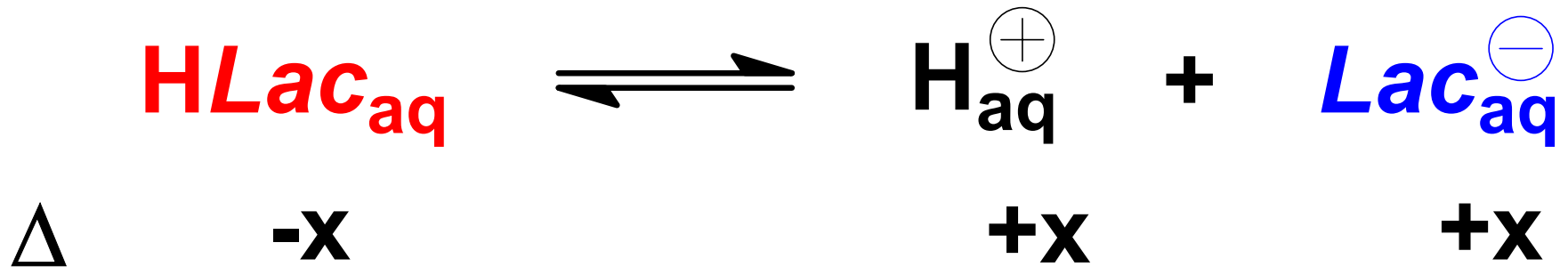
$$[\text{H}^+][\text{A}^-] = K_a [\text{HA}] \quad \text{but } [\text{H}^+] = [\text{A}^-]$$

$$[\text{H}^+] = \left(K_a [\text{HA}]_{\text{eq}} \right)^{\frac{1}{2}} \quad [\text{H}^+] \cong \left(K_a [\text{HA}]_{\text{init}} \right)^{\frac{1}{2}}$$

but $[\text{HA}] \gg x$, a weak acid

Calculation of the Ionization Constant, K_a , of a weak acid from a pH measurement.

A 0.025 M solution of Lactic Acid, $HLac$, has a $pH = 2.75$, calculate the K_a .

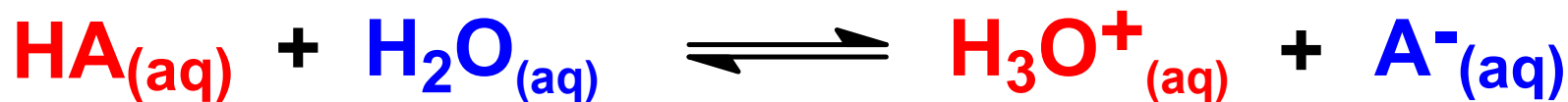


$$K_a = \frac{[H^{\oplus}] [Lac^{\ominus}]}{[HLac]}$$

Percent Ionization & Acid Concentration

Any weak acid (or base) dissociates to a greater extent as it becomes more dilute.

LeChatelier's Principle & the Common Ion Effect

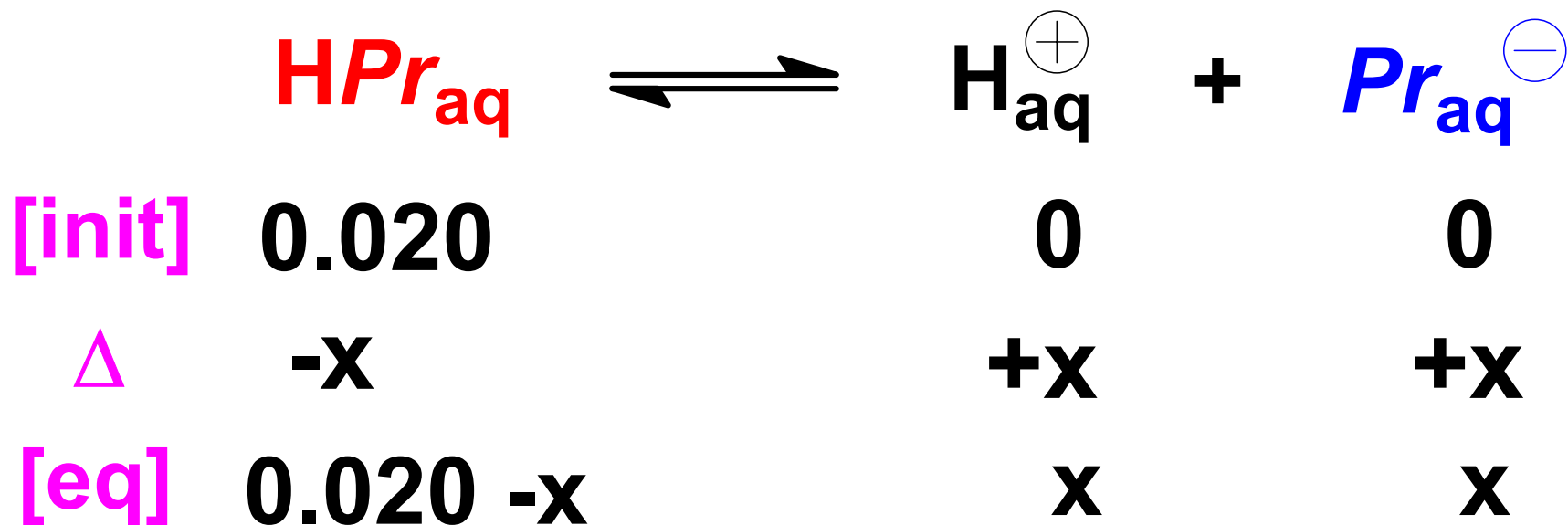


$$K_c = \frac{[\text{H}_3\text{O}^+][\text{A}^-]}{[\text{HA}][\text{H}_2\text{O}]}$$

as $[\text{H}_2\text{O}]$ increases and K_c remains constant the values of $[\text{H}_3\text{O}^+]$ & $[\text{A}^-]$ must increase and $[\text{HA}]$ must decrease!

Example: Weak acid Equilibrium

Calculate the Equilibrium Concentrations for 0.020 M propionic acid, $K_a = 1.3 \times 10^{-5}$



$$K_a = \frac{[H^{\oplus}][Pr^{\ominus}]}{[HPr]}$$

Solution:

$$K_a = \frac{[H^+][Pr^-]}{[HPr]} = \frac{(x)(x)}{(0.020 - x)} = 1.3 \times 10^{-5}$$

If $K_a/[HA] < 10^{-2}$
 $x \ll [HA]_{eq}$ and
 $[HA]_{eq} \approx [HA]_{initial}$

This equation will produce a quadratic unless we approximate. Errors less than 5% are acceptable.

$$K_a = \frac{(x)(x)}{(0.020 - x)} = 1.3 \times 10^{-5} \approx \frac{(x)(x)}{(0.020)}$$

a quadratic

not a quadratic

$$x = 5.0 \times 10^{-4}$$

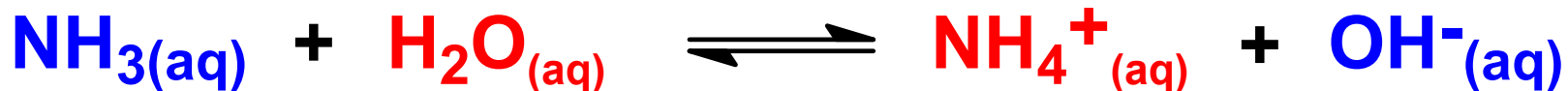
$$pH = 3.30$$

$$x = 5.1 \times 10^{-4}$$

$$pH = 3.29$$

\approx

Ionization Equilibria – Weak Bases



$$K_c = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3][\text{H}_2\text{O}]} \quad \text{but } [\text{H}_2\text{O}] \approx \text{constant!}$$

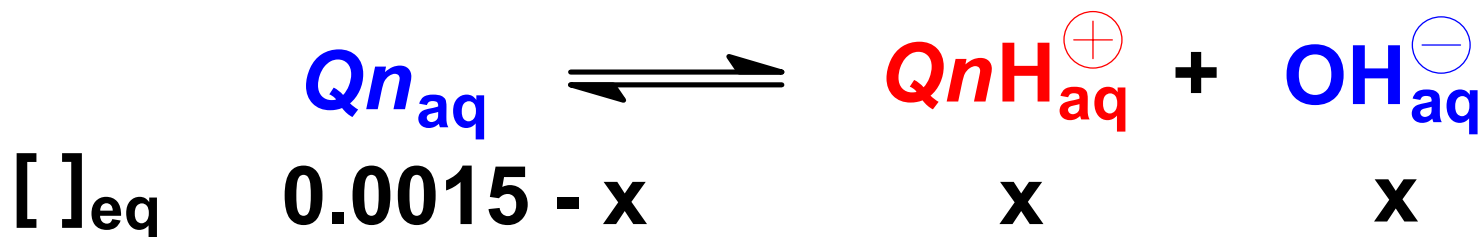
$$K_b \equiv K_c [\text{H}_2\text{O}] = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]}$$

$$K_b [\text{NH}_3] = [\text{NH}_4^+][\text{OH}^-] \quad \text{but: } [\text{NH}_4^+] = [\text{OH}^-]$$

$$[\text{OH}^-] = \left[K_b [\text{NH}_3]_{\text{eq}} \right]^{\frac{1}{2}} \approx \left[K_b [\text{NH}_3]_{\text{init}} \right]^{\frac{1}{2}}$$

Calculation of K_b from pH Measurements

A 0.0015 M solution of Quinine, Qn , has a pH = 9.84. Calculate the K_b for quinine.



$$[QnH^{\oplus}] = [OH^{\ominus}] = 10^{-\underbrace{(14.00 - 9.84)}_{pOH}} = 10^{-4.16}$$

$$[QnH^{\oplus}] = [OH^{\ominus}] = 6.92 \times 10^{-5} \text{ M}$$

$$K_b = \frac{[QnH^{\oplus}][OH^{\ominus}]}{[Qn]} = \frac{(6.92 \times 10^{-5})(6.92 \times 10^{-5})}{(0.0015 - 6.92 \times 10^{-5})}$$

$$K_b = \frac{(6.92 \times 10^{-5})^2}{(0.0015 - 0.00007)} = \underline{\underline{3.2 \times 10^{-6}}}$$

Acid/Base Properties of Salts

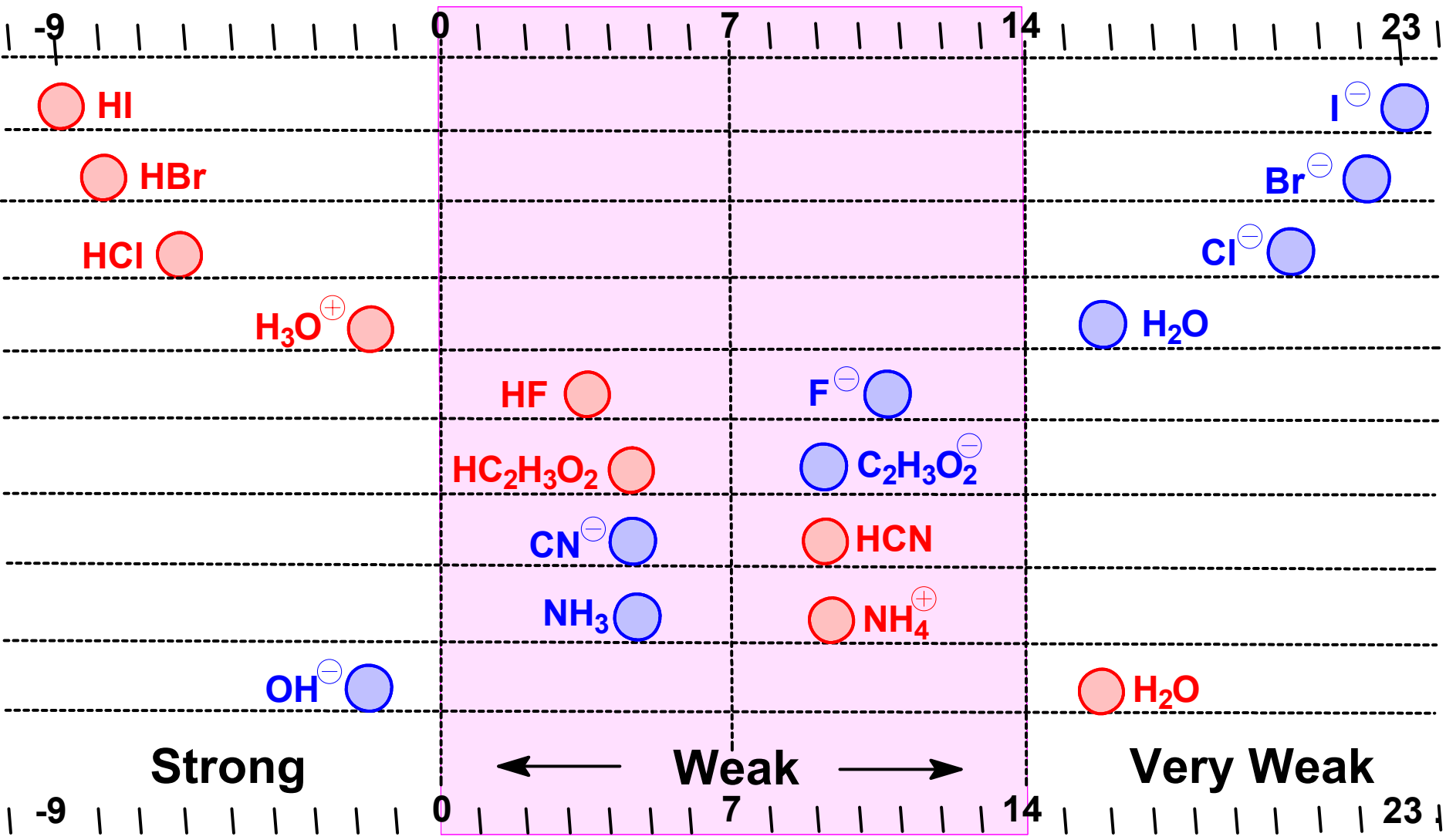
Hydrolysis of Salts

Salts of SA/SB are *neutral*. Both the conjugate base/acid are very weak *neither the conjugate acid or base alter* $\text{pH} = 7.00$.

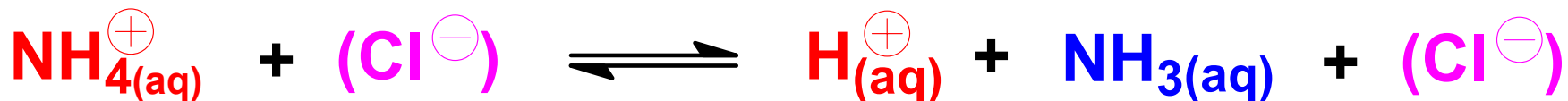
Salts of SA/WB are *acidic*. The *conjugate acid of the weak base* makes $\text{pH} < 7.00$.

Salts of WA/SB are *basic*. The *conjugate base of the weak acid* makes the $\text{pH} > 7.00$

pK_a & pK_b of Conjugate Acid/Base Pairs



Calculate the pH of 0.10 M Ammonium Chloride



$$0.10 - x$$

$$x$$

$$x$$

$$K_a = \frac{[\text{NH}_3][\text{H}^+]}{[\text{NH}_4^+]} = \frac{K_w}{K_b} = \frac{1.0 \times 10^{-14}}{1.8 \times 10^{-5}}$$

$$K_a = 5.6 \times 10^{-10} = \frac{(x)(x)}{0.10 - x} \approx \frac{x^2}{0.10}$$

$$[\text{H}^+] = x = \left[(5.6 \times 10^{-10})(0.10) \right]^{\frac{1}{2}} = \underline{\underline{7.5 \times 10^{-6} \text{ M}}}$$

$$\text{pH} = \underline{\underline{5.13}} \quad \text{an acidic solution!}$$

Salts of a Weak Acid / Strong Base

Calculate the pH of 0.10 M Sodium Cyanide

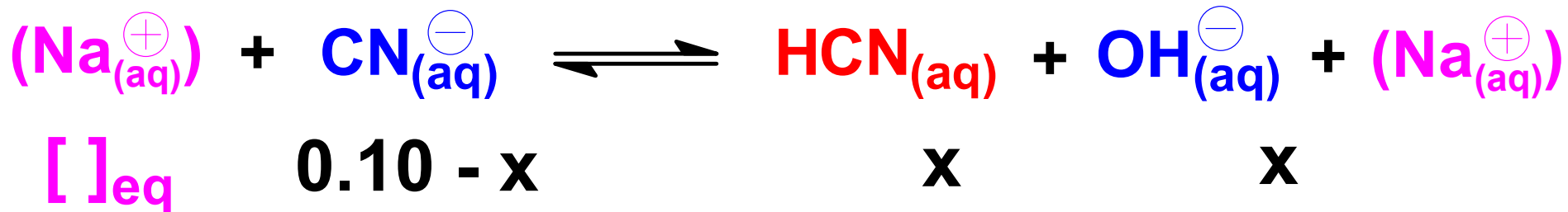


$$K_b = \frac{[\text{HCN}][\text{OH}^-]}{[\text{CN}^-]} \times \left\{ \frac{[\text{H}^+]}{[\text{H}^+]} \right\}$$

$$K_b = \frac{[\text{HCN}]}{[\text{CN}^-][\text{H}^+]} \frac{[\text{H}^+][\text{OH}^-]}{1} = \frac{K_w}{K_a} = \frac{1.0 \times 10^{-14}}{6.2 \times 10^{-10}}$$

$$K_b = 1.6 \times 10^{-5}$$

Calculate the pH of 0.10 M Sodium Cyanide



$$K_b = \frac{[\text{HCN}][\text{OH}^-]}{[\text{CN}^-]} = 1.6 \times 10^{-5}$$

$$K_b = 1.6 \times 10^{-5} = \frac{(x)(x)}{0.10 - x} \approx \frac{x^2}{0.10}$$

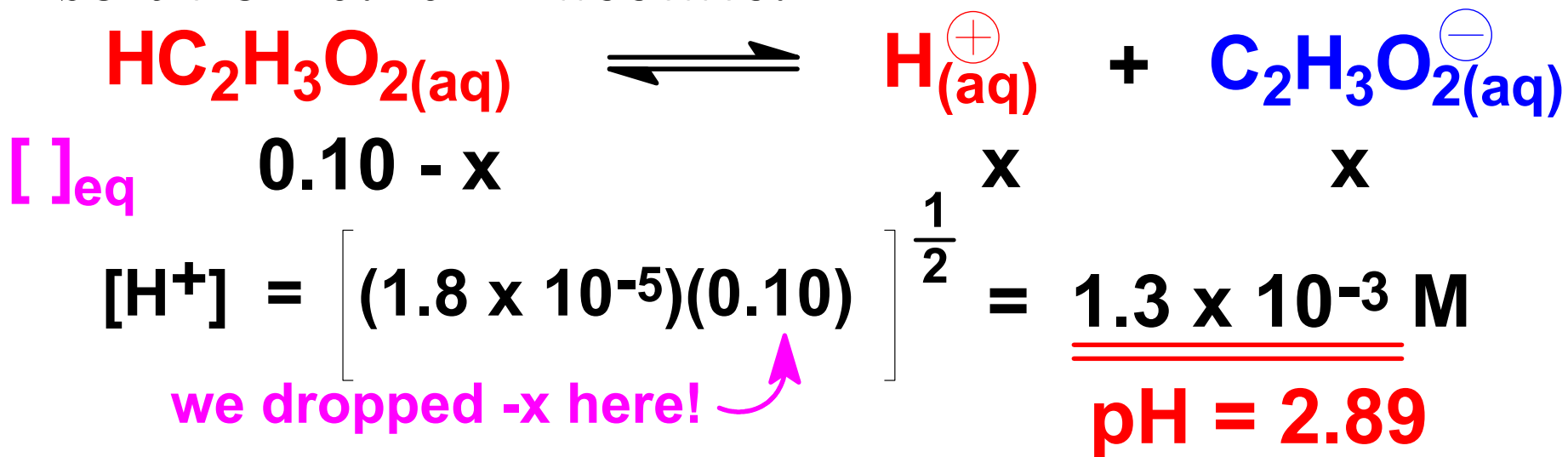
$$[\text{OH}^-] = x = \left[(1.6 \times 10^{-5})(0.10) \right]^{\frac{1}{2}} = \underline{1.3 \times 10^{-3} \text{ M}}$$

pOH = 2.9

$$\text{pH} = 14.0 - 2.9 = \underline{\underline{11.1}} \text{ a basic solution!}$$

The Common Ion Effect:

Calculate the pH of a 0.10 M acetic acid solution, then add enough dry sodium acetate to make the solution 0.10 M acetate.

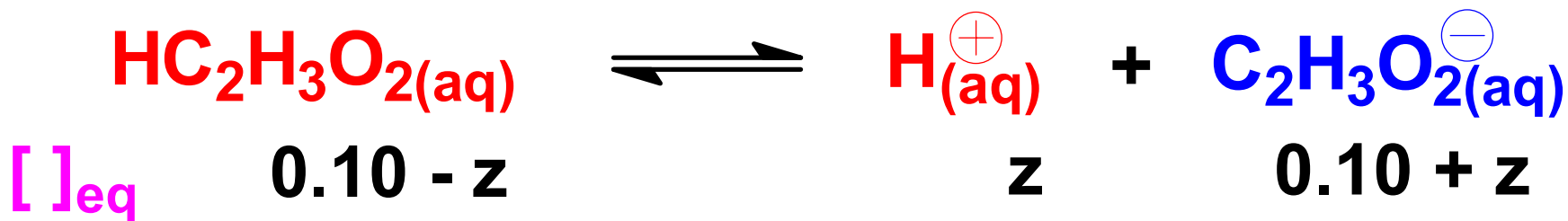


When we add the base and common ion acetate we will suppress the ionization of acetic acid!



The new dissociation z is a lot smaller than x .

Now calculate the pH of a 0.10 M acetic acid solution after adding the dry sodium acetate to make the solution 0.10 M in acetate. 1



we can drop +z here!

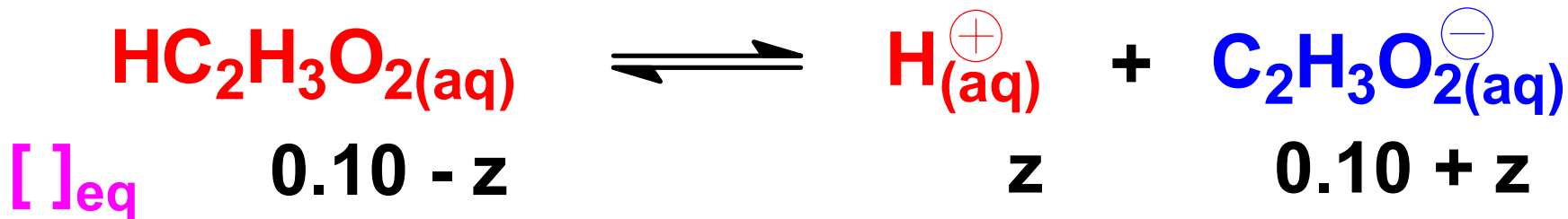
$$K_a = \frac{[\text{H}^+][\text{C}_2\text{H}_3\text{O}_2^-]}{[\text{HC}_2\text{H}_3\text{O}_2]} = \frac{(z)(0.10 + z)}{(0.10 - z)}$$


we can drop -z here!

Solving for $[\text{H}^+]$:

$$[\text{H}^+] = \frac{K_a [\text{HC}_2\text{H}_3\text{O}_2]}{[\text{C}_2\text{H}_3\text{O}_2^-]} = \left[\frac{(1.8 \times 10^{-5})(0.10 - z)}{(0.10 + z)} \right]$$

Calculate the pH of a 0.10 M acetic acid solution, then add enough dry sodium acetate to make the solution 0.10 M acetate. 2



we dropped -z here! 

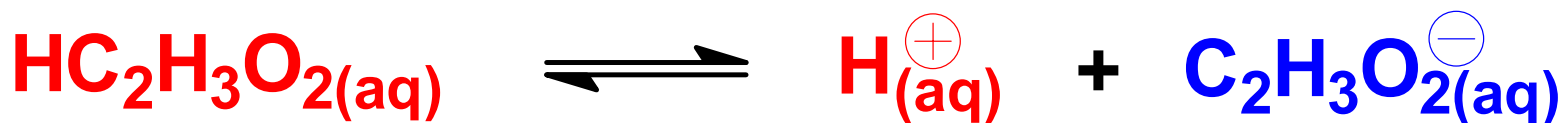
$$[\text{H}^+] = \left[\frac{(1.8 \times 10^{-5})(0.10 - z)}{(0.10 + z)} \right] \approx \left[\frac{(1.8 \times 10^{-5})(0.10)}{(0.10)} \right]$$

we dropped +z here! 

$$[\text{H}^+] = \underline{\underline{1.8 \times 10^{-5} \text{ M}}} \quad \text{pH} = 4.75$$

Compare this to just the weak acid! pH = 2.89

Buffers the “How” to Control pH



[]_{eq}

0.10 - x

x

x

this amount of acid
will absorb a lot of
hydroxide ion.

this amount of base
will not absorb a lot
of hydrogen ion.

If we add the conjugate base the solution will absorb both!

[]_{eq}

0.10 - z

z

0.10 + z

these amounts of both conjugates will absorb
comparable amounts of hydrogen or hydroxide ion.

$$[\text{H}^+] = \left[\frac{K_a (0.10)}{(0.10)} \right] = K_a = \underline{\underline{1.8 \times 10^{-5} \text{ M}}}$$

$$\text{pH} = 4.75 = \text{p}K_a$$

The Henderson Hasselbalch Equation



$$[\text{H}^+] = \left[\frac{K_a [\text{HA}]}{[\text{A}^-]} \right] \quad \text{or} \quad \text{pH} = \text{pKa} - \log \left[\frac{[\text{HA}]}{[\text{A}^-]} \right]$$

$$\text{pH} = \text{pKa} + \log \left[\frac{[\text{A}^-]}{[\text{HA}]} \right]$$

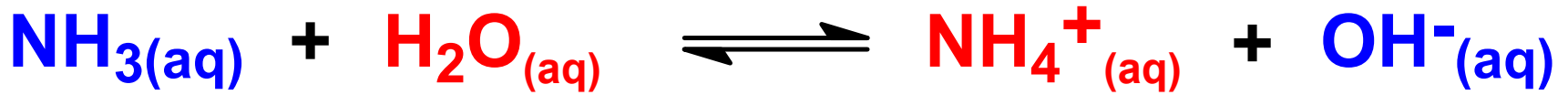
This equation will work for
an acid or base buffer!

or

$$\text{pH} = \text{pKa} + \log \left[\frac{[\text{CB}]}{[\text{CA}]} \right]$$

But it will only work when $[\text{CB}] \approx [\text{CA}]!!$

Buffers the “How” to Control pH



$$K_b = \frac{[\text{OH}^-][\text{NH}_4^+]}{[\text{NH}_3]} \quad [\text{H}^+] = K_a \frac{[\text{NH}_4^+]}{[\text{NH}_3]}$$

$$K_a = \frac{K_w}{K_b} = \frac{[\text{OH}^-][\text{H}^+][\text{NH}_3]}{[\text{OH}^-][\text{NH}_4^+]} = \frac{[\text{H}^+][\text{NH}_3]}{[\text{NH}_4^+]}$$

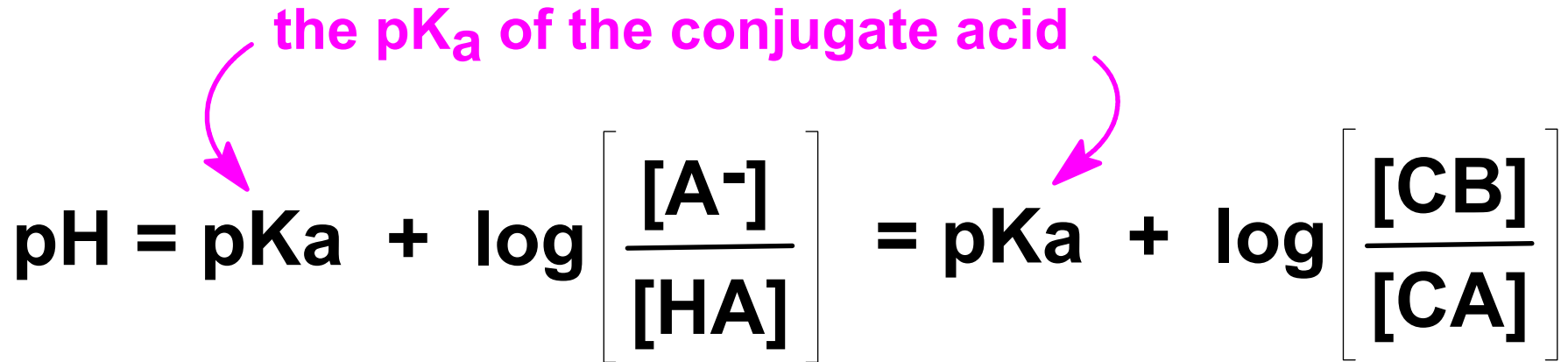
The Henderson Hasselbalch Equation

the pK_a of the conjugate acid

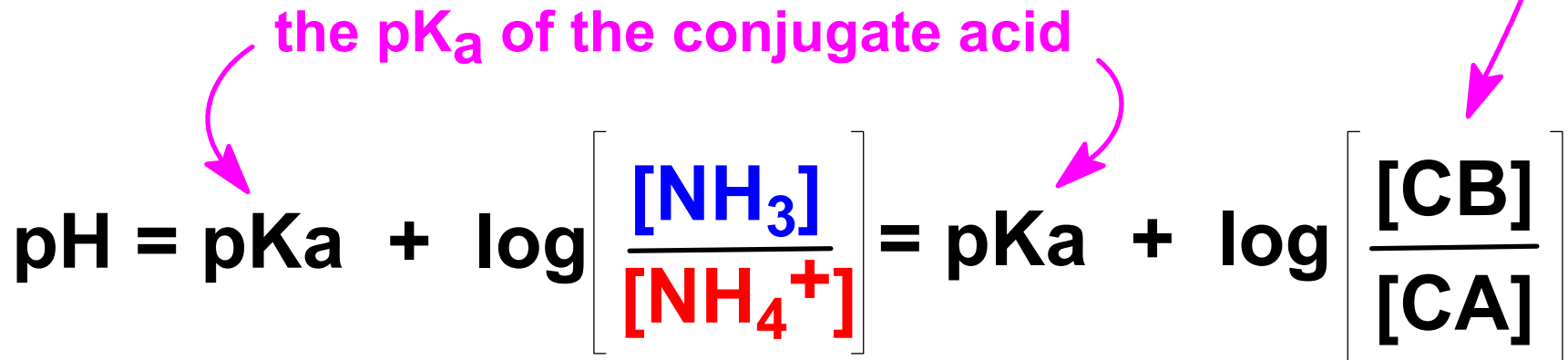
$$\text{pH} = \text{pK}_a + \log \left[\frac{[\text{NH}_3]}{[\text{NH}_4^+]} \right] = \text{pK}_a + \log \left[\frac{[\text{CB}]}{[\text{CA}]} \right]$$

This equation will work for an acid or base buffer!

Buffers Change pH only to the Extent that the Conjugate Ratios Change.



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Adding acid will cause NH_3 to react to form more NH_4^+

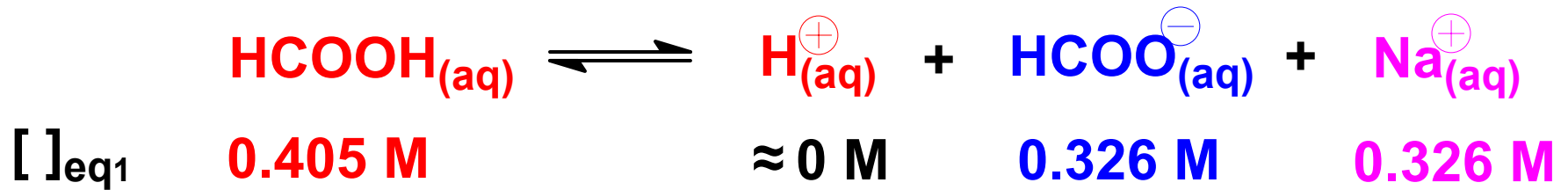
Adding base will cause NH_4^+ to react to form more NH_3

$$[\text{H}^+] = K_a \frac{[\text{NH}_4^+]}{[\text{NH}_3]} \Rightarrow \text{pH} = \text{pK}_a + \log \left[\frac{[\text{NH}_3]}{[\text{NH}_4^+]} \right]$$

Determining the pH of a buffer to which acid or base is added is a problem in stoichiometry and calculating the new conjugate ratio!

Challenging a Buffer

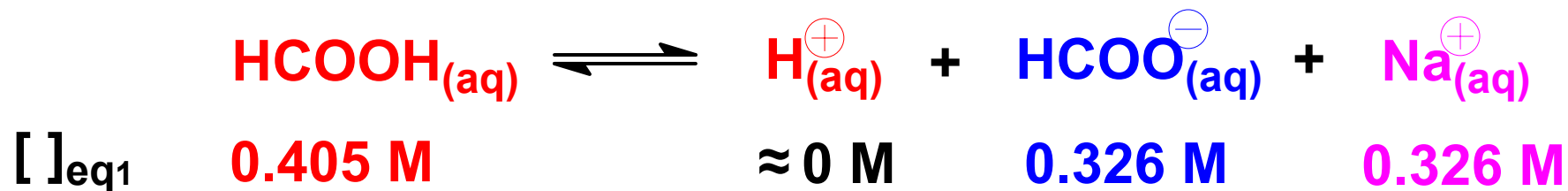
15-81: A solution 0.405 M in HCOOH and 0.326 M in HCOO⁻ is prepared. What is its pH?



15-85: To 50.0 mL of the above buffer is added 1.00 mL of 0.250 M HCl. What is the new pH?

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Titration of Acids and Bases

- The quantitative addition of an acid solution to a base solution until the *equivalence point* is reached.
- At the equivalence point the following equation applies:

Moles Acid = Moles Base

$$\text{Vol}_{\text{Acid}} \times M_{\text{Acid}} = \text{Vol}_{\text{Base}} \times M_{\text{Base}}$$



Titrating a Weak Base with Strong Acid

Calculate the volume of 0.052 M HCl required to titrate 32.0 mL of 0.077 M ammonia. Calculate pH at endpoint.



moles acid = moles base (at equivalence point)